Main Part 5 (Scala, 10 Marks)

This part is about a small (esoteric) programming language called brainf***. We will implement an interpreter and compiler for this language.

Important

- Make sure the files you submit can be processed by just calling scala-cli compile <<filename.scala>> on the command line.¹ Use the template files provided and do not make any changes to arguments of functions or to any types. You are free to implement any auxiliary function you might need.
- Do not leave any test cases running in your code because this might slow down your program! Comment out test cases before submission, otherwise you might hit a time-out.
- Do not use any mutable data structures in your submissions! They are not needed. This means you cannot create new Arrays or ListBuffers, for example.
- Do not use return in your code! It has a different meaning in Scala than
 in Java. It changes the meaning of your program, and you should never
 use it.
- Do not use var! This declares a mutable variable. Only use val!
- Do not use any parallel collections! No .par therefore! Our testing and marking infrastructure is not set up for it.

Also note that the running time of each part will be restricted to a maximum of 30 seconds on my laptop.

Disclaimer

It should be understood that the work you submit represents your **own** effort! You have implemented the code entirely on your own. You have not copied from anyone else. Do not be tempted to ask Copilot for help or do any other shenanigans like this! An exception is the Scala code I showed during the lectures or uploaded to KEATS, which you can freely use.

¹ All major OSes, including Windows, have a command line. So there is no good reason to not download scala-cli, install it and run it on your own computer. Just do it!

Reference Implementation

As usual, this Scala assignment comes with a reference implementation in form of two jar-files. You can download them from KEATS. They allow you to run any test cases on your own computer. For example you can call scala-cli on the command line with the option --extra-jars bf.jar and then query any function from the bf.scala template file. You have to prefix the calls with M5a and M5b, respectively. For example

Part A (6 Marks)

Coming from Java or C++, you might think Scala is a rather esoteric programming language. But remember, some serious companies have built their business on Scala.² I claim functional programming is not a fad. And there are far, far more esoteric languages out there. One is called *brainf*****. You are asked in this part to implement an interpreter for this language.

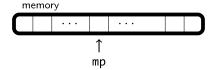
Urban Müller developed the original version of brainf*** in 1993. A close relative of this language was already introduced in 1964 by Corado Böhm, an Italian computer pioneer. The main feature of brainf*** is its minimalistic set of instructions—just 8 instructions in total and all of which are single characters. Despite the minimalism, this language has been shown to be Turing complete...if this doesn't ring any bell with you: it roughly means that every(!) algorithm can, in principle, be implemented in brainf***. It just takes a lot of determination and quite a lot of memory and time.

Some relatively sophisticated sample programs in brainf*** are given in the file bf.scala, including a brainf*** program for the Sierpinski triangle and the Mandelbrot set. There seems to be even a dedicated Windows IDE for bf programs, though I am not sure whether this is just an elaborate April fools' joke—judge yourself:

https://www.microsoft.com/en-us/p/brainf-ck/9nblgggzhvq5

As mentioned above, the original brainf*** has 8 single-character commands. Our version of bf will contain the commands '>', '<', '+', '-', '.', '[' and ']'. Every other character is considered a comment.

Our interpreter for bf operates on memory cells containing integers. For this it uses a single memory pointer, called mp, that points at each stage to one memory cell.



This pointer can be moved forward by one memory cell by using the command '>', and backward by using '<'. The commands '+' and '-' increase, respectively decrease, by 1 the content of the memory cell to which the memory pointer currently points to. The command for output in bf is '.' whereby output works by reading the content of the memory cell to which the memory pointer points to and printing it out as an ASCII character.³ The commands '[' and ']' are looping constructs. Everything in between '[' and ']' is repeated

²https://en.wikipedia.org/wiki/Scala_(programming_language)#Companies

³In the original version of bf, there is also a command for input, but we omit it here. All our programs will be "autonomous".

until a counter (memory cell) reaches zero. A typical program in brainf*** looks as follows:

```
++++++|>+++|>++++>+++>+<<<<-]>+>+>->>+[<]<-]>>.>---.++
+++++..+++.>>,<-.<..+++.-----.
```

This one prints out Hello World...obviously; o)

Tasks (file bf.scala)

- (1) Write a function that takes a filename (a string) as an argument and requests the corresponding file from disk. It returns the content of the file as a string. If the file does not exists, the function should return the empty string.

 [0.5 Marks]
- (2) Brainf**k memory is represented by a Map from integers to integers. The empty memory is represented by Map(), that is nothing is stored in the memory; Map(0 -> 1, 2 -> 3) stores 1 at memory location 0, and at 2 it stores 3. The convention is that if we query the memory at a location that is *not* defined in the Map, we return 0. Write a 'safe-read' function, sread, that takes a memory (a Map) and a memory pointer (an Int) as arguments, and 'safely' reads the corresponding memory location. If the Map is not defined at the memory pointer, sread returns 0.
 - Write another function write, which takes a memory, a memory pointer and an integer value as arguments and updates the Map with the value at the given memory location. As usual, the Map is not updated 'in-place' but a new map is created with the same data, except the new value is stored at the given memory pointer. [0.5 Marks]
- (3) Write two functions, jumpRight and jumpLeft, that are needed to implement the loop constructs in brainf**k. They take a program (a String) and a program counter (an Int) as arguments and move right (respectively left) in the string in order to find the matching opening/closing bracket. For example, given the following program with the program counter indicated by an arrow:

then the matching closing bracket is in 9th position (counting from 0) and jumpRight is supposed to return the position just after this

meaning it jumps to after the loop. Similarly, if you are in 8th position, then jumpLeft is supposed to jump to just after the opening bracket (that is jumping to the beginning of the loop):

Unfortunately we have to take into account that there might be other opening and closing brackets on the 'way' to find the matching bracket. For example in the brain*ck program

we do not want to return the index for the '-' in the 9th position, but the program counter for '.' in 12th position. The easiest to find out whether a bracket is matched is by using levels (which are the third argument in jumpLeft and jumpLeft). In case of jumpRight you increase the level by one whenever you find an opening bracket and decrease by one for a closing bracket. Then in jumpRight you are looking for the closing bracket on level 0. For jumpLeft you do the opposite. In this way you can find matching brackets in strings such as

for which jumpRight should produce the position:

It is also possible that the position returned by jumpRight or jumpLeft is outside the string in cases where there are no matching brackets. For example

[2 Marks]

(4) Write a recursive function compute that runs a brain*u*k program. It takes a program, a program counter, a memory pointer and a memory as arguments. If the program counter is outside the program string, the execution stops and compute returns the memory. If the program counter is inside the string, it reads the corresponding character and updates the program counter pc, memory pointer mp and memory mem according to the rules shown in Figure 1. It then calls recursively compute with the updated data. The most convenient way to implement the brainf**k rules

in Scala is to use pattern-matching and to calculate a triple consisting of the updated pc, mp and mem.

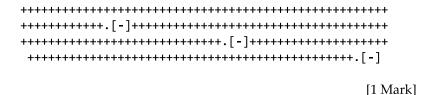
Write another function run that calls compute with a given brainfu*k program and memory, and the program counter and memory pointer set to 0. Like compute, it returns the memory after the execution of the program finishes. You can test your brainf**k interpreter with the Sierpinski triangle or the Hello world programs (they seem to be particularly useful for debugging purposes), or have a look at

https://esolangs.org/wiki/Brainfuck

for more bf-programs and the test cases given in bf.scala.

[2 Mark]

(5) Let us also generate some BF programs ourselves: Write a function generate which takes a list of characters as input and generates a corresponding BF program that prints out this list of characters. One way to generate such a program is to consider each character in the list, add as many "+" given by the ASCII code of the character, then add the "." command for printing and add the loop "[-]" for "zero-ing" the memory cell; then go to the next character in the list. For example the list "ABC".toString produces (as a single string)



Part B (4 Marks)

I am sure you agree while it is fun to marvel at bf-programs, like the Sierpinski triangle or the Mandelbrot program, being interpreted, it is much more fun to write a compiler for the bf-language.

Tasks (file bfc.scala)

(6) Compilers, in general, attempt to make programs run faster by precomputing as much information as possible before running the program. In our case we can precompute the addresses where we need to jump at the beginning and end of loops.

For this write a function jtable that precomputes the "jump table" for a bf-program. This function takes a bf-program as an argument and returns

'>'	• pc + 1
	ullet mp $+1$
	mem unchanged
'<'	• pc + 1
	$lackbox{lack}{lack}$ mp -1
	mem unchanged
'+'	• pc + 1
	mp unchanged
	• mem updated with mp -> mem(mp) + 1
'-'	• pc + 1
	mp unchanged
	• mem updated with mp -> mem(mp) - 1
'.'	• pc + 1
	mp and mem unchanged
	print out mem(mp) as a character
'['	if mem(mp) == 0 then
	pc = jumpRight(prog, pc + 1, 0)
	mp and mem unchanged
	otherwise if mem(mp) != 0 then
	• pc + 1
	• mp and mem unchanged
']'	if mem(mp) != 0 then
	• pc = jumpLeft(prog, pc - 1, 0)
	• mp and mem unchanged
	otherwise if mem(mp) == 0 then
	• pc + 1
	mp and mem unchanged
any	mp and mem unchanged
other	
char	

Figure 1: The rules for how commands in the brainf*** language update the program counter pc, the memory pointer mp and the memory mem.

a Map[Int, Int]. The purpose of this Map is to record the information, in cases a pc-position points to a '[' or a ']', to which pc-position do we need to jump next?

For example for the program

we obtain the Map (note the precise numbers might differ depending on white spaces etc. in the bf-program):

$$Map(69 \rightarrow 61, 5 \rightarrow 20, 60 \rightarrow 70, 27 \rightarrow 44, 43 \rightarrow 28, 19 \rightarrow 6)$$

This Map states that for the '[' on position 5, we need to jump to position 20, which is just after the corresponding ']'. Similarly, for the ']' on position 19, we need to jump to position 6, which is just after the '[' on position 5, and so on. The idea is to not calculate this information each time we hit a bracket, but just look up this information in the jtable.

Then adapt the compute and run functions from Part 1 in order to take advantage of the information stored in the jtable. This means whenever jumpLeft and jumpRight was called previously, you should look up the jump address in the jtable. Feel free to reuse the function jumpLeft and jumpRight for calculating the jtable. [1 Mark]

(7) Compilers try to eliminate any "dead" code that could slow down programs and also perform what is often called *peephole optimisations*. For the latter consider that it is difficult for compilers to comprehend what is intended with whole programs, but they are very good at finding out what small snippets of code do, and then try to generate faster code for such snippets.

In our case, dead code is everything that is not a bf-command. Therefore write a function optimise which deletes such dead code from a bf-program. Moreover this function should replace every substring of the form [-] by a new command 0. The idea is that the loop [-] just resets the memory at the current location to 0. It is more efficient to do this in a single step, rather than stepwise in a loop as in the original bf-programs.

In the extended compute3 and run3 functions you should implement this command by writing 0 to mem(mp), that is use write(mem, mp, 0) as the rule for the command 0. The easiest way to modify a string in this way is to use the regular expression """[^<>+\-.\[\]]""", which recognises everything that is not a bf-command. Similarly, the regular expression """\[-\]""" finds all occurrences of [-]. By using the Scala method .replaceAll you can replace substrings with new strings.

[1 Mark]

 $^{^4 \}verb|https://en.wikipedia.org/wiki/Peephole_optimization|$

(8) Finally, real compilers try to take advantage of modern CPUs which often provide complex operations in hardware that can combine many smaller instructions into a single faster instruction.

In our case we can optimise the several single increments performed at a memory cell, for example ++++, by a single "increment by 4". For this optimisation we just have to make sure these single increments are all next to each other. Similar optimisations should apply for the bf-commands -, < and >, which can all be replaced by extended versions that take the amount of the increment (decrement) into account. We will do this by introducing two-character bf-commands. For example

original bf-cmds	replacement
+	+A
++	+B
+++	+C
•••	
+++++	+Z
(these are $26 + 's$)	

If there are more than 26 +'s in a row, then more than one "two-character" bf-commands need to be generated (the idea is that more than 26 copies of a single bf-command in a row is a rare occurrence in actual bf-programs). Similar replacements apply for -, < and >, but all other bf-commands should be unaffected by this change.

For this write a function combine which replaces sequences of repeated increment and decrement commands by appropriate two-character commands. In the functions compute4 and run4, the "combine" and the optimisation from (6) should be performed. Make sure that when a two-character bf-command is encountered you need to increase the pc-counter by two in order to progress to the next command. For example

generates the improved program

for the original benchmark program

As you can see, the compiler bets on saving a lot of time on the +B and +M steps so that the optimisations is worthwhile overall (of course for the >A's and so on, the compiler incurs a penalty). Luckily, after you have performed all optimisations in (5) - (7), you can expect that the benchmark.bf program runs four to five times faster. You can also test whether your compiler produces the correct result by testing for example