

## Homework 4

1. Why is every finite set of strings a regular language?
2. What is the language recognised by the regular expressions  $(\emptyset^*)^*$ .
3. If a regular expression  $r$  does not contain any occurrence of  $\emptyset$  is it possible for  $L(r)$  to be empty?
4. Assume that  $s^{-1}$  stands for the operation of reversing a string  $s$ . Given the following *reversing* function on regular expressions

$$\begin{aligned} rev(\emptyset) &\stackrel{\text{def}}{=} \emptyset \\ rev(\epsilon) &\stackrel{\text{def}}{=} \epsilon \\ rev(c) &\stackrel{\text{def}}{=} c \\ rev(r_1 + r_2) &\stackrel{\text{def}}{=} rev(r_1) + rev(r_2) \\ rev(r_1 \cdot r_2) &\stackrel{\text{def}}{=} rev(r_2) \cdot rev(r_1) \\ rev(r^*) &\stackrel{\text{def}}{=} rev(r)^* \end{aligned}$$

and the set

$$Rev A \stackrel{\text{def}}{=} \{s^{-1} \mid s \in A\}$$

prove whether

$$L(rev(r)) = Rev(L(r))$$

holds.

5. Give a regular expression over the alphabet  $\{a, b\}$  recognising all strings that do not contain any substring  $bb$  and end in  $a$ .
6. Assume the delimiters for comments are  $/*$  and  $*/$ . Give a regular expression that can recognise comments of the form

$$/* \dots */$$

where the three dots stand for arbitrary characters, but not comment delimiters. (Hint: You can assume you are already given a regular expression written ALL, that can recognise any character, and a regular expression NOT that recognises the complement of a regular expression.)

7. Given the alphabet  $\{a, b\}$ . Draw the automaton that has two states, say  $q_0$  and  $q_1$ . The starting state is  $q_0$  and the final state is  $q_1$ . The transition function is given by

$$\begin{aligned} (q_0, a) &\rightarrow q_0 \\ (q_0, b) &\rightarrow q_1 \\ (q_1, b) &\rightarrow q_1 \end{aligned}$$

What is the languages recognised by this automaton?

8. Give a non-deterministic finite automaton that can recognise the language  $L(a \cdot (a + b)^* \cdot c)$ .
9. Given the following deterministic finite automaton over the alphabet  $\{0, 1\}$ , find the corresponding minimal automaton. In case states can be merged, state clearly which states can be merged.

