



The Isabelle Programmer's Cookbook (fragment)

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Contents

1	Introduction	2
1.1	Intended Audience and Prior Knowledge	2
1.2	Existing Documentation	2
2	First Steps	4
2.1	Antiquotations	5
2.2	Terms	6
2.3	Constructing Terms Manually	7
2.4	Type checking	8
2.5	Theorems	9
2.6	Tactical Reasoning	10
2.7	Storing and Changing Theorems and so on	11
3	Parsing	12
3.1	Parsing Isar input	12
3.2	The <code>Scan</code> structure	13
3.3	The <code>OuterLex</code> structure	16
3.4	The <code>OuterParse</code> structure	16
3.5	The <code>SpecParse</code> structure	18
3.6	The <code>Args</code> structure	19
3.7	Attributes, and the <code>Attrib</code> structure	21
3.8	Methods, and the <code>Method</code> structure	23
A	Recipes	25
A.1	Accumulate a List of Theorems under a Name	25
A.2	Ad-hoc Transformations of Theorems	26

Chapter 1

Introduction

The purpose of this cookbook is to guide the reader through the first steps of Isabelle programming, and to provide recipes for solving common problems.

1.1 Intended Audience and Prior Knowledge

This cookbook targets an audience who already knows how to use Isabelle for writing theories and proofs. We also assume that readers are familiar with the Standard ML, the programming language in which most of Isabelle is implemented. If you are unfamiliar with either of these two subjects, you should first work through the Isabelle/HOL tutorial [1] and Paulson's book on Standard ML [2].

1.2 Existing Documentation

The following documentation about Isabelle programming already exist (they are included in the distribution of Isabelle):

The Implementation Manual describes Isabelle from a programmer's perspective, documenting both the underlying concepts and some of the interfaces.

The Isabelle Reference Manual is an older document that used to be the main reference at a time when all proof scripts were written on the ML level. Many parts of this manual are outdated now, but some parts, particularly the chapters on tactics, are still useful.

Then of course there is:

The code is of course the ultimate reference for how things really work. Therefore you should not hesitate to look at the way things are actually implemented. More importantly, it is often good to look at code that does similar things as you want to do, to learn from other people's code.

Since Isabelle is not a finished product, these manuals, just like the implementation itself, are always under construction. This can be difficult and frustrating at times, especially when interfaces changes occur frequently. But it is a reality that progress means changing things (FIXME: need some short and convincing comment that this is a strategy, not a problem that should be solved).

Chapter 2

First Steps

Isabelle programming is done in Standard ML. Just like lemmas and proofs, code in Isabelle is part of a theory. If you want to follow the code written in this chapter, we assume you are working inside the theory defined by

```
theory CookBook
imports Main
begin
...
```

The easiest and quickest way to include code in a theory is by using the **ML** command. For example

```
ML {*
  3 + 4
*}
```

The expression inside **ML** commands is immediately evaluated, like “normal” Isabelle proof scripts, by using the advance and undo buttons of your Isabelle environment. The code inside the **ML** command can also contain value- and function bindings. However on such ML-commands the undo operation behaves slightly counter-intuitive, because if you define

```
ML {*
  val foo = true
*}
```

then Isabelle’s undo operation has no effect on the definition of `foo`.

(FIXME: add comment about including whole ML-files)

During developments you might find it necessary to quickly inspect some data in your code. This can be done in a “quick-and-dirty” fashion using the function `warning`. For example

```
ML {*
```

```
    val _ = warning "any string"
  *}
```

will print out "any string" inside the response buffer of Isabelle. PolyML provides a convenient, though again “quick-and-dirty”, method for converting arbitrary values into strings, for example:

```
ML {*
    val _ = warning (makestring 1)
  *}
```

However this only works if the type of what is printed is monomorphic and not a function.

(FIXME: add here or in the appendix a comment about tracing)

(FIXME: maybe a comment about redirecting the trace information)

2.1 Antiquotations

The main advantage of embedding all code in a theory is that the code can contain references to entities defined on the logical level of Isabelle. This is done using antiquotations. For example, one can print out the name of the current theory by typing

```
ML {* Context.theory_name @{theory} *}
```

where `@{theory}` is an antiquotation that is substituted with the current theory (remember that we assumed we are inside the theory `CookBook`). The name of this theory can be extracted using the function `Context.theory_name`. So the code above returns the string `"CookBook"`.

Note, however, that antiquotations are statically scoped, that is the value is determined at “compile-time”, not “run-time”. For example the function

```
ML {*
    fun current_thyname () = Context.theory_name @{theory}
  *}
```

does *not* return the name of the current theory, if it is run in a different theory. Instead, the code above defines the constant function that always returns the string `"CookBook"`, no matter where the function is called. Operationally speaking, `@{theory}` is *not* replaced with code that will look up the current theory in some data structure and return it. Instead, it is literally replaced with the value representing the theory name.

In a similar way you can use antiquotations to refer to types and theorems:

```
ML {* @{typ} "(int * nat) list" *}
ML {* @{thm} allI *}
```

In the course of this introduction, we will learn more about these antiquotations: they greatly simplify Isabelle programming since one can directly access all kinds of logical elements from ML.

2.2 Terms

One way to construct terms of Isabelle on the ML-level is by using the antiquotation `@{term ...}`:

```
ML {* @{term "(a::nat) + b = c"} *}
```

This will show the term $a + b = c$, but printed out using the internal representation of this term. This internal representation corresponds to the datatype term.

The internal representation of terms uses the usual de-Brujin index mechanism where bound variables are represented by the constructor Bound. The index in Bound refers to the number of Abstractions (Abs) we have to skip until we hit the Abs that binds the corresponding variable. However, in Isabelle the names of bound variables are kept at abstractions for printing purposes, and so should be treated only as comments.

Terms are described in detail in [Impl.Man., Sec. 2.2]. Their definition and many useful operations can be found in Pure/term.ML.

[Read More](#)

Sometimes the internal representation of terms can be surprisingly different from what you see at the user level, because the layers of parsing/type checking/pretty printing can be quite elaborate.

Exercise 2.2.1. *Look at the internal term representation of the following terms, and find out why they are represented like this.*

- $\text{case } x \text{ of } 0 \Rightarrow 0 \mid \text{Suc } y \Rightarrow y$
- $\lambda(x, y). P \ y \ x$
- $\{[x] \mid x. x \leq -2\}$

Hint: The third term is already quite big, and the pretty printer may omit parts of it by default. If you want to see all of it, you can use the following ML function to set the limit to a value high enough:

```
ML {* print_depth 50 *}
```

The antiquotation `@{prop ...}` constructs terms of propositional type, inserting the invisible `Trueprop` coercions whenever necessary. Consider for example

```
ML {* @{term "P x"} ; @{prop "P x"} *}
```

which needs the coercion and

```
ML {* @{term "P x ==> Q x"} ; @{prop "P x ==> Q x"} *}
```

which does not.

2.3 Constructing Terms Manually

While antiquotations are very convenient for constructing terms, they can only construct fixed terms. Unfortunately, one often needs to construct terms dynamically. For example, a function that returns the implication $\bigwedge(x::nat). P x \implies Q x$ taking P and Q as input terms can only be written as

```
ML {*
  fun make_imp P Q =
    let
      val x = @{term "x::nat"}
    in Logic.all x (Logic.mk_implies (HOLLogic.mk_Trueprop (P $ x),
                                     HOLLogic.mk_Trueprop (Q $ x)))
    end
  *}

```

The reason is that one cannot pass the arguments P and Q into an antiquotation, like

```
ML {*
  fun make_imp_wrong P Q = @{prop "\x. P x ==> Q x"}
  *}

```

To see the difference apply `@{term S}` and `@{term T}` to the functions.

One tricky point in constructing terms by hand is to obtain the fully qualified names for constants. For example the names for `zero` or `+` are more complex than one first expects, namely `HOL.zero_class.zero` and `HOL.plus_class.plus`. The extra prefixes `zero_class` and `plus_class` are present because these constants are defined within type classes; the prefix `HOL` indicates in which theory they are defined. Guessing such internal names can sometimes be quite hard. Therefore Isabelle provides the antiquotation `@{const_name ...}` does the expansion automatically, for example:

```
ML {* @{const_name HOL.zero}; @{const_name plus} *}
```

There are many functions in `Pure/logic.ML` and `HOL/hologic.ML` that make such manual constructions of terms easier.

[Read More](#)

Have a look at these files and try to solve the following two exercises:

Exercise 2.3.1. Write a function `rev_sum : term -> term` that takes a term of the form $t_1 + t_2 + \dots + t_n$ (whereby i might be zero) and returns the reversed sum $t_n + \dots + t_2 + t_1$. Assume the t_i can be arbitrary expressions and also note that `+` associates to the left. Try your function on some examples.

```
ML {*
  fun rev_sum t =
    let
      fun dest_sum (Const (@{const_name plus}, _) $ u $ u') =
        u' :: dest_sum u
      | dest_sum u = [u]
    in
      foldl1 (HOLogic.mk_binop @{const_name plus}) (dest_sum t)
    end;
*}
```

Exercise 2.3.2. Write a function which takes two terms representing natural numbers in unary (like `Suc (Suc (Suc 0))`), and produce the unary number representing their sum.

```
ML {*
  fun make_sum t1 t2 =
    HOLogic.mk_nat (HOLogic.dest_nat t1 + HOLogic.dest_nat t2)
*}
```

2.4 Type checking

(FIXME: Should we say something about types?)

We can freely construct and manipulate terms, since they are just arbitrary unchecked trees. However, we eventually want to see if a term is well-formed, or type checks, relative to a theory. Type checking is done via the function `cterm_of`, which turns a term into a `cterm`, a *certified* term. Unlike terms, which are just trees, `cterm`s are abstract objects that are guaranteed to be type-correct, and can only be constructed via the official interfaces.

Type checking is always relative to a theory context. For now we can use the `@{theory}` antiquotation to get hold of the current theory. For example we can write:

```
ML {* cterm_of @{theory} @{term "(a::nat) + b = c"} *
```

```
ML {*
  let
    val natT = @{typ "nat"}
    val zero = @{term "0::nat"}
  in
    cterm_of @{theory}
  end
```

```

      (Const (@{const_name plus}, natT --> natT --> natT)
        $ zero $ zero)
    end
  *}

```

Exercise 2.4.1. Check that the function defined in Exercise 2.3.1 returns a result that type checks.

2.5 Theorems

Just like `cterm`s, theorems (of type `thm`) are abstract objects that can only be built by going through the kernel interfaces, which means that all your proofs will be checked.

To see theorems in “action”, let us give a proof for the following statement

```

lemma
  assumes assm1: " $\bigwedge (x::\text{nat}). P\ x \implies Q\ x$ "
  and      assm2: "P t"
  shows "Q t"

```

on the ML level:¹

```

ML {*
let
  val thy = @{theory}

  val assm1 = cterm_of thy @{prop " $\bigwedge (x::\text{nat}). P\ x \implies Q\ x$ "}
  val assm2 = cterm_of thy @{prop " $((P::\text{nat} \Rightarrow \text{bool})\ t)$ "}

  val Pt_implies_Qt =
    assume assm1
    |> forall_elim (cterm_of thy @{term "t::nat"});

  val Qt = implies_elim Pt_implies_Qt (assume assm2);
in

  Qt
  |> implies_intr assm2
  |> implies_intr assm1
end
  *}

```

For how the functions `assume`, `forall_elim` etc work see [Impl. Man., Sec. 2.3].

[Read More](#)

The basic functions for theorems are defined in `Pure/thm.ML`.

¹Note that `|>` is just reverse application. This combinator, and several variants are defined in `Pure/General/basics.ML`.

2.6 Tactical Reasoning

The goal-oriented tactical style reasoning of the ML level is similar to the `apply`-style at the user level, i.e. the reasoning is centred around a *goal*, which is modified in a sequence of proof steps until it is solved.

A goal (or goal state) is a special `thm`, which by convention is an implication of the form:

$$A_1 \implies \dots \implies A_n \implies \#(C)$$

where C is the goal to be proved and the A_i are the open subgoals.

Since the goal C can potentially be an implication, there is a `#` wrapped around it, which prevents that premises are misinterpreted as open subgoals. The protection `# :: prop \Rightarrow prop` is just the identity function and used as a syntactic marker.

For more on goals see [Impl. Man., Sec. 3.1].

[Read More](#)

Tactics are functions that map a goal state to a (lazy) sequence of successor states, hence the type of a tactic is

```
thm -> thm Seq.seq
```

See `Pure/General/seq.ML` for the implementation of lazy sequences. However in day-to-day Isabelle programming, one rarely constructs sequences explicitly, but uses the predefined tactic combinators (tacticals) instead (see `Pure/tactical.ML`). (FIXME: Pointer to the old reference manual)

[Read More](#)

While tactics can operate on the subgoals (the A_i above), they are expected to leave the conclusion C intact, with the exception of possibly instantiating schematic variables.

To see how tactics work, let us transcribe a simple `apply`-style proof from the tutorial [1] into ML:

```
lemma disj_swap: "P  $\vee$  Q  $\implies$  Q  $\vee$  P"
  apply (erule disjE)
  apply (rule disjI2)
  apply assumption
  apply (rule disjI1)
  apply assumption
done
```

To start the proof, the function `Goal.prove ctxt params assms goal tac` sets up a goal state for proving *goal* under the assumptions *assms* with the variables *params* that will be generalised once the goal is proved; *tac* is a function that returns a tactic having some funny input parameters (FIXME by possibly having an explanation in the implementation-manual).

```
ML {*
```

```

let
  val ctxt = @{context}
  val goal = @{prop "P ∨ Q ⇒ Q ∨ P"}
in
  Goal.prove ctxt ["P", "Q"] [] goal (fn _ =>
    eresolve_tac [disjE] 1
    THEN resolve_tac [disjI2] 1
    THEN assume_tac 1
    THEN resolve_tac [disjI1] 1
    THEN assume_tac 1)
end
*}

```

An alternative way to transcribe this proof is as follows

```

ML {*
let
  val ctxt = @{context}
  val goal = @{prop "P ∨ Q ⇒ Q ∨ P"}
in
  Goal.prove ctxt ["P", "Q"] [] goal (fn _ =>
    (eresolve_tac [disjE]
    THEN' resolve_tac [disjI2]
    THEN' assume_tac
    THEN' resolve_tac [disjI1]
    THEN' assume_tac) 1)
end
*}

```

2.7 Storing and Changing Theorems and so on

Chapter 3

Parsing

Lots of Standard ML code is given in this document, for various reasons, including:

- direct quotation of code found in the Isabelle source files, or simplified versions of such code
- identifiers found in the Isabelle source code, with their types (or specialisations of their types)
- code examples, which can be run by the reader, to help illustrate the behaviour of functions found in the Isabelle source code
- ancillary functions, not from the Isabelle source code, which enable the reader to run relevant code examples
- type abbreviations, which help explain the uses of certain functions

3.1 Parsing Isar input

The typical parsing function has the type `'src -> 'res * 'src`, with input of type `'src`, returning a result of type `'res`, which is (or is derived from) the first part of the input, and also returning the remainder of the input. (In the common case, when it is clear what the “remainder of the input” means, we will just say that the functions “returns” the value of type `'res`). An exception is raised if an appropriate value cannot be produced from the input. A range of exceptions can be used to identify different reasons for the failure of a parse.

This contrasts the standard parsing function in Standard ML, which is of type `('res, 'src) reader = 'src -> ('res * 'src) option;` (for example, `List.getItem` and `Substring.getc`). However, much of the dis-

discussion at FIX file:/home/jeremy/html/ml/SMLBasis/string-cvt.html is relevant.

Naturally one may convert between the two different sorts of parsing functions as follows:

```
open StringCvt ;
type ('res, 'src) ex_reader = 'src -> 'res * 'src
(* ex_reader : ('res, 'src) reader -> ('res, 'src) ex_reader *)
fun ex_reader rdr src = Option.valOf (rdr src) ;
(* reader : ('res, 'src) ex_reader -> ('res, 'src) reader *)
fun reader exrdr src = SOME (exrdr src) handle _ => NONE ;
```

3.2 The Scan structure

The source file is src/General/scan.ML. This structure provides functions for using and combining parsing functions of the type 'src -> 'res * 'src. Three exceptions are used:

```
exception MORE of string option; (*need more input (prompt)*)
exception FAIL of string option; (*try alternatives (reason of failure)*)
exception ABORT of string;      (*dead end*)
```

Many functions in this structure (generally those with names composed of symbols) are declared as infix.

Some functions from that structure are

```
|-- : ('src -> 'res1 * 'src') * ('src' -> 'res2 * 'src'') ->
'src -> 'res2 * 'src''
--| : ('src -> 'res1 * 'src') * ('src' -> 'res2 * 'src'') ->
'src -> 'res1 * 'src''
-- : ('src -> 'res1 * 'src') * ('src' -> 'res2 * 'src'') ->
'src -> ('res1 * 'res2) * 'src''
^^ : ('src -> string * 'src') * ('src' -> string * 'src'') ->
'src -> string * 'src''
```

These functions parse a result off the input source twice.

|-- and --| return the first result and the second result, respectively.

-- returns both.

^^ returns the result of concatenating the two results (which must be strings).

Note how, although the types `'src`, `'src`' and `'src''` will normally be the same, the types as shown help suggest the behaviour of the functions.

```
:- : ('src -> 'res1 * 'src') * ('res1 -> 'src' -> 'res2 * 'src'') ->
'src -> ('res1 * 'res2) * 'src''
:|-- : ('src -> 'res1 * 'src') * ('res1 -> 'src' -> 'res2 * 'src'') ->
'src -> 'res2 * 'src''
```

These are similar to `|--` and `--|`, except that the second parsing function can depend on the result of the first.

```
>> : ('src -> 'res1 * 'src') * ('res1 -> 'res2) -> 'src -> 'res2 * 'src'
|| : ('src -> 'res_src) * ('src -> 'res_src) -> 'src -> 'res_src'
```

`p >> f` applies a function `f` to the result of a parse.

`||` tries a second parsing function if the first one fails by raising an exception of the form `FAIL _`.

```
succeed : 'res -> ('src -> 'res * 'src) ;
fail : ('src -> 'res_src) ;
!! : ('src * string option -> string) ->
('src -> 'res_src) -> ('src -> 'res_src) ;
```

`succeed r` returns `r`, with the input unchanged. `fail` always fails, raising exception `FAIL NONE`. `!! f` only affects the failure mode, turning a failure that raises `FAIL _` into a failure that raises `ABORT ...`. This is used to prevent recovery from the failure — thus, in `!! parse1 || parse2`, if `parse1` fails, it won't recover by trying `parse2`.

```
one : ('si -> bool) -> ('si list -> 'si * 'si list) ;
some : ('si -> 'res option) -> ('si list -> 'res * 'si list) ;
```

These require the input to be a list of items: they fail, raising `MORE NONE` if the list is empty. On other failures they raise `FAIL NONE`

`one p` takes the first item from the list if it satisfies `p`, otherwise fails.

`some f` takes the first item from the list and applies `f` to it, failing if this returns `NONE`.

```
many : ('si -> bool) -> 'si list -> 'si list * 'si list ;
```

many p takes items from the input until it encounters one which does not satisfy p. If it reaches the end of the input it fails, raising MORE NONE.

many1 (with the same type) fails if the first item does not satisfy p.

```
option : ('src -> 'res * 'src) -> ('src -> 'res option * 'src)
optional : ('src -> 'res * 'src) -> 'res -> ('src -> 'res * 'src)
```

option: where the parser f succeeds with result r or raises FAIL _, option f gives the result SOME r or NONE.

optional: if parser f fails by raising FAIL _, optional f default provides the result default.

```
repeat : ('src -> 'res * 'src) -> 'src -> 'res list * 'src
repeat1 : ('src -> 'res * 'src) -> 'src -> 'res list * 'src
bulk : ('src -> 'res * 'src) -> 'src -> 'res list * 'src
```

repeat f repeatedly parses an item off the remaining input until f fails with FAIL _

repeat1 is as for repeat, but requires at least one successful parse.

```
lift : ('src -> 'res * 'src) -> ('ex * 'src -> 'res * ('ex * 'src))
```

lift changes the source type of a parser by putting in an extra component 'ex, which is ignored in the parsing.

The Scan structure also provides the type lexicon, HOW DO THEY WORK ?? TO BE COMPLETED

```
dest_lexicon: lexicon -> string list ;
make_lexicon: string list list -> lexicon ;
empty_lexicon: lexicon ;
extend_lexicon: string list list -> lexicon -> lexicon ;
merge_lexicons: lexicon -> lexicon -> lexicon ;
is_literal: lexicon -> string list -> bool ;
literal: lexicon -> string list -> string list * string list ;
```

Two lexicons, for the commands and keywords, are stored and can be retrieved by:

```
val (command_lexicon, keyword_lexicon) = OuterSyntax.get_lexicons () ;
val commands = Scan.dest_lexicon command_lexicon ;
val keywords = Scan.dest_lexicon keyword_lexicon ;
```


3.3 The OuterLex structure

The source file is `src/Pure/Isar/outer_lex.ML`. In some other source files its name is abbreviated:

```
structure T = OuterLex;
```

This structure defines the type `token`. (The types `OuterLex.token`, `OuterParse.token` and `SpecParse.token` are all the same).

Input text is split up into tokens, and the input source type for many parsing functions is `token list`.

The datatype definition (which is not published in the signature) is

```
datatype token = Token of Position.T * (token_kind * string);
```

but here are some runnable examples for viewing tokens:

FIXME

```
begin{verbatim} type token = T.token ; val toks : token list = OuterSyntax.scan
''theory,imports;begin x.y.z apply ?v1 ?'a 'a -- || 44 simp (* xx *) {
* fff * }'' ; print_depth 20 ; List.map T.text_of toks ; val proper_toks
= List.filter T.is_proper toks ; List.map T.kind_of proper_toks ; List.map
T.unparse proper_toks ; List.map T.val_of proper_toks ; end{verbatim}
```

The function `is_proper : token -> bool` identifies tokens which are not white space or comments: many parsing functions assume require spaces or comments to have been filtered out.

There is a special end-of-file token:

```
val (tok_eof : token, is_eof : token -> bool) = T.stopper ;
(* end of file token *)
```

3.4 The OuterParse structure

The source file is `src/Pure/Isar/outer_parse.ML`. In some other source files its name is abbreviated:

```
structure P = OuterParse;
```

Here the parsers use `token list` as the input source type.

Some of the parsers simply select the first token, provided that it is of the right kind (as returned by `T.kind_of`): these are `command`, `keyword`, `short_ident`, `long_ident`, `sym_ident`, `term_var`, `type_ident`, `type_var`, `number`, `string`, `alt_string`, `verbatim`, `sync`, `eof` Others select the first token, provided that it is one of several kinds, (eg, `name`, `xname`, `text`, `typ`).

```
type 'a tlp = token list -> 'a * token list ; (* token list parser *)
$$$ : string -> string tlp
nat : int tlp ;
maybe : 'a tlp -> 'a option tlp ;
```

`$$$ s` returns the first token, if it equals `s` and `s` is a keyword.

`nat` returns the first token, if it is a number, and evaluates it.

`maybe`: if `p` returns `r`, then `maybe p` returns `SOME r` ; if the first token is an underscore, it returns `NONE`.

A few examples:

```
P.list : 'a tlp -> 'a list tlp ; (* likewise P.list1 *)
P.and_list : 'a tlp -> 'a list tlp ; (* likewise P.and_list1 *)
val toks : token list = OuterSyntax.scan "44 ,_, 66,77" ;
val proper_toks = List.filter T.is_proper toks ;
P.list P.nat toks ; (* OK, doesn't recognize white space *)
P.list P.nat proper_toks ; (* fails, doesn't recognize what follows ',' *)
P.list (P.maybe P.nat) proper_toks ; (* fails, end of input *)
P.list (P.maybe P.nat) (proper_toks @ [tok_eof]) ; (* OK *)
val toks : token list = OuterSyntax.scan "44 and 55 and 66 and 77" ;
P.and_list P.nat (List.filter T.is_proper toks @ [tok_eof]) ; (* ??? *)
```

The following code helps run examples:

```
fun parse_str tlp str =
let val toks : token list = OuterSyntax.scan str ;
    val proper_toks = List.filter T.is_proper toks @ [tok_eof] ;
    val (res, rem_toks) = tlp proper_toks ;
    val rem_str = String.concat
      (Library.separate " " (List.map T.unparse rem_toks)) ;
in (res, rem_str) end ;
```

Some examples from `src/Pure/Isar/outer_parse.ML`

```

val type_args =
  type_ident >> Library.single ||
  $$$ "(" |-- !!! (list1 type_ident --| $$$ ")") ||
  Scan.succeed [];

```

There are three ways parsing a list of type arguments can succeed. The first line reads a single type argument, and turns it into a singleton list. The second line reads “(”, and then the remainder, ignoring the “(” ; the remainder consists of a list of type identifiers (at least one), and then a “)” which is also ignored. The !!! ensures that if the parsing proceeds this far and then fails, it won’t try the third line (see the description of Scan.!!). The third line consumes no input and returns the empty list.

```

fun triple2 (x, (y, z)) = (x, y, z);
val arity = xname -- ($$$ ":@" |-- !!! (
  Scan.optional ($$$ "(" |-- !!! (list1 sort --| $$$ ")")) []
  -- sort)) >> triple2;

```

The parser `arity` reads a typename t , then “:.” (which is ignored), then optionally a list ss of sorts and then another sort s . The result $(t, (ss, s))$ is transformed by `triple2` to (t, ss, s) . The second line reads the optional list of sorts: it reads first “(” and last “)”, which are both ignored, and between them a comma-separated list of sorts. If this list is absent, the default [] provides the list of sorts.

```

parse_str P.type_args "('a, 'b) ntyp" ;
parse_str P.type_args "'a ntyp" ;
parse_str P.type_args "ntyp" ;
parse_str P.arity "ty :: tycl" ;
parse_str P.arity "ty :: (tycl1, tycl2) tycl" ;

```

3.5 The SpecParse structure

The source file is `src/Pure/Isar/spec_parse.ML`. This structure contains token list parsers for more complicated values. For example,

```

open SpecParse ;
attrib : Attrib.src tok_rdr ;
attribs : Attrib.src list tok_rdr ;

```

```

opt_attribs : Attrib.src list tok_rdr ;
xthm : (thmref * Attrib.src list) tok_rdr ;
xthms1 : (thmref * Attrib.src list) list tok_rdr ;

parse_str attrib "simp" ;
parse_str opt_attribs "hello" ;
val (ass, "") = parse_str attribs "[standard, xxxx, simp, intro, OF sym]" ;
map Args.dest_src ass ;
val (asrc, "") = parse_str attrib "THEN trans [THEN sym]" ;

parse_str xthm "mythm [attr]" ;
parse_str xthms1 "thm1 [attr] thms2" ;

```

As you can see, attributes are described using types of the `Args` structure, described below.

3.6 The `Args` structure

The source file is `src/Pure/Isar/args.ML`. The primary type of this structure is the `src` datatype; the single constructors not published in the signature, but `Args.src` and `Args.dest_src` are in fact the constructor and destructor functions. Note that the types `Attrib.src` and `Method.src` are in fact `Args.src`.

```

src : (string * Args.T list) * Position.T -> Args.src ;
dest_src : Args.src -> (string * Args.T list) * Position.T ;
Args.pretty_src : Proof.context -> Args.src -> Pretty.T ;
fun pr_src ctxt src = Pretty.string_of (Args.pretty_src ctxt src) ;

val thy = ML_Context.the_context () ;
val ctxt = ProofContext.init thy ;
map (pr_src ctxt) ass ;

```

So an `Args.src` consists of the first word, then a list of further “arguments”, of type `Args.T`, with information about position in the input.

```

(* how an Args.src is parsed *)
P.position : 'a tlp -> ('a * Position.T) tlp ;
P.arguments : Args.T list tlp ;

val parse_src : Args.src tlp =

```

```

P.position (P.xname -- P.arguments) >> Args.src ;

val ((first_word, args), pos) = Args.dest_src asrc ;
map Args.string_of args ;

```

The Args structure contains more parsers and parser transformers for which the input source type is Args.T list. For example,

```

type 'a atlp = Args.T list -> 'a * Args.T list ;
open Args ;
nat : int atlp ; (* also Args.int *)
thm_sel : PureThy.interval list atlp ;
list : 'a atlp -> 'a list atlp ;
attribs : (string -> string) -> Args.src list atlp ;
opt_attribs : (string -> string) -> Args.src list atlp ;

(* parse_atl_str : 'a atlp -> (string -> 'a * string) ;
   given an Args.T list parser, to get a string parser *)
fun parse_atl_str atlp str =
let val (ats, rem_str) = parse_str P.arguments str ;
    val (res, rem_ats) = atlp ats ;
in (res, String.concat (Library.separate " "
(List.map Args.string_of rem_ats @ [rem_str]))) end ;

parse_atl_str Args.int "-1-," ;
parse_atl_str (Scan.option Args.int) "x1-," ;
parse_atl_str Args.thm_sel "(1-,4,13-22)" ;

val (ats as atsrc :: _, "") = parse_atl_str (Args.attribs I)
"[THEN trans [THEN sym], simp, OF sym]" ;

```

From here, an attribute is interpreted using Attrib.attribute.

Args has a large number of functions which parse an Args.src and also refer to a generic context. Note the use of Scan.lift for this. (as does Attrib - RETHINK THIS)

(Args.syntax shown below has type specialised)

```

type ('res, 'src) parse_fn = 'src -> 'res * 'src ;
type 'a cgatlp = ('a, Context.generic * Args.T list) parse_fn ;
Scan.lift : 'a atlp -> 'a cgatlp ;
term : term cgatlp ;

```

```

typ : typ cgatlp ;

Args.syntax : string -> 'res cgatlp -> src -> ('res, Context.generic) parse_fn ;
Attrib.thm : thm cgatlp ;
Attrib.thms : thm list cgatlp ;
Attrib.multi_thm : thm list cgatlp ;

(* parse_cgatl_str : 'a cgatlp -> (string -> 'a * string) ;
given a (Context.generic * Args.T list) parser, to get a string parser *)
fun parse_cgatl_str cgatlp str =
let
  (* use the current generic context *)
  val generic = Context.Theory thy ;
  val (ats, rem_str) = parse_str P.arguments str ;
  (* ignore any change to the generic context *)
  val (res, (_, rem_ats)) = cgatlp (generic, ats) ;
in (res, String.concat (Library.separate " "
  (List.map Args.string_of rem_ats @ [rem_str]))) end ;

```

3.7 Attributes, and the `Attrib` structure

The type `attribute` is declared in `src/Pure/thm.ML`. The source file for the `Attrib` structure is `src/Pure/Isar/attrib.ML`. Most attributes use a theorem to change a generic context (for example, by declaring that the theorem should be used, by default, in simplification), or change a theorem (which most often involves referring to the current theory). The functions `Thm.rule_attribute` and `Thm.declaration_attribute` create attributes of these kinds.

```

type attribute = Context.generic * thm -> Context.generic * thm;
type 'a trf = 'a -> 'a ; (* transformer of a given type *)
Thm.rule_attribute : (Context.generic -> thm -> thm) -> attribute ;
Thm.declaration_attribute : (thm -> Context.generic trf) -> attribute ;

Attrib.print_attributes : theory -> unit ;
Attrib.pretty_attribs : Proof.context -> src list -> Pretty.T list ;

List.app Pretty.writeln (Attrib.pretty_attribs ctxt ass) ;

```

An attribute is stored in a theory as indicated by:

```

Attrib.add_attributes :
(bstring * (src -> attribute) * string) list -> theory trf ;
(*
Attrib.add_attributes [("THEN", THEN_att, "resolution with rule")] ;
*)

```

where the first and third arguments are name and description of the attribute, and the second is a function which parses the attribute input text (including the attribute name, which has necessarily already been parsed). Here, `THEN_att` is a function declared in the code for the structure `Attrib`, but not published in its signature. The source file `src/Pure/Isar/attrib.ML` shows the use of `Attrib.add_attributes` to add a number of attributes.

```

FullAttrib.THEN_att : src -> attribute ;
FullAttrib.THEN_att atsrc (generic, ML_Context.thm "sym") ;
FullAttrib.THEN_att atsrc (generic, ML_Context.thm "all_comm") ;

```

```

Attrib.syntax : attribute cgatlp -> src -> attribute ;
Attrib.no_args : attribute -> src -> attribute ;

```

When this is called as `syntax scan src (gc, th)` the generic context `gc` is used (and potentially changed to `gc'`) by `scan` in parsing to obtain an attribute `attr` which would then be applied to `(gc', th)`. The source for parsing the attribute is the arguments part of `src`, which must all be consumed by the parse.

For example, for `Attrib.no_args attr src`, the attribute parser simply returns `attr`, requiring that the arguments part of `src` must be empty.

Some examples from `src/Pure/Isar/attrib.ML`, modified:

```

fun rot_att_n n (gc, th) = (gc, rotate_prem n th) ;
rot_att_n : int -> attribute ;
val rot_arg = Scan.lift (Scan.optional Args.int 1 : int atlp) : int cgatlp ;
val rotated_att : src -> attribute =
Attrib.syntax (rot_arg >> rot_att_n : attribute cgatlp) ;

val THEN_arg : int cgatlp = Scan.lift
(Scan.optional (Args.bracks Args.nat : int atlp) 1 : int atlp) ;

Attrib.thm : thm cgatlp ;

THEN_arg -- Attrib.thm : (int * thm) cgatlp ;

```

```

fun THEN_att_n (n, tht) (gc, th) = (gc, th RSN (n, tht)) ;
THEN_att_n : int * thm -> attribute ;

val THEN_arg : src -> attribute = Attrib.syntax
(THEN_arg -- Attrib.thm >> THEN_att_n : attribute cgoalp);

```

The functions I've called `rot_arg` and `THEN_arg` read an optional argument, which for `rotated` is an integer, and for `THEN` is a natural enclosed in square brackets; the default, if the argument is absent, is 1 in each case. Functions `rot_att_n` and `THEN_att_n` turn these into attributes, where `THEN_att_n` also requires a theorem, which is parsed by `Attrib.thm`. Infix operators `--` and `>>` are in the structure `Scan`.

3.8 Methods, and the Method structure

The source file is `src/Pure/Isar/method.ML`. The type `method` is defined by the datatype declaration

```

(* datatype method = Meth of thm list -> cases_tactic; *)
RuleCases.NO_CASES : tactic -> cases_tactic ;

```

In fact `RAW_METHOD_CASES` (below) is exactly the constructor `Meth`. A `cases_tactic` is an elaborated version of a tactic. `NO_CASES tac` is a `cases_tactic` which consists of a `cases_tactic` without any further case information. For further details see the description of structure `RuleCases` below. The list of theorems to be passed to a method consists of the current *facts* in the proof.

```

RAW_METHOD : (thm list -> tactic) -> method ;
METHOD : (thm list -> tactic) -> method ;

SIMPLE_METHOD : tactic -> method ;
SIMPLE_METHOD' : (int -> tactic) -> method ;
SIMPLE_METHOD'' : ((int -> tactic) -> tactic) -> (int -> tactic) -> method ;

RAW_METHOD_CASES : (thm list -> cases_tactic) -> method ;
METHOD_CASES : (thm list -> cases_tactic) -> method ;

```

A method is, in its simplest form, a tactic; applying the method is to apply the tactic to the current goal state.

Applying `RAW_METHOD tacf` creates a tactic by applying `tacf` to the current facts, and applying that tactic to the goal state.

`METHOD` is similar but also first applies `Goal.conjunction_tac` to all subgoals.

`SIMPLE_METHOD tac` inserts the facts into all subgoals and then applies `tacf`.

`SIMPLE_METHOD' tacf` inserts the facts and then applies `tacf` to subgoal 1.

`SIMPLE_METHOD'' quant tacf` does this for subgoal(s) selected by `quant`, which may be, for example, `ALLGOALS` (all subgoals), `TRYALL` (try all subgoals, failure is OK), `FIRSTGOAL` (try subgoals until it succeeds once), `(fn tacf => tacf 4)` (subgoal 4), etc (see the `Tactical` structure, [?, Chapter 4]).

A method is stored in a theory as indicated by:

```
Method.add_method :  
  (bstring * (src -> Proof.context -> method) * string) -> theory trf ;  
  ( *  
  * )
```

where the first and third arguments are name and description of the method, and the second is a function which parses the method input text (including the method name, which has necessarily already been parsed).

Here, `xxx` is a function declared in the code for the structure `Method`, but not published in its signature. The source file `src/Pure/Isar/method.ML` shows the use of `Method.add_method` to add a number of methods.

Appendix A

Recipes

A.1 Accumulate a List of Theorems under a Name

Problem: Your tool *foo* works with special rules, called *foo*-rules.

Users should be able to declare *foo*-rules in the theory, which are then used by some method.

```
ML {*  
  structure FooRules = NamedThmsFun(  
    val name = "foo"  
    val description = "Rules for foo"  
  );  
*}
```

```
setup FooRules.setup
```

This declares a context data slot where the theorems are stored, an attribute *foo* (with the usual *add* and *del* options to declare new rules, and the internal ML interface to retrieve and modify the facts.

Furthermore, the facts are made available under the dynamic fact name *foo*:

```
lemma rule1[foo]: "A" sorry  
lemma rule2[foo]: "B" sorry
```

```
declare rule1[foo del]
```

thm *foo*

```
ML {*  
  FooRules.get @{context};  
*}
```

For more information see `Pure/Tools/named_thms.ML`.

[Read More](#)

A.2 Ad-hoc Transformations of Theorems

Bibliography

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