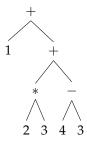
Handout 8 (A Functional Language)

The language we looked at in the previous lecture was rather primitive and the compiler rather crude. In this handout we like to have a look at a slightly more comfortable language and a tiny-teeny bit more realistic compiler. A small collection of programs we want to be able to write and compile is as follows:

We will still restrict us to just programs about integers, that means for example that every function needs to return an integer. The grammar of the Funlanguage is slightly simpler than the While-language, because almost everything is an expression. The grammar rules are as follows:

where $\langle Id \rangle$ stands for variables and $\langle Num \rangle$ for numbers. For the moment let us omit variables from arithmetic expressions. Our parser will take this grammar and given an input produce abstract syntax trees. For example for the expression 1 + ((2*3) + (4-3)) it will produce the following tree.



To generate code for this expression, we need to traverse this tree in post-order fashion and emit code for each node—this traversal in post-order fashion will produce code for a stack-machine (what the JVM is). Doing so for the tree above generates the instructions

ldc 1 ldc 2 ldc 3 imul ldc 4 ldc 3 isub iadd

If we "run" these instructions, the result 8 will be on top of the stack (I leave this to you to verify; the meaning of each instruction should be clear). The result being on the top of the stack will be a convention we always observe in our compiler, that is the results of arithmetic expressions will always be on top of the stack. Note, that a different bracketing of the expression, for example (1 + (2*3)) + (4-3), produces a different abstract syntax tree and thus potentially also a different list of instructions. Generating code in this fashion is rather easy to implement: it can be done with the following recursive *compile*-function, which takes the abstract syntax tree as argument:

$$\begin{array}{lll} \textit{compile}(n) & \stackrel{\text{def}}{=} & \mathsf{ldc} \; n \\ \textit{compile}(a_1 + a_2) & \stackrel{\text{def}}{=} & \textit{compile}(a_1) \; @ \; \textit{compile}(a_2) \; @ \; \mathsf{iadd} \\ \textit{compile}(a_1 - a_2) & \stackrel{\text{def}}{=} & \textit{compile}(a_1) \; @ \; \textit{compile}(a_2) \; @ \; \mathsf{isub} \\ \textit{compile}(a_1 * a_2) & \stackrel{\text{def}}{=} & \textit{compile}(a_1) \; @ \; \textit{compile}(a_2) \; @ \; \mathsf{imul} \\ \textit{compile}(a_1 \backslash a_2) & \stackrel{\text{def}}{=} & \textit{compile}(a_1) \; @ \; \textit{compile}(a_2) \; @ \; \mathsf{idiv} \\ \end{array}$$

However, our arithmetic expressions can also contain variables. We will represent them as *local variables* in the JVM. Essentially, local variables are an array or pointers to memory cells, containing in our case only integers. Looking up a variable can be done with the instruction

iload index

which places the content of the local variable *index* onto the stack. Storing the top of the stack into a local variable can be done by the instruction

istore index

Note that this also pops off the top of the stack. One problem we have to overcome, however, is that local variables are addressed, not by identifiers, but by numbers (starting from 0). Therefore our compiler needs to maintain a kind of environment where variables are associated to numbers. This association needs to be unique: if we muddle up the numbers, then we essentially confuse variables and the consequence will usually be an erroneous result. Our extended *compile*-function for arithmetic expressions will therefore take two arguments: the abstract syntax tree and the environment, *E*, that maps identifiers to indexnumbers.

```
\begin{array}{lll} compile(n,E) & \stackrel{\mathrm{def}}{=} & \mathsf{ldc} \ n \\ compile(a_1+a_2,E) & \stackrel{\mathrm{def}}{=} & compile(a_1,E) @ compile(a_2,E) @ \mathsf{iadd} \\ compile(a_1-a_2,E) & \stackrel{\mathrm{def}}{=} & compile(a_1,E) @ compile(a_2,E) @ \mathsf{isub} \\ compile(a_1*a_2,E) & \stackrel{\mathrm{def}}{=} & compile(a_1,E) @ compile(a_2,E) @ \mathsf{imul} \\ compile(a_1\backslash a_2,E) & \stackrel{\mathrm{def}}{=} & compile(a_1,E) @ compile(a_2,E) @ \mathsf{idiv} \\ compile(x,E) & \stackrel{\mathrm{def}}{=} & \mathsf{iload} \ E(x) \end{array}
```

In the last line we generate the code for variables where E(x) stands for looking up the environment to which index the variable x maps to.

There is a similar *compile*-function for boolean expressions, but it includes a "trick" to do with if- and while-statements. To explain the issue let us first describe the compilation of statements of the While-language. The clause for skip is trivial, since we do not have to generate any instruction

$$compile(skip, E) \stackrel{\text{def}}{=} ([], E)$$

[] is the empty list of instructions. Note that the *compile*-function for statements returns a pair, a list of instructions (in this case the empty list) and an environment for variables. The reason for the environment is that assignments in the While-language might change the environment—clearly if a variable is used for the first time, we need to allocate a new index and if it has been used before, we need to be able to retrieve the associated index. This is reflected in the clause for compiling assignments:

$$compile(x := a, E) \stackrel{\text{def}}{=} (compile(a, E) @ istore index, E')$$

We first generate code for the right-hand side of the assignment and then add an istore-instruction at the end. By convention the result of the arithmetic expression a will be on top of the stack. After the istore instruction, the result will be stored in the index corresponding to the variable x. If the variable x has been used before in the program, we just need to look up what the index is

and return the environment unchanged (that is in this case E' = E). However, if this is the first encounter of the variable x in the program, then we have to augment the environment and assign x with the largest index in E plus one (that is $E' = E(x \mapsto largest_index + 1)$). That means for the assignment x := x + 1 we generate the following code

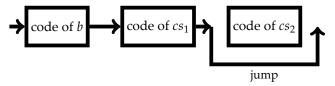
```
iload n_x ldc 1 iadd istore n_x
```

where n_x is the index for the variable x.

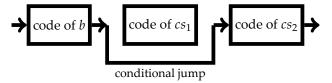
More complicated is the code for if-statments, say

```
if b then cs_1 else cs_2
```

where b is a boolean expression and the $cs_{1/2}$ are the statements for each ifbranch. Lets assume we already generated code for b and $cs_{1/2}$. Then in the true-case the control-flow of the program needs to be



where we start with running the code for b; since we are in the true case we continue with running the code for cs_1 . After this however, we must not run the code for cs_2 , but always jump after the last instruction of cs_2 (the code for the else-branch). Note that this jump is unconditional, meaning we always have to jump to the end of cs_2 . The corresponding instruction of the JVM is goto. In case b turns out to be false we need the control-flow



where we now need a conditional jump (if the if-condition is false) from the end of the code for the boolean to the beginning of the instructions cs_2 . Once we are finished with running cs_2 we can continue with whatever code comes after the if-statement.

The goto and the conditional jumps need addresses to where the jump should go. Since we are generating assembly code for the JVM, we do not actually have to give (numeric) addresses, but can just attach (symbolic) labels to our code. These labels specify a target for a jump. Therefore the labels need to be unique, as otherwise it would be ambiguous where a jump should go to. A label, say L, is attached to code like

```
L: instr_1 instr_2
```

where a label is indicated by a colon.

Recall the "trick" with compiling boolean expressions: the *compile*-function for boolean expressions takes three arguments: an abstract syntax tree, an environment for variable indices and also the label, lab, to where an conditional jump needs to go. The clause for the expression $a_1 = a_2$, for example, is as follows:

$$compile(a_1 = a_2, E, lab) \stackrel{\text{def}}{=} \\ compile(a_1, E) @ compile(a_2, E) @ if_icmpne \ lab$$

where we are first generating code for the subexpressions a_1 and a_2 . This will mean after running the corresponding code there will be two integers on top of the stack. If they are equal, we do not have to do anything (except for popping them off from the stack) and just continue with the next instructions (see control-flow of ifs above). However if they are *not* equal, then we need to (conditionally) jump to the label lab. This can be done with the instruction

```
if_icmpne lab
```

Other jump instructions for boolean operators are

$$\begin{array}{cccc} \neq & \Rightarrow & & \text{if_icmpeq} \\ < & \Rightarrow & & \text{if_icmpge} \\ \leq & \Rightarrow & & \text{if_icmpgt} \end{array}$$

and so on. I leave it to you to extend the *compile*-function for the other boolean expressions. Note that we need to jump whenever the boolean is *not* true, which means we have to "negate" the jump condition—equals becomes not-equal, less becomes greater-or-equal. If you do not like this design (it can be the source of some nasty, hard-to-detect errors), you can also change the layout of the code and first give the code for the else-branch and then for the if-branch. However in the case of while-loops this way of generating code still seems the most convenient.

We are now ready to give the compile function for if-statments—remember this function returns for staments a pair consisting of the code and an environment:

```
\begin{array}{l} \textit{compile}(\texttt{if}\ b\ \texttt{then}\ cs_1\ \texttt{else}\ cs_2, E) & \stackrel{\text{def}}{=} \\ L_{\textit{ifelse}}\ \ (\texttt{fresh}\ label) \\ L_{\textit{ifend}}\ \ (\texttt{fresh}\ label) \\ (\textit{is}_1, E') = \textit{compile}(cs_1, E) \\ (\textit{is}_2, E'') = \textit{compile}(cs_2, E') \\ (\textit{compile}(b, E, L_{\textit{ifelse}}) \\ @\ \textit{is}_1 \\ @\ \texttt{goto}\ L_{\textit{ifend}} \\ @\ L_{\textit{ifelse}}: \\ @\ \textit{is}_2 \\ @\ L_{\textit{ifend}}:, E'') \end{array}
```

In the first two lines we generate two fresh labels for the jump addresses (just before the else-branch and just after). In the next two lines we generate the instructions for the two branches, is_1 and is_2 . The final code will be first the code for b (including the label just-before-the-else-branch), then the goto for after the else-branch, the label L_{ifesle} , followed by the instructions for the else-branch, followed by the after-the-else-branch label. Consider for example the if-statement:

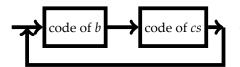
```
if 1 = 1 then x := 2 else y := 3
```

The generated code is as follows:

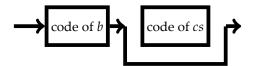
```
1    ldc 1
2    ldc 1
3    if_icmpne L_ifelse
4    ldc 2
5    istore 0
6    goto L_ifend
7    L_ifelse:
8    ldc 3
9    istore 1
10    L_ifend:
```

The first three lines correspond to the the boolean expression 1 = 1. The jump for when this boolean expression is false is in Line 3. Lines 4-6 corresponds to the if-branch; the else-branch is in Lines 8 and 9. Note carefully how the environment E is threaded through the recursive calls of *compile*. The function receives an environment E, but it might extend it when compiling the if-branch, yielding E'. This happens for example in the if-statement above whenever the variable x has not been used before. Similarly with the environment E'' for the second call to *compile*. E'' is also the environment that needs to be returned as part of the answer.

The compilation of the while-loops, say while b do cs, is very similar. In case the condition is true and we need to do another iteration, and the control-flow needs to be as follows



Whereas if the condition is *not* true, we need to jump out of the loop, which gives the following control flow.



Again we can use the *compile*-function for boolean expressions to insert the appropriate jump to the end of the loop (label L_{wend} below).

```
compile( \mbox{while } b \mbox{ do } cs, E) \stackrel{\mathrm{def}}{=} L_{wbegin} \  \, ( \mbox{fresh label}) \  \, L_{wend} \  \, ( \mbox{fresh label}) \  \, ( \mbox{is, } E') = compile(cs_1, E) \  \, ( L_{wbegin} : \  \, @ \mbox{compile}(b, E, L_{wend}) \  \, @ \mbox{is} \  \, @ \mbox{goto } L_{wbegin} \  \, @ L_{wend} :, E')
```

I let you go through how this clause works. As an example you can consider the while-loop

```
while x \le 10 do x := x + 1 yielding the following code
```

L_wbegin:
iload 0
ldc 10
if_icmpgt L_wend
iload 0
ldc 1
iadd
istore 0
goto L_wbegin
L wend:

Next we need to consider the statement write x, which can be used to print out the content of a variable. For this we need to use a Java library function. In order to avoid having to generate a lot of code for each write-command, we use

a separate helper-method and just call this method with an argument (which needs to be placed onto the stack). The code of the helper-method is as follows.

```
.method public static write(I)V
.limit locals 1
.limit stack 2
getstatic java/lang/System/out Ljava/io/PrintStream;
iload 0
invokevirtual java/io/PrintStream/println(I)V
return
.end method
```

The first line marks the beginning of the method, called write. It takes a single integer argument indicated by the (I) and returns no result, indicated by the V. Since the method has only one argument, we only need a single local variable (Line 2) and a stack with two cells will be sufficient (Line 3). Line 4 instructs the JVM to get the value of the field out of the class java/lang/System. It expects the value to be of type java/io/PrintStream. A reference to this value will be placed on the stack. Line 5 copies the integer we want to print out onto the stack. In the next line we call the method println (from the class java/io/PrintStream). We want to print out an integer and do not expect anything back (that is why the type annotation is (I)V). The return-instruction in the next line changes the control-flow back to the place from where write was called. This method needs to be part of a header that is included in any code we generate. The helper-method write can be invoked with the two instructions

```
i iload E(x) invokestatic XXX/XXX/write(I)V
```

where we first place the variable to be printed on top of the stack and then call write. The XXX need to be replaced by an appropriate class name (this will be explained shortly).

By generating code for a While-program, we end up with a list of (JVM assembly) instructions. Unfortunately, there is a bit more boilerplate code needed before these instructions can be run. The complete code is shown in Figure 1. This boilerplate code is very specific to the JVM. If we target any other virtual machine or a machine language, then we would need to change this code. Lines 4 to 8 in Figure 1 contain a method for object creation in the JVM; this method is called *before* the main-method in Lines 10 to 17. Interesting are the Lines 11 and 12 where we hardwire that the stack of our programs will never be larger than 200 and that the maximum number of variables is also 200. This seem to be conservative default values that allow is to run some simple While-programs. In a real compiler, we would of course need to work harder and find out appropriate values for the stack and local variables.

To sum up, in Figure 2 is the complete code generated for the slightly non-sensical program

```
.class public XXX.XXX
  .super java/lang/Object
  .method public <init>()V
       aload_0
       invokenonvirtual java/lang/Object/<init>()V
      return
  .end method
  .method public static main([Ljava/lang/String;)V
       .limit locals 200
11
       .limit stack 200
12
13
         ...here comes the compiled code...
15
      return
  .end method
```

Figure 1: Boilerplate code needed for running generated code.

```
1  X := 1 + 2;
2  write X
```

Having this code at our disposal, we need the assembler to translate the generated code into JVM bytecode (a class file). This bytecode is understood by the JVM and can be run by just invoking the java-program.

```
.class public test.test
  .super java/lang/Object
  .method public <init>()V
      aload_0
      invokenonvirtual java/lang/Object/<init>()V
      return
  .end method
  .method public static write(I)V
10
       .limit locals 1
11
       .limit stack 2
12
       getstatic java/lang/System/out Ljava/io/PrintStream;
13
       iload 0
14
       invokevirtual java/io/PrintStream/println(I)V
       return
16
  .end method
18
   .method public static main([Ljava/lang/String;)V
      .limit locals 200
20
      .limit stack 200
21
      ldc 1
22
      ldc 2
23
      iadd
24
      istore 0
      iload 0
      invokestatic test/test/write(I)V
27
      return
  .end method
```

Figure 2: Generated code for a test program. This code can be processed by an Java assembler producing a class-file, which can be run by the <code>java-program</code>.