Compilers and Formal Languages

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Compilers & Boeings 777

First flight in 1994. They want to achieve triple redundancy in hardware faults.

They compile 1 Ada program to

• Intel 80486

- Motorola 68040 (old Macintosh's)
- AMD 29050 (RISC chips used often in laser printers) using 3 independent compilers.

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Airbus uses C and static analysers. Recently started using CompCert.



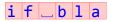
- verified a microkernel operating system (\approx 8000 lines of C code)
- US DoD has competitions to hack into drones; they found that the isolation guarantees of seL4 hold up
- CompCert and seL4 sell their code

POSIX Matchers

• Longest match rule ("maximal munch rule"): The longest initial substring matched by any regular expression is taken as the next token.

iffoo_bla

• Rule priority: For a particular longest initial substring, the first regular expression that can match determines the token.



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Kuklewicz: most POSIX matchers are buggy http://www.haskell.org/haskellwiki/Regex_Posix

def der $c(\mathbf{0})$ 0 def der c(1)0 def der c(d)def == der c $(r_1 + r_2)$ def der c $(\mathbf{r}_1 \cdot \mathbf{r}_2)$ if nullable(r_1) def $(der \ c \ r) \cdot (r^*)$ der c (r^*) def = der c $(r^{\{n\}})$ if n = 0 then **0** $\stackrel{\text{def}}{=}$ if n = 0 then **0** der c $(r^{\uparrow n})$

if c = d then 1 else 0 $(der \ c \ r_1) + (der \ c \ r_2)$ then $((\operatorname{der} \operatorname{c} r_1) \cdot r_2) + (\operatorname{der} \operatorname{c} r_2)$ else (der c r_1) · r_2 else if nullable(r) then (der c r) \cdot (r^{{n-1}}) else (der c r) · $(r^{\{n-1\}})$ else (der c r) · ($r^{\{\uparrow n-1\}}$)

Proofs about Rexps

Remember their inductive definition:

```
 \begin{array}{c} ::= & \mathbf{0} \\ & | & \mathbf{1} \\ & | & c \\ & | & r_1 \cdot r_2 \\ & | & r_1 + r_2 \\ & | & r^* \\ & | & r^{\{n\}} \\ & | & r^{\{n\}} \\ & | & r^{\{\uparrow n\}} \end{array}
```

If we want to prove something, say a property P(r), for all regular expressions r then ...

Proofs about Rexp (2)

- P holds for 0, 1 and c
- P holds for $r_1 + r_2$ under the assumption that P already holds for r_1 and r_2 .
- *P* holds for $r_1 \cdot r_2$ under the assumption that *P* already holds for r_1 and r_2 .
- *P* holds for *r*^{*} under the assumption that *P* already holds for *r*.

Proofs about Strings

If we want to prove something, say a property P(s), for all strings s then ...

- *P* holds for the empty string, and
- P holds for the string c::s under the assumption that P already holds for s

Correctness of the Matcher

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where matches $r s \stackrel{\text{def}}{=} nullable(ders s r)$

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• We want to prove

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• We can do this, if we know

 $L(der \ c \ r) = Der \ c \ (L(r))$

Some Lemmas

- Der c $(A \cup B) = (Der c A) \cup (Der c B)$
- If $[] \in A$ then Der $c (A @ B) = (Der c A) @ B \cup (Der c B)$
- If [] \notin A then Der c (A @ B) = (Der c A) @ B
- Der c $(A^*) = (Der c A) @A^*$

(interesting case)

Why?

Why does *Der c* $(A^*) = (Der c A) @ A^*$ hold?

$$Der c (A^*) = Der c (A^* - \{[]\})$$

= Der c ((A - {[]})@A^*)
= (Der c (A - {[]}))@A^*
= (Der c A)@A^*

using the facts Der c A = Der c $(A - \{[]\})$ and $(A - \{[]\}) @A^* = A^* - \{[]\}$

POSIX Spec

 $[] \in 1 \rightarrow Empty$ $\overline{c \in c \rightarrow Char(c)}$ $s \in r_1 \rightarrow v$ $s \in r_2 \rightarrow v$ $s \notin L(r_1)$

 $\overline{s \in r_1 + r_2 \rightarrow Left(v)}$

 $\frac{s \in r_2 \to v \quad s \notin L(r_1)}{s \in r_1 + r_2 \to Right(v)}$

 $s_1 \in r_1 \rightarrow \nu_1$ $s_2 \in r_2 \rightarrow \nu_2$ $\neg (\exists s_3 s_4. s_3 \neq [] \land s_3 @ s_4 = s_2 \land s_1 @ s_3 \in L(r_1) \land s_4 \in L(r_2))$ $s_1 @ s_2 \in r_1 \cdot r_2 \rightarrow Seq(\nu_1, \nu_2)$

. . .

Sulzmann & Lu Paper

• I have no doubt the algorithm is correct — the problem is I do not believe their proof.

"How could I miss this? Well, I was rather careless when stating this Lemma :)

Great example how formal machine checked proofs (and proof assistants) can help to spot flawed reasoning steps."

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Lemma 3 (Projection and Injection). Let r be a regular expression, l a letter and v a parse tree.

1. If $\vdash v : r$ and |v| = lw for some word w, then $\vdash proj_{(r,l)} v : r \setminus l$.

2. If $\vdash v : r \setminus l$ then $(proj_{(r,l)} \circ inj_{r \setminus l}) v = v$.

3. If $\vdash v : r$ and |v| = lw for some word w, then $(inj_{r \setminus l} \circ proj_{(r,l)}) v = v$.

MS:BUG[Come accross this issue when going back to our constructive reg-ex work] Consider $\vdash [Right (), Left a] : (a + \epsilon)^*$. However, $proj_{((a+\epsilon)^*,a)}$ [Right (), Left a] fails! The point is that proj only works correctly if applied on POSIX parse trees.

MS:Possible fixes We only ever apply proj on Posix parse trees.

For convenience, we write " $\vdash v : r$ is POSIX" where we mean that $\vdash v : r$ holds and v is the POSIX parse tree of r for word |v|.

Lemma 2 follows from the following statement.