Compilers and Formal Languages (1)

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Why Study Compilers?

John Regehr (Univ. Utah, LLVM compiler hacker)

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 Hardware is getting weirder rather than getting clocked faster.

"Almost all processors are multicores nowadays and it looks like there is increasing asymmetry in resources across cores. Processors come with vector units, crypto accelerators etc. We have DSPs, GPUs, ARM big.little, and Xeon Phi. This is only scratching the surface."

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 We're getting tired of low-level languages and their associated security disasters.

> "We want to write new code, to whatever extent possible, in safer, higher-level languages. Compilers are caught right in the middle of these opposing trends: one of their main jobs is to help bridge the large and growing gap between increasingly high-level languages and increasingly wacky platforms."

What are Compilers?

```
guare(int):
                                                                                   push
                                                                                           rbp
                                                                                           rbp, rsp
                                                                                           DWORD PTR [rbp-4], edi
                                                                                           eax, DWORD PTR [rbp-4]
    // Type your code here, or load an example.
                                                                                   and
                                                                                           eax. 1
2 = int square(int num) {
                                                                                           eax. eax
        if (num % 2 == 0)
                                                                                           . T.2
          { return num + num; }
                                                                                           eax, DWORD PTR [rbp-4]
5 -
        else
                                                                     10
                                                                                   add
                                                                                           eax, eax
          { return num * num: }
                                                                                           .L3
                                                                     12 F .L2:
                                                                     13
                                                                                   mov
                                                                                           eax, DWORD PTR [rbp-4]
                                                                                   imul
                                                                                           eax. eax
                                                                    15 E .L3:
                                                                                   pop
                                                                                           rbp
                                                                                   ret
```

"source" ------ "binary"

Compiler explorers, e.g.: https://gcc.godbolt.org

Why Bother? Compilers & Boeings 777

First flight in 1994. They want to achieve triple redundancy in hardware faults.

They compile 1 Ada program to

- Intel 80486
- Motorola 68040 (old Macintosh's)
- AMD 29050 (RISC chips used often in laser printers)
 using 3 independent compilers.

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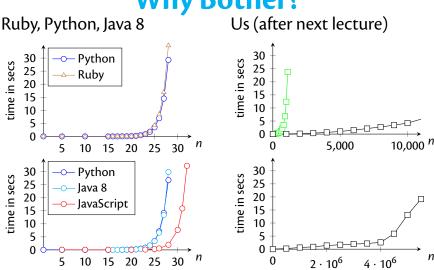
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using 3 independent compilers.

Airbus uses C and static analysers. Recently started using CompCert.

Why Bother?



matching $[a?]{n}[a]{n}$ and (a*)*b against a...a

Incidents

 a global outage on 2 July 2019 at Cloudflare (first one for six years)

```
(?:(?:\"|'|\]|\\|\d|(?:nan|infinity|true|false|
null|undefined|symbol|math)|\`|\-|\+)+[)]*;?((?:\s
|-|~|!|{}|\\||\+)*.*(?:.*=.*)))
```



It serves more web traffic than Twitter, Amazon, Apple, Instagram, Bing & Wikipedia combined.

 on 20 July 2016 the Stack Exchange webpage went down because of an evil regular expression

Evil Regular Expressions

- Regular expression Denial of Service (ReDoS)
- Evil regular expressions
 - $(a^{?\{n\}}) \cdot a^{\{n\}}$
 - $(a^*)^* \cdot b$
 - $([a-z]^+)^*$
 - $(a + a \cdot a)^*$
 - $(a + a^{?})^{*}$
- sometimes also called catastrophic backtracking
- this is a problem for Network Intrusion Detection systems, Cloudflare, StackExchange, Atom editor
- https://vimeo.com/112065252



lexer input: a string "read(n);" lexer output: a sequence of tokens key(read) lpar id(n) rpar semi binary code program lexer code gen parser

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program

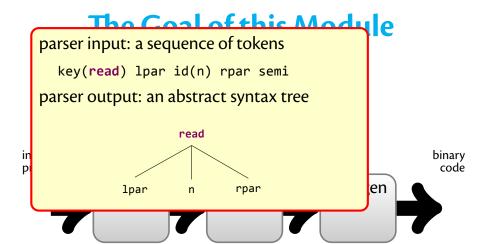
lexer

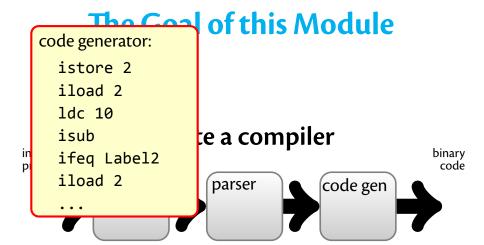
lexing \Rightarrow recognising words (Stone of Rosetta)

lexer input: a string
 "read(n);"
lexer output: a sequence of tokens

key(read) lpar id(n) rpar semi binary codeprogram lexer if \Rightarrow keyword $iffoo \Rightarrow identifier$

lexing \Rightarrow recognising words (Stone of Rosetta)





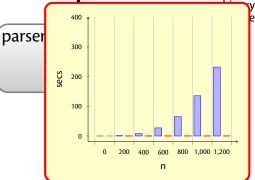
code generator:

istore 2 iload 2 ldc 10

isub

ifeq Label2
iload 2

te a compiler



The Acad. Subject is Mature

- Turing Machines, 1936 (a tape as memory)
- Regular Expressions, 1956
- The first compiler for COBOL, 1957 (Grace Hopper)
- But surprisingly research papers are still published nowadays
- "Parsing: The Solved Problem That Isn't"



Grace Hopper

(she made it to David Letterman's Tonight Show, https://youtu.be/3N ywhx6 K0?t=31)

Remember BF* from PEP?**

```
> ⇒ move one cell right
\leftrightarrow move one cell left
+ \Rightarrow increase cell by one
\rightarrow decrease cell by one
. ⇒ print current cell
\Rightarrow input current cell
 \Rightarrow loop begin
1 \Rightarrow loop end
   ⇒ everything else is a comment
```

A "Compiler" for BF***

```
\Rightarrow ptr++
\leftrightarrow ptr--
+ \Rightarrow (*ptr)++
- ⇒ (*ptr)--
. ⇒ putchar(*ptr)
\Rightarrow *ptr = getchar()
\Rightarrow while(*ptr){
1 \Rightarrow 1
   \Rightarrow ignore everything else
```

```
char field[30000]
char *ptr = field[15000]
```

Lectures 1 - 5

transforming strings into structured data

Lexing

based on regular expressions

(recognising "words")

Parsing

(recognising "sentences")



Stone of Rosetta

Lectures 5 - 10

code generation for a small imperative and a small functional languages

Interpreters

(directly runs a program)

Compilers

(generates JVM code)



Familiar Regular Expr.

$$[a-z0-9_\.-]+ @ [a-z0-9\.-]+ . [a-z\.]{2,6}$$

```
matches 0 or more times
re*
           matches 1 or more times
re+
re?
           matches 0 or 1 times
re{n}
           matches exactly n number of times
           matches at least n and at most m times
re{n,m}
[\ldots]
           matches any single character inside the brackets
[^...]
           matches any single character not inside the brackets
a-z A-Z
           character ranges
           matches digits; equivalent to [0-9]
\d
           matches every character except newline
           groups regular expressions and remembers the
(re)
           matched text
```

A Regular Expression

• ... is a pattern or template for specifying strings

```
"https?://[^"]*"
```

matches for example

```
"http://www.foobar.com"
"https://www.tls.org"
```

but not

```
"http://www."foo"bar.com"
```

A Regular Expression

... is a pattern or template for specifying strings

```
""""https?://[^"]*""".r
```

matches for example

```
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"http://www."foo"bar.com"
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Regular Expressions

Their inductive definition:

```
r ::= 0nothing| 1empty string / "" / []| ccharacter| r_1 + r_2alternative / choice| r_1 \cdot r_2sequence| r^*star (zero or more)
```

abstract class Rexp
case object ZERO extends Rexp
case object ONE extends Rexp
case class CHAR(c: Char) extends Rexp
case class ALT(r1: Rexp, r2: Rexp) extends Rexp
case class SEQ(r1: Rexp, r2: Rexp) extends Rexp
case class STAR(r: Rexp) extends Rexp

r ::= 0nothing1empty string / "" / []ccharacter $r_1 + r_2$ alternative / choice $r_1 \cdot r_2$ sequence r^* star (zero or more)

Strings

...are lists of characters. For example "hello"

the empty string: or ""

the concatenation of two strings:

$$s_1 @ s_2$$

$$foo @ bar = foobar$$

 $baz @ [] = baz$

Languages, Strings

Strings are lists of characters, for example[], abc (Pattern match: c::s)

• A language is a set of strings, for example

Concatenation of strings and languages

foo @ bar = foobar
$$A @ B \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in A \land s_2 \in B\}$$

```
L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}
L(\mathbf{1}) \stackrel{\text{def}}{=} \{[]\}
L(c) \stackrel{\text{def}}{=} \{[c]\}
L(r_1 + r_2) \stackrel{\text{def}}{=} L(r_1) \cup L(r_2)
L(r_1 \cdot r_2) \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}
L(r^*) \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}
```

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$$L(r)^{n+1} \stackrel{\text{def}}{=} L(r) @ L(r)^n$$

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$$L(r)^0 \stackrel{\text{def}}{=} \{[]\}$$

$$L(r)^{n+1} \stackrel{\text{def}}{=} L(r) @ L(r)^n \text{ (append on sets)}$$

$$\{s_1 @ s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}$$

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$$L(r^*) \stackrel{\text{def}}{=} \bigcup_{0 \le n} L(r)^n$$

$$L(r)^0 \stackrel{\text{def}}{=} \{[]\}$$

$$L(r)^{n+1} \stackrel{\text{def}}{=} L(r) @ L(r)^n \quad \text{(append on sets)}$$

$$\{s_1 @ s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}$$

The Meaning of Matching

A regular expression *r* matches a string *s* provided

$$s \in L(r)$$

...and the point of the next lecture is to decide this problem as fast as possible (unlike Python, Ruby, Java)

The Power Operation

• The *n*th Power of a language:

$$A^{0} \stackrel{\text{def}}{=} \{[]\}$$

$$A^{n+1} \stackrel{\text{def}}{=} A @ A^{n}$$

For example

$$A^4 = A@A@A@A$$
 (@ {[]})
 $A^1 = A$ (@ {[]})
 $A^0 = \{[]\}$

Questions

• Say $A = \{[a], [b], [c], [d]\}.$

How many strings are in A^4 ?

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• Say $A = \{[a], [b], [c], [d]\}.$

How many strings are in A^4 ?

What if $A = \{[a], [b], [c], []\};$ how many strings are then in A^4 ?

The Star Operation

• The Kleene Star of a language:

$$A\star \stackrel{\text{def}}{=} \bigcup_{0 \le n} A^n$$

This expands to

$$A^0 \cup A^1 \cup A^2 \cup A^3 \cup A^4 \cup \dots$$

or

$$\{[]\} \cup A \cup A@A \cup A@A@A \cup A@A@A@A \cup \dots$$

Written Exam

- Accounts for 80%.
- The question "Is this relevant for the exam?" is very demotivating for the lecturer!
- Deal: Whatever is in the homework (and is not marked "optional") is relevant for the exam.
- Each lecture has also a handout. There are also handouts about notation and Scala.

Coursework

• Accounts for 20%. Two strands. Choose one!

Strand 1

- 4 programming tasks:
 - matcher (4%, 11.10.)
 - lexer (5%, 04.11.)
 - parser (5%, 22.11.)
 - compiler (6%, 13.12.)
- in any lang. you like, but I want to see the code

Strand 2

- one task: prove the correctness of a regular expression matcher in the <u>Isabelle</u> theorem prover
- 20%, submission on 13.12.

Solving more than one strand will not give you more marks.

Lecture Capture

• Hope it works...

Lecture Capture

• Hope it works...actually no, it does not!

Lecture Capture

- Hope it works...actually no, it does not!
- It is important to use lecture capture wisely (it is only the "baseline"):
 - Lecture recordings are a study and revision aid.
 - Statistically, there is a clear and direct link between attendance and attainment: students who do not attend lectures, do less well in exams.
- Attending a lecture is more than watching it online if you do not attend, you miss out!

Questions?