Security Engineering

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Slides: KEATS (also homework is there)

Imagine you have a completely innocent email message, like birthday wishes to your grandmother? Why should you still encrypt this message and your grandmother take the effort to decrypt it?

 (Hint: The answer has nothing to do with preserving the privacy of your grandmother and nothing to do with keeping her birthday wishes super-secret. Also nothing to do with you and grandmother testing the latest encryption technology, nor just for the sake of it.)



M.C.Escher, Amazing World (from Gödel, Escher, Bach by D.Hofstadter)



Interlock Protocols

A Protocol between a car *C* and a key transponder *T*:

- C generates a random number N

- T calculates $(F', G') = \{N\}_K$
- **o** T checks that F = F'
- \bigcirc C checks that G = G'

Zero-Knowledge Proofs

- Essentially every NP-problem can be used for ZKPs
- modular logarithms: Alice chooses public A, B, p;
 and private x

$$A^x \equiv B \mod p$$

Modular Arithmetic

It is easy to calculate

$$? \equiv 46 \bmod 12$$

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$$10 \equiv 46 \bmod 12$$

A: 10

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Conclusion: 1.2304489 is very close to the *true* solution, slightly low

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$$2^? \equiv 88319671 \mod 97330327$$

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Slightly lower. I might be tempted to try 28305820...but the real answer is 12314.

Commitment Stage

- Alice generates z random numbers $r_1, ..., r_z$, all less than p 1.
- Alice sends Bob for all 1..z

$$b_i = A^{r_i} \mod p$$

- **9** Bob generates random bits $b_1, ..., b_z$ by flipping a coin
- For each bit b_i , Alice sends Bob an s_i where

$$b_i = 0$$
: $s_i = r_i$
 $b_i = 1$: $s_i = (r_i - r_i) \mod (p - 1)$

where r_i is the lowest j with $b_i = 1$

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where r_i is the lowest j with $b_i = 1$

Confirmation Stage

• For each b_i Bob checks whether s_i conforms to the protocol

$$b_i = 0$$
: $A^{s_i} \equiv b_i \mod p$
 $b_i = 1$: $A^{s_i} \equiv b_i * b_j^{-1} \mod p$

Bob was sent

$$b_1, ..., b_z,$$

 $r_1 - r_j, r_2 - r_j, ..., r_z - r_j \mod p - 1$

where the corresponding bits were I; Bob does not know r_j , he does not know any r_i where the bit was I

Confirmat

For each b_i Bob checks with the protocol

$$A^{s_i} = A^{r_i - r_j}$$

$$= A^{r_i} * A^{-r_j}$$

$$= b_{r_i} * b_{r_j}^{-1} \bmod p$$

$$b_i = 0$$
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Proving Stage

Alice proves she knows x, the discrete log of B she sends

$$s_{z+1} = (x - r_j)$$

Bob confirms

$$A^{s_{z+1}} \equiv B * h_j^{-1} \mod p$$

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Bob confirms

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In order to cheat, Alice has to guess all bits in advance. She has only $\frac{1}{2}$ chance of doing so.

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• if she can guess j (first 1) then she sends y as b_j and o as s_j .

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for *y*.

- if she can guess j (first 1) then she sends y as h_j and o as s_j .
- however she does not know r_j because she would need to solve

$$A^{r_j} \equiv y \mod p$$

Alice still needs to decide on the other b_i and s_i.
 They have to satisfy the test:

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for z. It still does not allow us to find out the r_i . Let us call an b_i calculated in this way as bogus.

• Alice has to produce bogus b_i for all bits that are going to be I in advance.

- Alice has to produce bogus h_i for all bits that are going to be I in advance.
- Lets say $b_i = 1$ where Alice guessed 0: She already has sent b_i and b_j and now must find a correct s_i (which she chose at random at first)

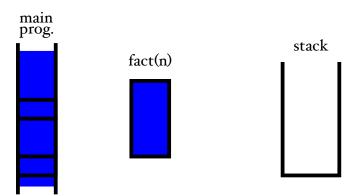
$$A^{s_i} \equiv b_i * b_j^{-1} \bmod p$$

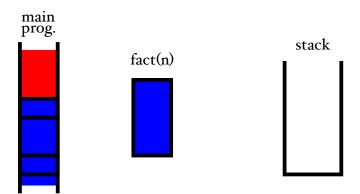
If she knew r_i and r_j , then easy: $s_i = r_i - r_j$. But she does not. So she will be found out.

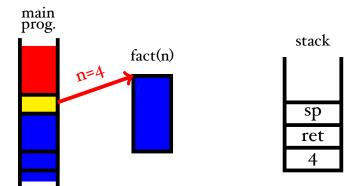
- Alice has to produce bogus h_i for all bits that are going to be I in advance.
- Lets say $b_i = 0$ where Alice guessed I: She has to send an s_i so that

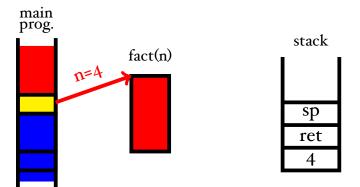
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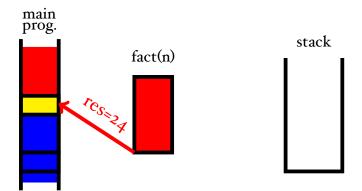
She does not know r_i . So this is too hard and she will be found out.

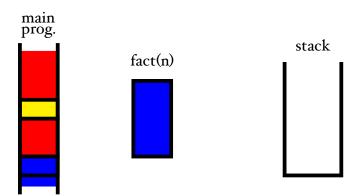


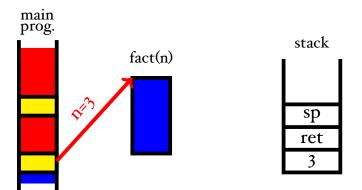


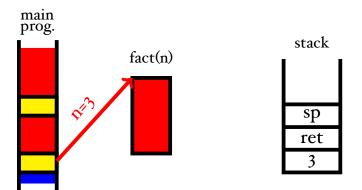


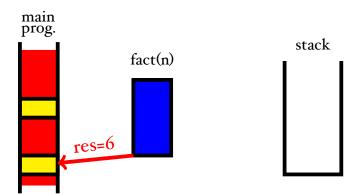


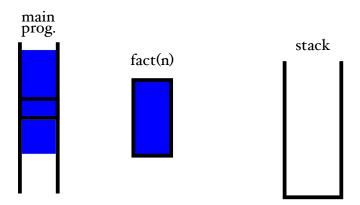


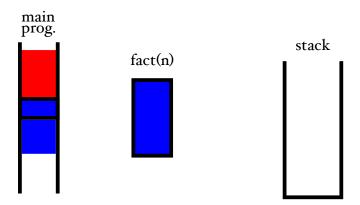


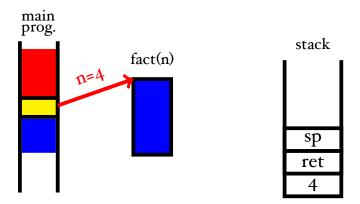


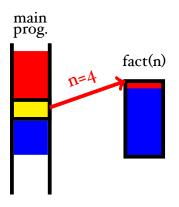




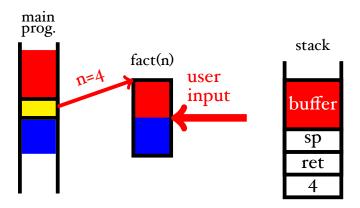


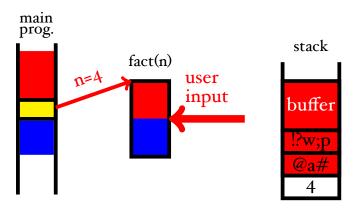


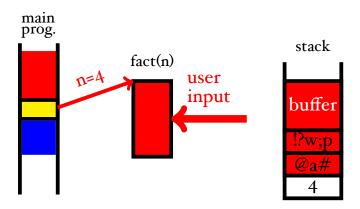


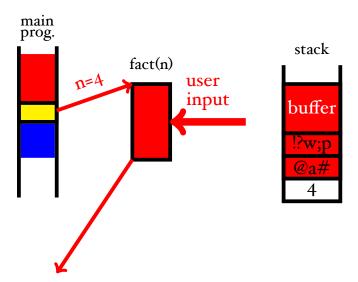












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- Any wild guesses?
- Bruce Schneier
 NSA Surveillance and What To Do About It
 https://www.youtube.com/watch?v=QXtS6Ucd0Ms

Terrorists use encrypted mobile-messaging apps. The spy agencies argue that although they can follow the conversations on Twitter, they "go dark" on the encrypted message apps. To counter this "going-dark problem", the spy agencies push for the implementation of back-doors in iMessage and Facebook and Skype and everything else UK or US-made, which they can use eavesdrop on conversations without the conversants' knowledge or consent.

• What is the fallacy in the spy agencies going-dark argument?