

Access Control and Privacy Policies (6)

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Slides: KEATS (also homework is there)

Problems with Key Fobs



- (I learned) jamming the closing signal
- relay signals

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- relay signals
- use diagnostic port to program blank keys

Hashes for History

Q: What is the hash for?

Dismantling Megamos Crypto: Wirelessly Lockpicking a Vehicle Immobilizer

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1 Disclaimer

Due to a interim injunction, ordered by the High Court of London on Tuesday 25th June 2013, the authors are restrained from publishing the technical contents of the scientific article *Dismantling Megamos Crypto: Wirelessly Lockpicking a Vehicle Immobilizer* [1] until further notice.

2 Historical claim

Figure 1 contains the cryptographic hash (SHA-512) of the original final paper which was scheduled to appear in the proceedings of the 22nd USENIX Security Symposium, Washington DC, August 2013.

```
9d05ba88740499eecea3d8609174b444
43683da139f78b783666954ccc605da8
4601888134bf0c23ba46fb4a88c056bf
bbb629e1dddfcf60fa91880b4d5b4aca
```

Figure 1: SHA-512 hash of the final paper

References

Checking Solutions

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*“an **individual** leaf of paper or parchment, either loose as one of a series or forming part of a bound volume, which is numbered on the recto or front side only.”*

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Alice and Bob solve crosswords. Alice knows the answer for 21D (folio) but doesn't want to tell Bob.

You use an English dictionary:

- folio \xrightarrow{I} individual
*“a single **human** being as distinct from a group”*

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- folio $\xrightarrow{1}$ individual $\xrightarrow{2}$ human

*“relating to **or** characteristic of humankind”*

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this is essentially a hash function...but Bob can only check once he has also found the solution

Zero-Knowledge Proofs

Two remarkable properties of **Zero-Knowledge Proofs**:

- Alice only reveals the fact that she knows a secret, not the secret itself (meaning she can convince Bob that she knows the secret, but does not give it to him).
- Having been convinced, Bob cannot use the evidence in order to convince Carol that Alice knows the secret.

Interactive Protocols

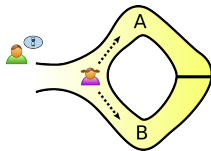
Q: How to cut a cake into two equal slices?



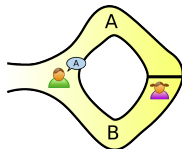
The Idea

The Alibaba cave:

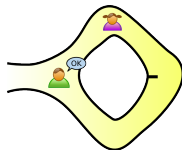
1.



2.



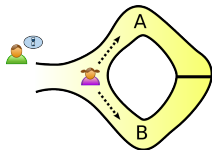
3.



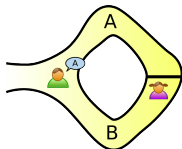
The Idea

The Alibaba cave:

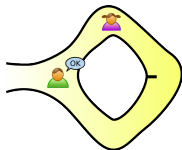
1.



2.



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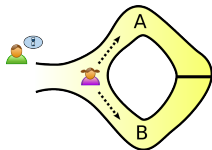


Even if Bob has a hidden camera, a recording will not be convincing to anyone else (Alice and Bob could have made it all up).

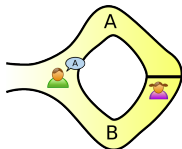
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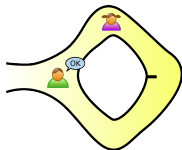
1.



2.



3.



Even worse, an observer present at the experiment would not be convinced.

Applications of ZKPs

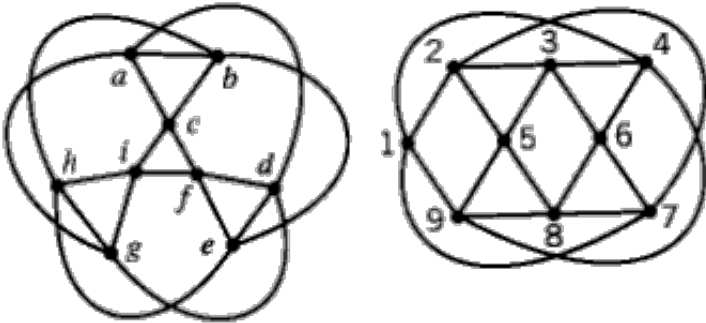
- authentication, where one party wants to prove its identity to a second party via some secret information, but doesn't want the second party to learn anything about this secret
- to enforce honest behaviour while maintaining privacy: the idea is to force users to prove, using a zero-knowledge proof, that their behaviour is correct according to the protocol

Central Properties

Zero-knowledge proof protocols should satisfy:

- **Completeness** If Alice knows the secret, Bob accepts Alice “proof” for sure.
- **Soundness** If Alice does not know the secret, Bob accepts her “proof” with a very small probability.

Graph Isomorphism



Finding an isomorphism between two graphs is an NP complete problem.

Graph Isomorphism Protocol

Alice starts with knowing an isomorphism σ between graphs G_1 and G_2

- 1 Alice generates an isomorphic graph H which she sends to Bob
- 2 Bob asks either for an isomorphism between G_1 and H , or G_2 and H
- 3 Alice and Bob repeat this procedure n times

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- these are called commitment algorithms

Graph Isomorphism Protocol

If Alice knows the isomorphism, she can always calculate σ .

If she doesn't, she can only correctly respond if Bob's choice of index is the same as the one she used to form H . The probability of this happening is $\frac{1}{2}$, so after n rounds the probability of her always responding correctly is only $\frac{1}{2^n}$.

Graph Isomorphism Protocol

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Why is the GI-protocol zero-knowledge?

A: We can generate a fake transcript of a conversation, which cannot be distinguished from a “real” conversation.

Anything Bob can compute using the information obtained from the transcript can be computed using only a forged transcript and therefore participation in such a communication does not increase Bob's capability to perform any computation.

Non-Interactive ZKPs

This is amazing: Alison can publish some data that contains no data about her secret, but this data can be used to convince anyone of the secret's existence.

Non-Interactive ZKPs (2)

Alice starts with knowing an isomorphism σ between graphs G_1 and G_2

- 1 Alice generates n isomorphic graphs $H_{1..n}$ which she makes public
- 2 she feeds the $H_{1..n}$ into a hashing function (she has no control over what the output will be)
- 3 Alice takes the first n bits of the output:
whenever output is 0, she shows an isomorphism with G_1 ; for 1 she shows an isomorphism with G_2

Problems of ZKPs

- “grand chess master problem”
(person in the middle)
- Alice can have multiple identities; once she committed a fraud she stops using one

Other Methods for ZKPs

Essentially every NP-problem can be used for ZKPs

- modular logarithms: Alice chooses public A , B , p ; and private x

$$A^x \equiv B \pmod{p}$$

Commitment Stage

1 Alice generates z random numbers r_1, \dots, r_z , all less than $p - 1$.

2 Alice sends Bob for all $i..z$

$$b_i = A^{r_i} \text{ mod } p$$

3 Bob generates random bits b_1, \dots, b_z by flipping a coin

4 For each bit b_i , Alice sends Bob an s_i where

$$b_i = 0: s_i = r_i$$

$$b_i = 1: s_i = (r_i - r_j) \text{ mod } (p - 1)$$

where r_j is the lowest j where $b_j = 1$

Confirmation Stage

- For each b_i Bob checks whether s_i conforms to the protocol

$$b_i = 0: A^{s_i} \equiv B \pmod{p}$$

$$b_i = 1: A^{s_i} \equiv b_i * b_j^{-1} \pmod{p}$$

Bob was send

$$r_j - r_j, r_m - r_j, \dots, r_p - r_j \pmod{p}$$

where the corresponding bits were 1; Bob does not know r_j , he does not know any r_i where the bit was 1

Proving Stage

- 1 Alice proves she knows x , the discrete log of B
she sends

$$s_{z+1} = (x - r_j)$$

- 2 Bob confirms

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In order to cheat, Alice has to guess all bits in advance. She has only 1 to 2^z chance.

(explanation → <http://goo.gl/irL9GK>)

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c increment

X_0 start value

and calculate

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Random Number Generators

- Computers are deterministic. How do we generate random numbers?

- The most popular method to generate random numbers between 0 and m is: choose three integers

$m =$	16		16
$X_0 =$	1		1
$a =$	5		5
$c =$	1		0

a multiplier

c increment

X_0 start value

and calculate

$$X_{n+1} = (a * X_n + c) \text{ mod } m$$