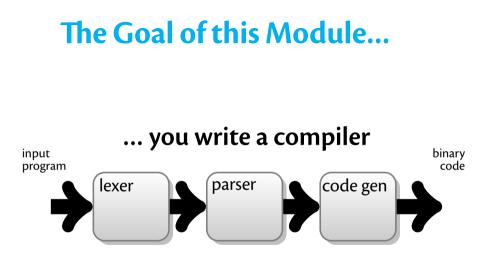
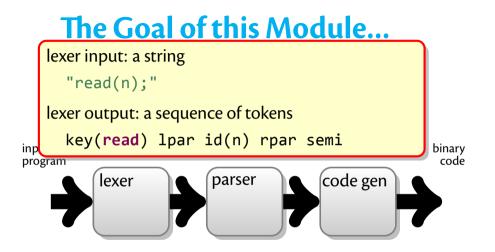
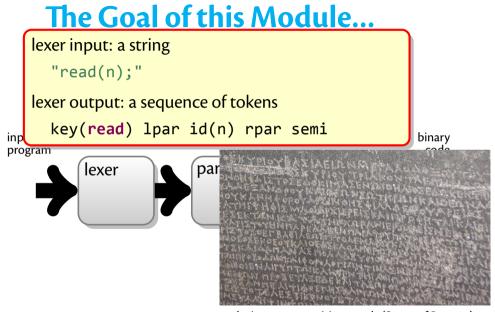
### Compilers and Formal Languages

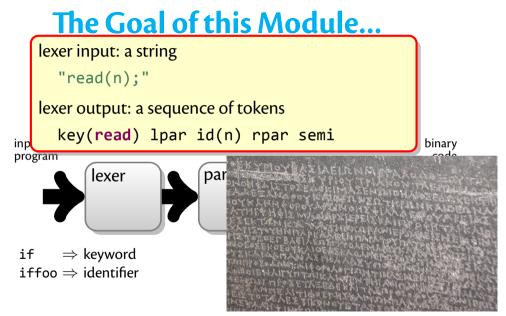
#### Email: christian.urban at kcl.ac.uk Slides & Progs: KEATS

1 Introduction, Languages	6 While-Language
2 Regular Expressions, Derivatives	7 Compilation, JVM
3 Automata, Regular Languages	8 Compiling Functional Languages
4 Lexing, Tokenising	9 Optimisations
5 Grammars, Parsing	10 LLVM

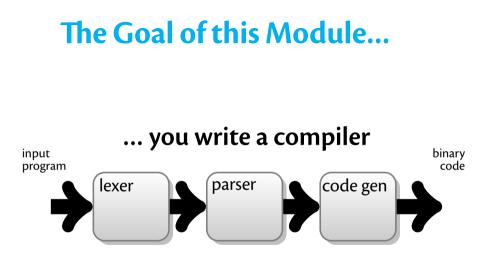


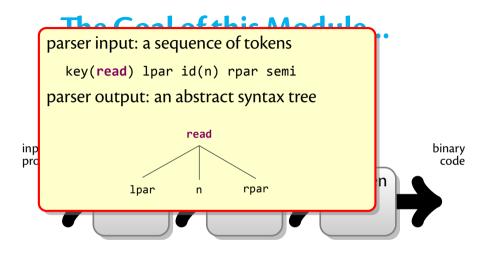


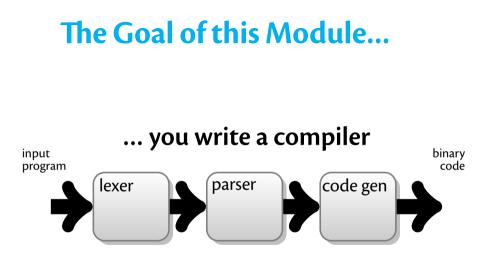


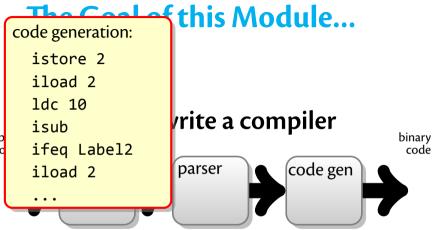


 $lexing \Rightarrow recognising words (Stone of Rosetta)_{I, King's College London - p. 2/30}$ 

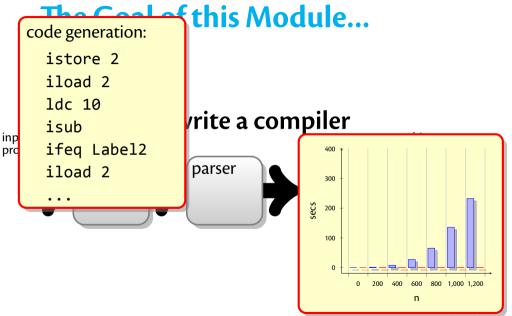






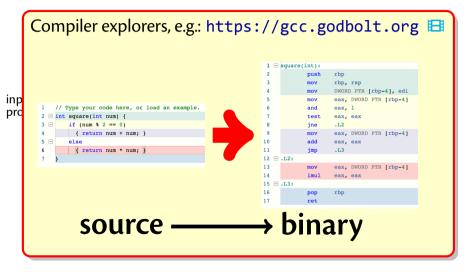


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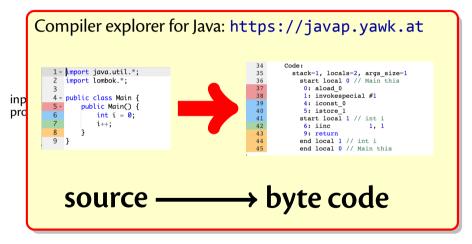


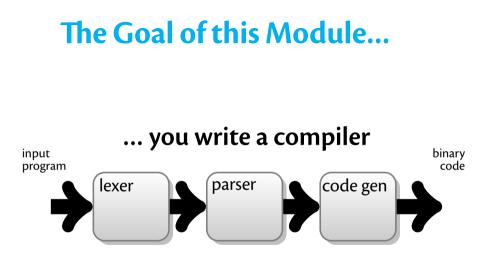
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### The Goal of this Module...



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### Why Study Compilers?

John Regehr (Univ. Utah, LLVM compiler hacker) 🖒

"...It's effectively a perpetual employment act for solid compiler hackers."

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# • Hardware is getting weirder rather than getting clocked faster.

"Almost all processors are multicores nowadays and it looks like there is increasing asymmetry in resources across cores. Processors come with vector units, crypto accelerators etc. We have DSPs, GPUs, ARM big.little, and Xeon Phi. This is only scratching the surface."

### Why Study Compilers?

John Regehr (Univ. Utah, LLVM compiler hacker) 🖒

"...It's effectively a perpetual employment act for solid compiler hackers."

# • We're getting tired of low-level languages and their associated security disasters.

"We want to write new code, to whatever extent possible, in safer, higher-level languages. Compilers are caught right in the middle of these opposing trends: one of their main jobs is to help bridge the large and growing gap between increasingly high-level languages and increasingly wacky platforms."

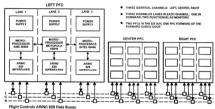
### Why Bother with Compilers?

**Boeing 777's**: First flight in 1994. They want to achieve triple redundancy for potential hardware faults.

They compile 1 Ada program to

- Intel 80486
- Motorola 68040 (old Macintosh's)
- AMD 29050 (RISC chips used often in laser printers)

using 3 independent compilers.



## Why Bother with Compilers?

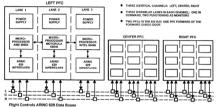
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Airbus uses C and static analysers. Recently started using CompCert.



### What Do Compilers Do?

#### Remember BF\*\*\* from PEP?

- $\Rightarrow$  move one cell right
- +  $\Rightarrow$  increase cell by one
- $\Rightarrow$  decrease cell by one
- .  $\Rightarrow$  print current cell
- ,  $\Rightarrow$  input current cell
- $[ \Rightarrow loop begin$
- ]  $\Rightarrow$  loop end
  - $\Rightarrow$  everything else is a comment

char field[30000] char \*ptr = &field[15000]

- $\Rightarrow$  ignore everything else
- $1 \Rightarrow \}$
- $\Rightarrow$  while(\*ptr){
- $\Rightarrow$  \*ptr = getchar()

$$\Rightarrow$$
 putchar(\*ptr)

$$\Rightarrow$$
 (\*ptr)--

$$+ \Rightarrow (*ptr)++$$

 $\rightarrow$  ptr++

<

$$\Rightarrow$$
 (\*ptr)++

$$\Rightarrow$$
 ptr--

A "Compiler" for BF\*\*\* to C

$$\Rightarrow$$
 ptr--  
 $\Rightarrow$  (\*ptr)++

$$\Rightarrow$$
 (\*ptr)++  
 $\Rightarrow$  (\*ptr)--

char field[30000] char \*ptr = &field[15000]

 $\Rightarrow$  ignore everything else

$$\Rightarrow$$
 while(\*ptr){  
 $\Rightarrow$  }

. 
$$\Rightarrow$$
 putchar(\*ptr)  
,  $\Rightarrow$  \*ptr = getchar()

$$\Rightarrow$$
 putchar(\*ptr)

$$-\dots - \Rightarrow (*ptr) -= n$$

$$<... < \Rightarrow ptr -= n$$
  
 $+...+ \Rightarrow (*ptr) += n$ 

$$\rightarrow ... \rightarrow ptr += n$$

### **A Brief Compiler History**

- Turing Machines, 1936 (a tape as memory)
- Regular Expressions, 1956
- The first compiler for COBOL, 1957 (Grace Hopper)
- But surprisingly research papers are still published nowadays
- "Parsing: The Solved Problem That Isn't" 🖒



Grace Hopper (she made it to David Letterman's Tonight Show 🖒

#### Exams will be online:

- final exam in January (30%)
- mid-term shortly after Reading Week (10%)
- weekly engagement (10%)

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#### Weekly Homework (optional):

- uploaded on KEATS, send answers via email, responded individually
- all questions in the exam and mid-term will be from the HW!!

#### Coursework (5 accounting for 45%):

- matcher (5%)
- lexer (8%)
- parser / interpreter (10%)
- JVM compiler (10%)
- LLVM compiler (12%)

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### Lectures 1 - 5

transforming strings into structured data

**Lexing** based on regular expressions (recognising "words")

### Parsing

(recognising "sentences")



Stone of Rosetta

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Stone of Rosetta

### **Lectures 5 - 10**

code generation for a small imperative and a small functional language

### Interpreters

(directly runs a program)

### Compilers

(generate JVM code and LLVM-IR code)



### **Familiar Regular Expresssions**

[a-z0-9].-]+ @ [a-z0-9].-]+ . [a-z]{2,6}

- re\* matches 0 or more times
- re+ matches 1 or more times
- re? matches 0 or 1 times
- re{n} matches exactly n number of times
- re{n,m} matches at least n and at most m times
- [...] matches any single character inside the brackets
- [^...] matches any single character not inside the brackets
- a-z A-Z character ranges
- \d matches digits; equivalent to [0-9]
  - matches every character except newline
- (re) groups regular expressions and remembers the matched text

### Some "innocent" examples

Let's try two examples

(a\*)\*b [a?]{n}[a]{n}

### Some "innocent" examples

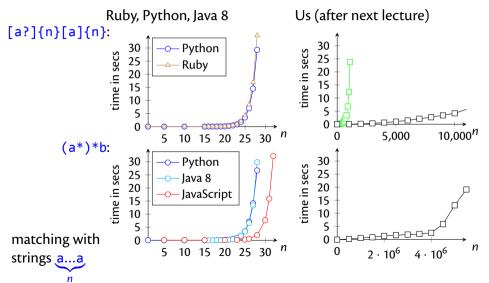
Let's try two examples

(a\*)\*b [a?]{n}[a]{n}

and match them with strings of the form

a, aa, aaa, aaaa, aaaaa, <u>a...a</u>

### Why Bother with Regexes?



### Incidents

• a global outage on 2 July 2019 at **Cloudflare** (first one for six years)

(?:(?:\"|'|\]|\}|\\|\d|(?:nan|infinity|true|false|
null|undefined|symbol|math)|\`|\-|\+)+[)]\*;?((?:\s
|-|~|!|{}|\|\||+)\*.\*(?:.\*=.\*)))



It serves more web traffic than Twitter, Amazon, Apple, Instagram, Bing & Wikipedia combined.

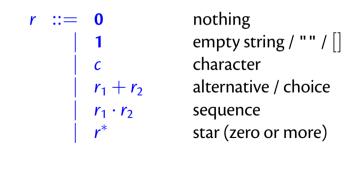
 on 20 July 2016 the Stack Exchange webpage went down because of an evil regular expression C

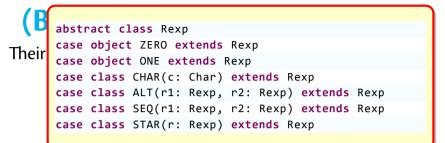
# **Evil Regular Expressions**

- Regular expression Denial of Service (ReDoS)
- Some evil regular expressions:
  - [a?]{n} [a]{n}
  - (a\*)\* b
  - ([a-z]+)\*
  - (a + aa)\*
  - (a + a?)\*
- sometimes also called catastrophic backtracking
- this is a problem for Network Intrusion Detection systems, Cloudflare, StackExchange, Atom editor
- https://vimeo.com/112065252

# (Basic) Regular Expressions

Their inductive definition:





r ::= 0nothing1empty string / "" / []ccharacter $r_1 + r_2$ alternative / choice $r_1 \cdot r_2$ sequence $r^*$ star (zero or more)



#### ... are lists of characters. For example "hello"

[h, e, l, l, o] or just hello

the empty string: [] or ""

the concatenation of two strings:

s<sub>1</sub>@s<sub>2</sub>

foo @ bar = foobar baz @ [] = baz

# Languages, Strings

- Strings are lists of characters, for example
  [], *abc* (Pattern match: *c*::s)
- A language is a set of strings, for example

 $\{[], hello, foobar, a, abc\}$ 

Concatenation of strings and languages
 foo @ bar = foobar
 A @ B <sup>def</sup> = {s<sub>1</sub> @ s<sub>2</sub> | s<sub>1</sub> ∈ A ∧ s<sub>2</sub> ∈ B}

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Let  

$$A = \{foo, bar\}$$
  
 $B = \{a, b\}$ 

 $A @ B = \{fooa, foob, bara, barb\}$ 

## **Two Corner Cases**

# $A @ \{[]\} = ?$

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## **Two Corner Cases**

# $A @ \{[]\} = ?$

 $A @ \{\} = ?$ 

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...all the strings a regular expression can match.

$$L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}$$

$$L(\mathbf{1}) \stackrel{\text{def}}{=} \{[]\}$$

$$L(c) \stackrel{\text{def}}{=} \{[c]\}$$

$$L(r_1 + r_2) \stackrel{\text{def}}{=} L(r_1) \cup L(r_2)$$

$$L(r_1 \cdot r_2) \stackrel{\text{def}}{=} L(r_1) @ L(r_2)$$

$$L(r^*) \stackrel{\text{def}}{=}$$

*L* is a function from regular expressions to sets of strings (languages):  $L : \text{Rexp} \Rightarrow \text{Set}[\text{String}]$ 

## **The Power Operation**

• The *n*th Power of a language:

$$\begin{array}{rcl} A^0 & \stackrel{\text{def}}{=} & \{[]\} \\ A^{n+1} & \stackrel{\text{def}}{=} & A @ A^n \end{array}$$

#### For example

$$A^{4} = A @ A @ A @ A @ A A^{1} = A A^{0} = \{[]\}$$

$$(@ \{[]\})$$

$$L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}$$

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$$L(r^*) \stackrel{\text{def}}{=} \bigcup_{0 \le n} L(r)^n$$

## **The Star Operation**

• The Kleene Star of a language:

$$\mathsf{A}\star\stackrel{\mathrm{\tiny def}}{=}\bigcup_{0\leq n}\mathsf{A}^n$$

This expands to

 $A^0 \cup A^1 \cup A^2 \cup A^3 \cup A^4 \cup \dots$ 

#### or

#### $\{[]\} \cup A \cup A@A \cup A@A@A \cup A@A@A@A \cup \dots$

$$L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}$$

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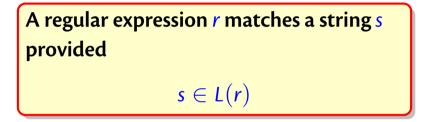
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$$L(r^*) \stackrel{\text{def}}{=} (L(r)) \star$$

# **The Meaning of Matching**



...and the point of the next lecture is to decide this problem as fast as possible (unlike Python, Ruby, Java)



• Say  $A = \{[a], [b], [c], [d]\}.$ 

How many strings are in  $A^4$ ?



• Say  $A = \{[a], [b], [c], [d]\}.$ 

How many strings are in  $A^4$ ?

What if  $A = \{[a], [b], [c], []\};$ how many strings are then in  $A^4$ ?

