Automata and Formal Languages (1)





Antikythera automaton, 100 BC (Archimedes?)

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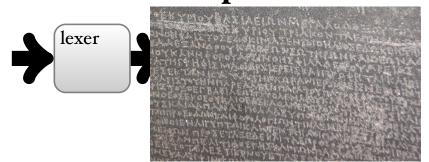
A Compiler



```
lexer input: a string
    "read(n);"
lexer output: a sequence of tokens
    key(read); lpar; id(n); rpar; semi
```



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```



lexing ⇒ recognising words (Stone of Rosetta)

parser input: a sequence of token
parser output: an abstract syntax tree

read

lpar
n
rpar



code generator:

istore 2
iload 2
ldc 10
isub
ifeq Label2
iload 2

Compiler



code generator: istore 2

iload 2

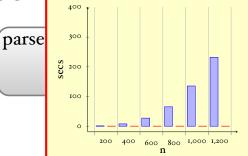
ldc 10 isub

ifea Lahe

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iload 2

. . .





The subject is quite old

- Turing Machines, 1936
- Regular Expressions, 1956
- The first compiler for COBOL, 1957 (Grace Hopper)
- But surprisingly research papers are still published nowadays



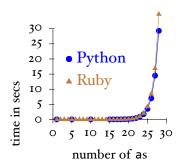
Grace Hopper

(she made it to David Letterman's Tonight Show,

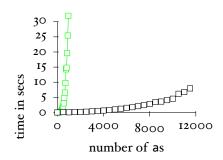
http://www.youtube.com/watch?v=aZOxtURhfEU)

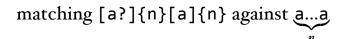
Why Bother?

Ruby, Python and Others



Us (after this course)





Lectures 1 - 6

transforming strings into structured data

Lexing

(recognising "words")

Parsing

(recognising "sentences")



Stone of Rosetta

Lectures 1 - 6

transforming strings into structured data

Lexing

baseed on regular expressions

(recognising "words")

Parsing

(recognising "sentences")



Stone of Rosetta

Familiar Regular Expr.

$$[a-z0-9..]+ @ [a-z0-9..]+ . [a-z.]{2,6}$$

```
re*
          matches o or more times
          matches I or more times
re+
re?
          matches o or I times
          matches exactly n number of times
re{n}
          matches at least n and at most m times
re{n,m}
[\ldots]
          matches any single character inside the brackets
          matches any single character not inside the
[^...]
          brackets
a-zA-Z
          character ranges
١d
          matches digits; equivalent to [0-9]
          matches every character except newline
(re)
          groups regular expressions and remembers the
          matched text
```

Today

• the ultimate goal is to implement a small compiler (a really small one for the JVM)

Let's start with:

- a web-crawler
- an email harvester
- a web-scraper

A Web-Crawler

- given an URL, read the corresponding webpage
- extract all links from it
- o call the web-crawler again for all these links

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(we need a bound for the number of recursive calls) (the purpose is to check all links on my own webpage)





Scala

A simple Scala function for reading webpages:

```
import io.Source

def get_page(url: String) : String = {
   Source.fromURL(url).take(10000).mkString
}
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get_page("""http://www.inf.kcl.ac.uk/staff/urbanc/""")
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import io.Source
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get page("""http://www.inf.kcl.ac.uk/staff/urbanc/""")
A slightly more complicated version for handling errors
properly:
def get page(url: String) : String = {
  Try(Source.fromURL(url).take(10000).mkString) getOrElse
    { println(s" Problem with: $url"); ""}
```

Linked in theguardian Morgan Stanley

CREDIT SUISSE

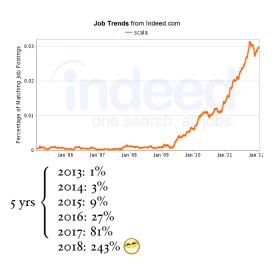


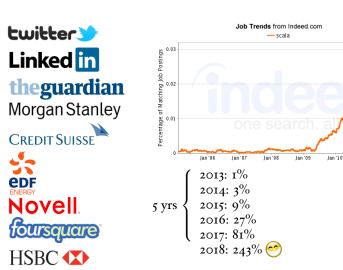
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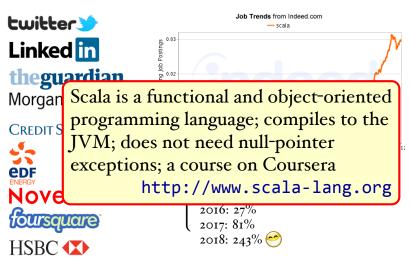




in London today: I Scala job for every 30 Java jobs; Scala programmers seem to get up to 20% better salary

Jan 11

Jan 17



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A Regular Expression

• ... is a pattern or template for specifying strings

```
"https?://[^"]*"
```

matches for example

```
"http://www.foobar.com"
"https://www.tls.org"
```

A Regular Expression

• ... is a pattern or template for specifying strings

```
""""https?://[^"]*""".r
```

matches for example

```
"http://www.foobar.com"
"https://www.tls.org"
```

Finding Operations

rexp.findAllIn(string)

returns a list of all (sub)strings that match the regular expression

rexp.findFirstIn(string)

returns either

- None if no (sub)string matches or
- Some(s) with the first (sub)string

```
val http pattern = """"https?://[^"]*"""".r
def unquote(s: String) = s.drop(1).dropRight(1)
def get all_URLs(page: String) : Set[String] =
  http pattern.findAllIn(page).map(unquote).toSet
def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else {
    println(s"Visiting: $n $url")
    for (u <- get_all_URLs(get_page(url))) crawl(u, n - 1)</pre>
crawl(some start URL, 2)
```

A version that only crawls links in "my" domain:

```
val my urls = """urbanc"".r
def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else if (my urls.findFirstIn(url) == None) {
    println(s"Visiting: $n $url")
    get page(url); ()
  else {
    println(s"Visiting: $n $url")
    for (u <- get_all_URLs(get_page(url))) crawl(u, n - 1)</pre>
```

A little email harvester:

```
val http pattern = """"https?://[^"]*""".r
val my urls = """urbanc""".r
val email pattern =
  """([a-z0-9 \ \ ]+)@([\ da-z\ \ ]+)\ ([a-z\ \ ]{2,6})""".r
def print str(s: String) =
  if (s == "") () else println(s)
def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else {
    println(s"Visiting: $n $url")
    val page = get page(url)
    print str(email pattern.findAllIn(page).mkString("\n"))
    for (u <- get all URLs(page).par) crawl(u, n - 1)</pre>
```

Regular Expressions

Their inductive definition:

```
r ::= \emptyset null
\begin{array}{ccc} & & & & & & \\ & \epsilon & & & & & \\ & c & & & & \\ & c & & & & \\ & r_1 \cdot r_2 & & & \\ & r_1 + r_2 & & & \\ & r^* & & & \\ & & & & \\ \end{array}
null
empty string / "" / []
c character
sequence
star(zero or more)
```

Regular Expressions

In Scala:

```
def OPT(r: Rexp) = ALT(r, EMPTY)

def NTIMES(r: Rexp, n: Int) : Rexp = n match {
   case 0 => EMPTY
   case 1 => r
   case n => SEQ(r, NTIMES(r, n - 1))
}
```

Strings

...are lists of characters. For example "hello"

the empty string: [] or ""

the concatenation of two strings:

$$s_1 @ s_2$$

$$egin{array}{lll} L(arnothing) & \stackrel{ ext{def}}{=} & arnothing \ L(\epsilon) & \stackrel{ ext{def}}{=} & \{[]\} \ L(oldsymbol{r}_1 + oldsymbol{r}_2) & \stackrel{ ext{def}}{=} & L(oldsymbol{r}_1) \cup L(oldsymbol{r}_2) \ L(oldsymbol{r}_1 \cdot oldsymbol{r}_2) & \stackrel{ ext{def}}{=} & \{s_1 @ s_2 \mid s_1 \in L(oldsymbol{r}_1) \wedge s_2 \in L(oldsymbol{r}_2)\} \ L(oldsymbol{r}^*) & \stackrel{ ext{def}}{=} & \{s_1 @ s_2 \mid s_1 \in L(oldsymbol{r}_1) \wedge s_2 \in L(oldsymbol{r}_2)\} \ \end{array}$$

$$egin{aligned} L(arnothing) & \stackrel{ ext{def}}{=} & arnothing \ L(archi) & \stackrel{ ext{def}}{=} & \{[]\} \ L(archi_1 + arrho_2) & \stackrel{ ext{def}}{=} & L(arrho_1) \cup L(arrho_2) \ L(arrho_1 \cdot arrho_2) & \stackrel{ ext{def}}{=} & \{s_1 @ s_2 \mid s_1 \in L(arrho_1) \wedge s_2 \in L(arrho_2)\} \ L(arrho^*) & \stackrel{ ext{def}}{=} & \{[]\} \ L(arrho)^{n+1} & \stackrel{ ext{def}}{=} & L(arrho) @ L(arrho)^n \end{aligned}$$

$$L(\varnothing) \stackrel{\mathrm{def}}{=} \varnothing$$
 $L(\epsilon) \stackrel{\mathrm{def}}{=} \{[]\}$
 $L(c) \stackrel{\mathrm{def}}{=} \{[c]\}$
 $L(r_1 + r_2) \stackrel{\mathrm{def}}{=} L(r_1) \cup L(r_2)$
 $L(r_1 \cdot r_2) \stackrel{\mathrm{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}$
 $L(r^*) \stackrel{\mathrm{def}}{=} \{[]\}$
 $L(r)^{n+1} \stackrel{\mathrm{def}}{=} L(r) @ L(r)^n \quad \text{(append on sets)}$
 $\{s_1 @ s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}$

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 $L(r^*) \stackrel{\mathrm{def}}{=} \bigcup_{n \geq 0} L(r)^n$
 $L(r)^{\circ} \stackrel{\mathrm{def}}{=} \{[]\}$
 $L(r)^{n+1} \stackrel{\mathrm{def}}{=} L(r) @ L(r)^n \text{ (append on sets)}$
 $\{s_1 @ s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}$

The Meaning of Matching

A regular expression *r* matches a string *s* provided

$$s \in L(r)$$

Written Exam

- Accounts for 75%.
- You will understand the question "Is this relevant for the exam?" is very demotivating for the lecturer!
- Deal: Whatever is in the homework (and is not marked "optional") is relevant for the exam.

Coursework

• Accounts for 25%. Two strands. Choose one!

Strand 1

- four programming subtasks:
 - matcher (5%, 13.10.)
 - lexer (5%, 03.11.)
 - parser (5%, 27.11.)
 - compiler (10%, 12.12.)

Strand 2

- one task: prove the correctness of a regular expression matcher in the Isabelle theorem prover
- 25%, submission 12.12.
- Solving more than one strand will **not** give you more marks.
- The exam will contain in much, much smaller form elements from both (but will also be in lectures and HW).

Questions?