

# Compilers and Formal Languages (I)



Antikythera automaton, 100 BC (Archimedes?)

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Slides: KEATS

# The Goal of this Course

## Write A Compiler



# The Goal of this Course

lexer input: a string

```
"read(n);"
```

lexer output: a sequence of tokens

```
key(read); lpar; id(n); rpar; semi
```



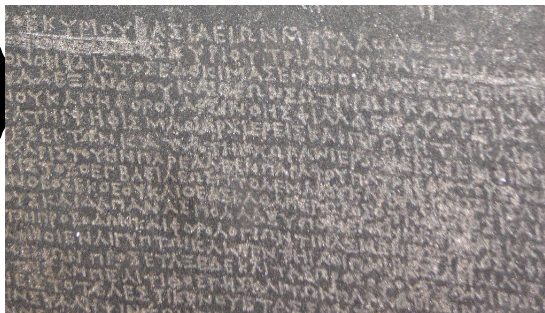
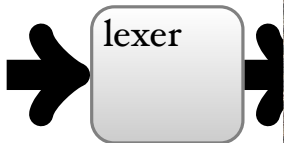
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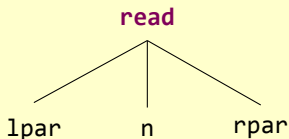


lexing  $\Rightarrow$  recognising words (Stone of Rosetta)

# The Goal of this Course

parser input: a sequence of token

parser output: an abstract syntax tree

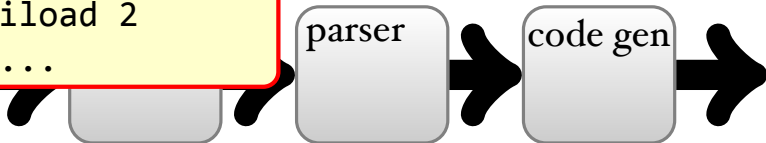


# The Goal of this Course

code generator:

```
istore 2  
iload 2  
ldc 10  
isub  
ifeq Label2  
iload 2  
...
```

## Building A Compiler



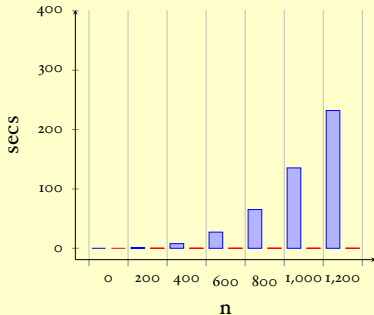
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```

## Building A Compiler

parse



# The subject is quite old

- Turing Machines, 1936
- Regular Expressions, 1956
- The first compiler for COBOL, 1957  
(Grace Hopper)
- But surprisingly research papers are still published nowadays



Grace Hopper

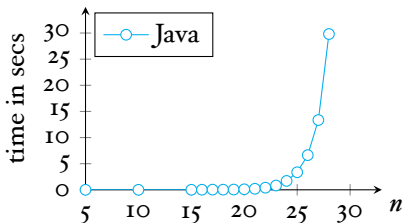
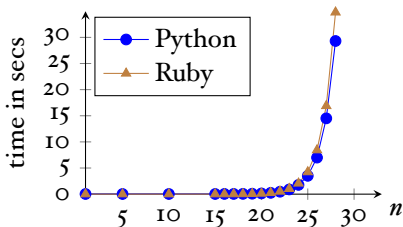
(she made it to David Letterman's Tonight Show,

<http://www.youtube.com/watch?v=aZ0xtURhfEU>)

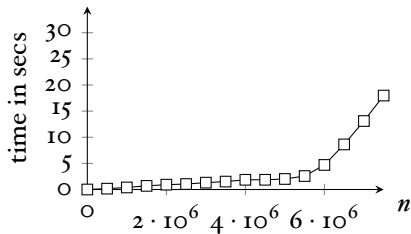
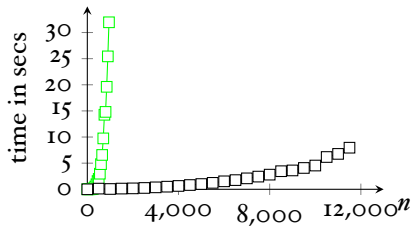


# Why Bother?

Ruby, Python, Java



Us (after next lecture)



matching  $[a?]\{n\}[a]\{n\}$  and  $[a^*]*b$  against  $\underbrace{a\dots a}_n$

# Lectures 1 - 5

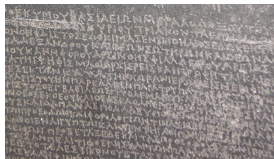
transforming strings into structured data

## Lexing

(recognising “words”)

## Parsing

(recognising “sentences”)



Stone of Rosetta

# Lectures 1 - 5

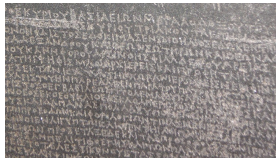
transforming strings into structured data

**Lexing** based on regular expressions

(recognising “words”)

**Parsing**

(recognising “sentences”)



Stone of Rosetta

# Familiar Regular Expr.

`[a-zA-Z0-9_.-]+ @ [a-zA-Z0-9.-]+ . [a-zA-Z.]{2,6}`

<code>re*</code>	matches 0 or more times
<code>re+</code>	matches 1 or more times
<code>re?</code>	matches 0 or 1 times
<code>re{n}</code>	matches exactly n number of times
<code>re{n,m}</code>	matches at least n and at most m times
<code>[...]</code>	matches any single character inside the brackets
<code>[^...]</code>	matches any single character not inside the brackets
<code>a-zA-Z</code>	character ranges
<code>\d</code>	matches digits; equivalent to <code>[0-9]</code>
<code>.</code>	matches every character except newline
<code>(re)</code>	groups regular expressions and remembers the matched text

# Today

- While the ultimate goal is to implement a small compiler (a really small one for the JVM)...

Let's start with:

- a web-crawler
- an email harvester
- (a web-scraper)

# A Web-Crawler

- 1 given an URL, read the corresponding webpage
- 2 extract all links from it
- 3 call the web-crawler again for all these links

# A Web-Crawler

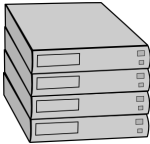
- ➊ given an URL, read the corresponding webpage
- ➋ if not possible print, out a problem
- ➌ if possible, extract all links from it
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# A Web-Crawler

- 1 given an URL, read the corresponding webpage
- 2 if not possible print, out a problem
- 3 if possible, extract all links from it
- 4 call the web-crawler again for all these links

(we need a bound for the number of recursive calls)  
(the purpose is to check all links on my own webpage)





Server

GET request



webpage



POST data



Browser

# Scala

A simple Scala function for reading webpages:

```
import io.Source

def get_page(url: String) : String = {
  Source.fromURL(url).take(10000).mkString
}
```

# Scala

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import io.Source

def get_page(url: String) : String = {
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get_page("""http://www.inf.kcl.ac.uk/staff/urbanc/""")
```

# Scala

A simple Scala function for reading webpages:

```
import io.Source

def get_page(url: String) : String = {
  Source.fromURL(url).take(10000).mkString
}

get_page("""http://www.inf.kcl.ac.uk/staff/urbanc/""")
```

A slightly more complicated version for handling errors:

```
def get_page(url: String) : String = {
  Try(Source.fromURL(url).take(10000).mkString).
    getOrElse { println(s" Problem with: $url"); ""}
}
```

# Why Scala?

twitter 

Linked 

theguardian

Morgan Stanley

CREDIT SUISSE 



edf  
ENERGY

Novell.

foursquare™

HSBC 

...

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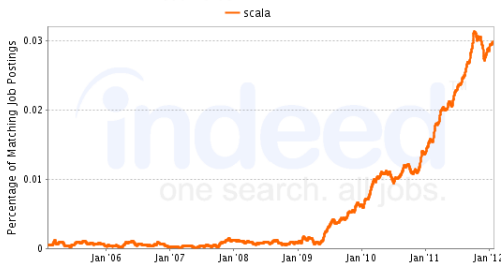
Novell

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HSBC 

...

Job Trends from Indeed.com



5 yrs {  
2013: 1%  
2014: 3%  
2015: 9%  
2016: 27%  
2017: 81%  
2018: 243% 😊

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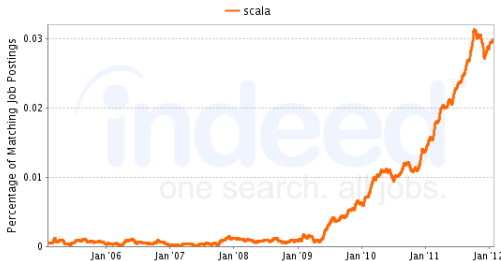
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**in London today:** 1 Scala job for every 30 Java jobs;  
Scala programmers seem to get up to 20% better salary



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Job Trends from Indeed.com



Scala is a functional and object-oriented programming language; compiles to the JVM; does not need null-pointer exceptions; a course on Coursera

<http://www.scala-lang.org>

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**in London today:** 1 Scala job for every 30 Java jobs;  
Scala programmers seem to get up to 20% better salary

# A Regular Expression

- ... is a pattern or template for specifying strings

```
"https?://[^\"]*"
```

matches for example

```
"http://www.foobar.com"
```

```
"https://www.tls.org"
```

# A Regular Expression

- ... is a pattern or template for specifying strings

```
""""https?://[^\"]*"""".r
```

matches for example

```
”http://www.foobar.com”
```

```
”https://www.tls.org”
```

# Finding Operations

**rexp.findAllIn(string)**

returns a list of all (sub)strings that match the regular expression

**rexp.findFirstIn(string)**

returns either

- None if no (sub)string matches or
- Some(s) with the first (sub)string

```

val http_pattern = """https?://[^\"]*""".r

def unquote(s: String) = s.drop(1).dropRight(1)

def get_all_URLs(page: String) : Set[String] =
  http_pattern.findAllIn(page).map(unquote).toSet

def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else {
    println(s"Visiting: $n $url")
    for (u <- get_all_URLs(get_page(url))) crawl(u, n - 1)
  }
}

crawl(some_start_URL, 2)

```

A version that only crawls links in “my” domain:

```
val my_urls = """urbanc""".r

def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else if (my_urls.findFirstIn(url) == None) {
    println(s"Visiting: $n $url")
    get_page(url); ()
  }
  else {
    println(s"Visiting: $n $url")
    for (u <- get_all_URLs(get_page(url))) crawl(u, n - 1)
  }
}
```

## A little email harvester:

```
val http_pattern = """https?://[^\"]*""".r
val email_pattern =
  """([a-z0-9_\.-]+)@([\da-z\.-]+)\.([a-z\.]{2,6})""".r

def print_str(s: String) =
  if (s == "") () else println(s)

def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else {
    println(s"Visiting: $n $url")
    val page = get_page(url)
    print_str(email_pattern.findAllIn(page).mkString("\n"))
    for (u <- get_all_URLs(page).par) crawl(u, n - 1)
  }
}
```

<http://net.tutsplus.com/tutorials/other/8-regular-expressions-you-should-know/>

# Regular Expressions

Their inductive definition:

$r ::=$	<b>0</b>	null
	<b>1</b>	empty string / "" / []
	$c$	character
	$r_1 + r_2$	alternative / choice
	$r_1 \cdot r_2$	sequence
	$r^*$	star (zero or more)



Th

```
abstract class Rexp
case object ZERO extends Rexp
case object ONE extends Rexp
case class CHAR(c: Char) extends Rexp
case class ALT(r1: Rexp, r2: Rexp) extends Rexp
case class SEQ(r1: Rexp, r2: Rexp) extends Rexp
case class STAR(r: Rexp) extends Rexp
```

$r ::= \mathbf{0}$	null
$\mathbf{I}$	empty string / "" / []
$c$	character
$r_1 + r_2$	alternative / choice
$r_1 \cdot r_2$	sequence
$r^*$	star (zero or more)

# Regular Expressions

In Scala:

```
def OPT(r: Rexp) = ALT(r, ONE)
```

```
def NTIMES(r: Rexp, n: Int) : Rexp = n match {  
  case 0 => ONE  
  case 1 => r  
  case n => SEQ(r, NTIMES(r, n - 1))  
}
```

# Strings

...are lists of characters. For example "hello"

$[h, e, l, l, o]$  or just *hello*

the empty string:  $[]$  or ""

the concatenation of two strings:

$s_1 @ s_2$

$foo @ bar = foobar, baz @ [] = baz$

# Languages, Strings

- **Strings** are lists of characters, for example

$[], abc$  (Pattern match:  $c::s$ )

- A **language** is a set of strings, for example

$\{[], bello, foobar, a, abc\}$

- **Concatenation** of strings and languages

$foo @ bar = foobar$

$A @ B \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in A \wedge s_2 \in B\}$

# The Meaning of a Regular Expression

$$L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}$$

$$L(\mathbf{I}) \stackrel{\text{def}}{=} \{\emptyset\}$$

$$L(c) \stackrel{\text{def}}{=} \{[c]\}$$

$$L(r_1 + r_2) \stackrel{\text{def}}{=} L(r_1) \cup L(r_2)$$

$$L(r_1 \cdot r_2) \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \wedge s_2 \in L(r_2)\}$$

$$L(r^*) \stackrel{\text{def}}{=} \{s_1 @ s_2 @ s_3 @ \dots @ s_n \mid s_i \in L(r)\}$$

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# The Meaning of Matching

A regular expression  $r$  matches a string  $s$  provided

$$s \in L(r)$$

...and the point of the next lecture is to decide this problem as fast as possible (unlike Python, Ruby, Java)

# Written Exam

- Accounts for 80%.
- You will understand the question “*Is this relevant for the exam?*” is very demotivating for the lecturer!
- Deal: Whatever is in the homework (and is not marked “*optional*”) is relevant for the exam.
- Each lecture has also a handout. There are also handouts about notation and Scala.

# Coursework

- Accounts for 20%. Two strands. Choose **one!**

## Strand 1

- four programming tasks:
  - matcher (4%, 20.10.)
  - lexer (5%, 03.11.)
  - parser (5%, 24.11.)
  - compiler (6%, 13.12.)

## Strand 2

- one task: prove the correctness of a regular expression matcher in the Isabelle theorem prover
- 20%, submission 13.12.

- Solving more than one strand will **not** give you more marks.
- The exam will contain in much, much smaller form elements from both (but will also be in lectures and HW).

**Questions?**