

# A Formalised Theory of Turing Machines in Isabelle/HOL

Xu Jian, Xingyuan Zhang  
*PLA University of Science and Technology Nanjing, China*

Christian Urban  
*King's College London, UK*

**Abstract**—Isabelle/HOL is an interactive theorem prover based on classical logic. While classical reasoning allow users to take convenient shortcuts in some proofs, it precludes *direct* reasoning about decidability: every boolean predicate is either true or false because of the law of excluded middle. The only way to reason about decidability in a classical theorem prover, like Isabelle/HOL, is to formalise a concrete model for computation. In this paper we formalise Turing machines and relate them to register machines.

**Keywords**-Turing Machines, Decidability, Isabelle/HOL;

## I. INTRODUCTION

Norrish choose the  $\lambda$ -calculus as a starting point for his formalisation, because of its “simplicity” [Norrish]

“Turing machines are an even more daunting prospect” [Norrish]

**Contributions:**