# **Security Engineering**

#### Email: christian.urban at kcl.ac.uk Office: S1.27 (1st floor Strand Building) Slides: KEATS (also homework is there)

Imagine you have a completely innocent email message, like birthday wishes to your grandmother. Why should you still encrypt this message and your grandmother take the effort to decrypt it?

• (Hint: The answer has nothing to do with preserving the privacy of your grandmother and nothing to do with keeping her birthday wishes super-secret. Also nothing to do with you and grandmother testing the latest encryption technology, nor just for the sake of it.)



M.C.Escher, Amazing World (from Gödel, Escher, Bach by D.Hofstadter)



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### **Interlock Protocols**

A Protocol between a car C and a key transponder T:

- C generates a random number N
- C calculates  $(F, G) = \{N\}_K$

 $O C \to T: N, F$ 

- T calculates  $(F', G') = \{N\}_K$
- T checks that**F**=**F**'
- $T \rightarrow C: N, G'$
- C checks that G = G'

## **Zero-Knowledge Proofs**

- Essentially every NP-problem can be used for ZKPs
- modular logarithms: Alice chooses public A, B, p; and private x

 $A^x \equiv B \bmod p$ 

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### **Modular Arithmetic**

It is easy to calculate

 $? \equiv 46 \mod 12$ 

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### $10 \equiv 46 \mod 12$

A: 10

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Conclusion: 1.2304489 is very close to the *true* solution, slightly low

In contrast, modular logarithms behave much differently:

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 $2^{28305819} \equiv 88032151 \mod 97330327$ 

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Slightly lower. I might be tempted to try 28305820...

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 $2^{28_{3}05_{819}} \equiv 88_{032151} \mod 9733_{0327}$ 

Slightly lower. I might be tempted to try 28305820...but the real answer is 12314.

### **Commitment Stage**

- Alice generates z random numbers  $r_1, ..., r_z$ , all less than p 1.
- Alice sends Bob for all **1**..*z*

 $b_i = A^{r_i} \mod p$ 

- Solution Bob generates random bits  $b_1, ..., b_z$  by flipping a coin
- For each bit  $b_i$ , Alice sends Bob an  $s_i$  where

 $b_i = 0$ :  $s_i = r_i$  $b_i = 1$ :  $s_i = (r_i - r_j) \mod (p - 1)$ 

where  $r_j$  is the lowest j with  $b_j = I$ 

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- less than p I. Alice  $r_i$ :  $4 \quad 9 \quad I \quad 3$ Bob  $b_i$ :  $0 \quad I \quad 0 \quad I$   $b_i = A$  $b_i = A$
- Solution Bob generates random bits  $b_1, ..., b_z$  by flipping a coin
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### **Confirmation Stage**

For each b<sub>i</sub> Bob checks whether s<sub>i</sub> conforms to the protocol

$$b_i = 0$$
:  $A^{s_i} \equiv b_i \mod p$   
 $b_i = 1$ :  $A^{s_i} \equiv b_i * b_j^{-1} \mod p$ 

Bob was sent

 $b_1, \ldots, b_z,$  $r_1 - r_j, r_2 - r_j, \ldots, r_z - r_j \mod p - 1$ 

where the corresponding bits were I; Bob does not know  $r_j$ , he does not know any  $r_i$  where the bit was I Confirmation
 For each b<sub>i</sub> Bob checks the protocol

$$A^{s_i} = A^{r_i - r_j}$$
  
=  $A^{r_i} * A^{-r_j}$   
=  $b_{r_i} * b_{r_j}^{-1} \mod p$ 

$$b_i = 0$$
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## **Proving Stage**

Alice proves she knows x, the discrete log of B she sends

$$s_{z+i} = (x - r_j)$$

Bob confirms

$$A^{s_{z+1}} \equiv B * b_j^{-1} \mod p$$

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In order to cheat, Alice has to guess all bits in advance. She has only  $\frac{1^{z}}{2}$  chance of doing so.

• Alice needs to coordinate what she sends as  $b_i$  (in step 2),  $s_i$  (in step 4) and  $s_{z+1}$  (in step 6).

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 if she can guess j (first I) then she sends y as b<sub>j</sub> and o as s<sub>j</sub>.

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for **y**.

- if she can guess j (first I) then she sends y as b<sub>j</sub> and o as s<sub>j</sub>.
- however she does not know r<sub>j</sub> because she would need to solve

 $A^{r_j} \equiv y \mod p$ 

 Alice still needs to decide on the other b<sub>i</sub> and s<sub>i</sub>. They have to satisfy the test:

$$A^{s_i} \stackrel{?}{\equiv} \boldsymbol{b_i} * \boldsymbol{b_j^{-1}} \mod p$$

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• Lets say she choses the *s<sub>i</sub>* at random, then she needs to solve

$$A^{s_i} \equiv z * b_j^{-1} \mod p$$

for **z**.

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• Lets say she choses the *s<sub>i</sub>* at random, then she needs to solve

$$A^{s_i} \equiv z * b_j^{-1} \bmod p$$

for z. It still does not allow us to find out the  $r_i$ . Let us call an  $b_i$  calculated in this way as bogus.

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- Alice has to produce bogus b<sub>i</sub> for all bits that are going to be I in advance.
- Lets say b<sub>i</sub> = 1 where Alice guessed 0: She already has sent b<sub>i</sub> and b<sub>j</sub> and now must find a correct s<sub>i</sub> (which she chose at random at first)

$$A^{s_i} \equiv b_i * b_j^{-1} \bmod p$$

If she knew  $r_i$  and  $r_j$ , then easy:  $s_i = r_i - r_j$ . But she does not. So she will be found out.

- Alice has to produce bogus b<sub>i</sub> for all bits that are going to be I in advance.
- Lets say  $b_i = 0$  where Alice guessed 1: She has to send an  $s_i$  so that

 $A^{s_i} \equiv b_i \mod p$ 

She does not know  $r_i$ . So this is too hard and she will be found out.





























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## **Coming Back To...**

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- Any wild guesses?
- Bruce Schneier NSA Surveillance and What To Do About It https://www.youtube.com/watch?v=QXtS6UcdOMs

Terrorists use encrypted mobile-messaging apps. The spy agencies argue that although they can follow the conversations on Twitter, they "go dark" on the encrypted message apps. To counter this "going-dark problem", the spy agencies push for the implementation of back-doors in iMessage and Facebook and Skype and everything else UK or US-made, which they can use eavesdrop on conversations without the conversants' knowledge or consent.

• What is the fallacy in the spy agencies going-dark argument?

Even good passwords consisting of 8 characters, can be broken in around 50 days (obviously this time varies a lot and also gets shorter and shorter over time). Do you think it is good policy to require users to change their password every 3 months (as King's did until recently)?

Under which circumstance should users be required to change their password?