## Homework 2

- 1. What is the meaning of a regular expression? Give an inductive definition.
- 2. Given the regular expressions  $r_1 = \epsilon$  and  $r_2 = \emptyset$  and  $r_3 = a$ . How many strings can the regular expressions  $r_1^*$ ,  $r_2^*$  and  $r_3^*$  each match?
- 3. Give regular expressions for (a) decimal numbers and for (b) binary numbers. (Hint: Observe that the empty string is not a number. Also observe that leading 0s are normally not written.)
- 4. Decide whether the following two regular expressions are equivalent  $(\epsilon + a)^* \equiv a^*$  and  $(a \cdot b)^* \cdot a \equiv a \cdot (b \cdot a)^*$ .
- 5. Given the regular expression  $r = (a \cdot b + b)^*$ . Compute what the derivative of *r* is with respect to *a* and *b*. Is *r* nullable?
- 6. What is a regular language?
- 7. Prove that for all regular expressions r we have

 $\operatorname{nullable}(r)$  if and only if ""  $\in L(r)$