

Homework 7

1. Suppose the context-sensitive grammar

$$\begin{aligned} S &\rightarrow bSAA \mid \epsilon \\ A &\rightarrow a \\ bA &\rightarrow Ab \end{aligned}$$

where S is the starting symbol of the grammar. Give a derivation of the string "aaabaaabb". What can you say about the number of as and bs in the strings recognised by this grammar.

2. Consider the following grammar

$$\begin{aligned} S &\rightarrow N \cdot P \\ P &\rightarrow V \cdot N \\ N &\rightarrow N \cdot N \\ N &\rightarrow A \cdot N \\ N &\rightarrow \text{student} \mid \text{trainer} \mid \text{team} \mid \text{trains} \\ V &\rightarrow \text{trains} \mid \text{team} \\ A &\rightarrow \text{The} \mid \text{the} \end{aligned}$$

where S is the start symbol and S, P, N, V and A are non-terminals. Using the CYK-algorithm, check whether or not the following string can be parsed by the grammar:

The trainer trains the student team

3. Transform the grammar

$$\begin{aligned} A &\rightarrow 0A1 \mid BB \\ B &\rightarrow \epsilon \mid 2B \end{aligned}$$

into Chomsky normal form.