Homework 7

1. Suppose the context-sensitive grammar

$$\begin{array}{ccc} S & \rightarrow & bSAA \mid \epsilon \\ A & \rightarrow & a \\ bA & \rightarrow & Ab \end{array}$$

where S is the starting symbol of the grammar. Give a derivation of the string "aaabaaabb". What can you say about the number of as and bs in the strings recognised by this grammar.

2. Consider the following grammar

$$\begin{split} S &\to N \cdot P \\ P &\to V \cdot N \\ N &\to N \cdot N \\ N &\to A \cdot N \\ N &\to \text{student} \mid \text{trainer} \mid \text{team} \mid \text{trains} \\ V &\to \text{trains} \mid \text{team} \\ A &\to \text{The} \mid \text{the} \end{split}$$

where S is the start symbol and S, P, N, V and A are non-terminals. Using the CYK-algorithm, check whether or not the following string can be parsed by the grammar:

The trainer trains the student team

3. Transform the grammar

$$\begin{array}{ccc} A & \rightarrow & 0A1 \mid BB \\ B & \rightarrow & \epsilon \mid 2B \end{array}$$

into Chomsky normal form.