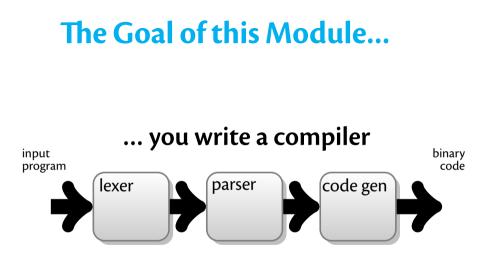
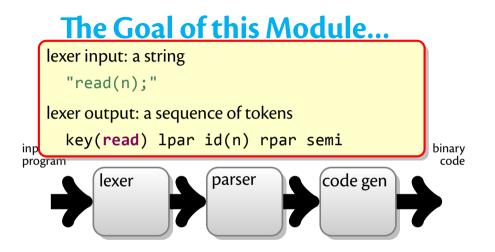
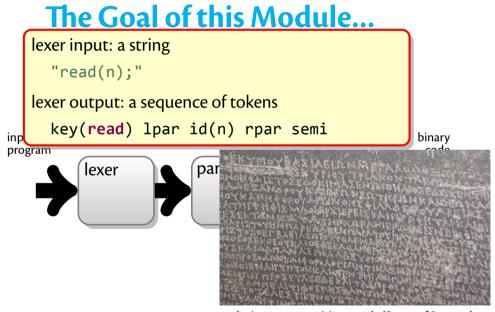
Compilers and Formal Languages

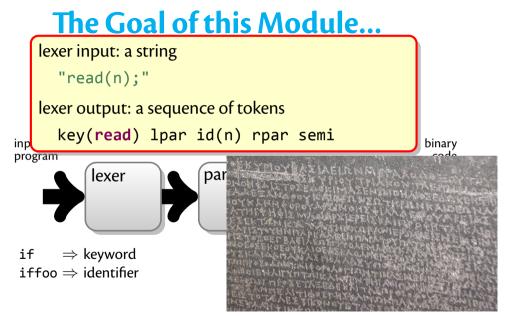
Email: christian.urban at kcl.ac.uk Slides & Progs: KEATS

1 Introduction, Languages	6 While-Language
2 Regular Expressions, Derivatives	7 Compilation, JVM
3 Automata, Regular Languages	8 Compiling Functional Languages
4 Lexing, Tokenising	9 Optimisations
5 Grammars, Parsing	10 LLVM

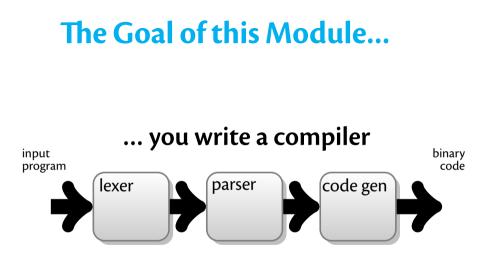


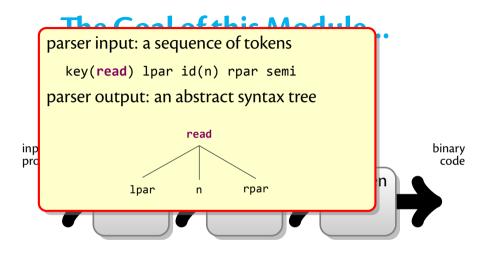


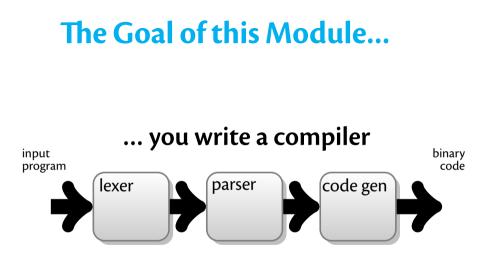


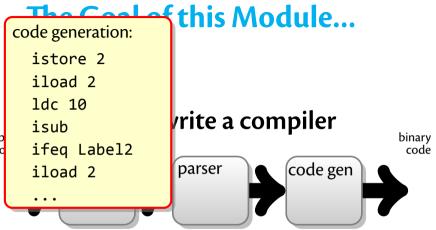


 $lexing \Rightarrow recognising words (Stone of Rosetta)_{I, King's College London - p. 2/29}$

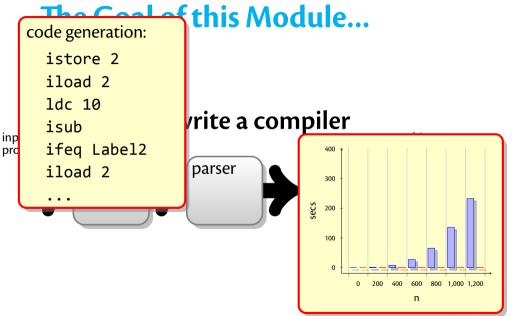






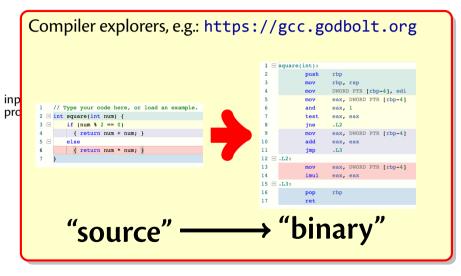


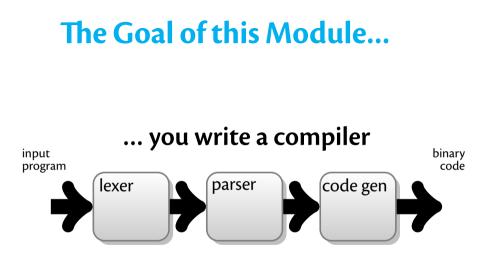
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The Goal of this Module...





Why Study Compilers?

John Regehr (Univ. Utah, LLVM compiler hacker) 🖒

"...It's effectively a perpetual employment act for solid compiler hackers."

Why Study Compilers?

John Regehr (Univ. Utah, LLVM compiler hacker) 🖒

"...It's effectively a perpetual employment act for solid compiler hackers."

• Hardware is getting weirder rather than getting clocked faster.

"Almost all processors are multicores nowadays and it looks like there is increasing asymmetry in resources across cores. Processors come with vector units, crypto accelerators etc. We have DSPs, GPUs, ARM big.little, and Xeon Phi. This is only scratching the surface."

Why Study Compilers?

John Regehr (Univ. Utah, LLVM compiler hacker) 🖒

"...It's effectively a perpetual employment act for solid compiler hackers."

• We're getting tired of low-level languages and their associated security disasters.

"We want to write new code, to whatever extent possible, in safer, higher-level languages. Compilers are caught right in the middle of these opposing trends: one of their main jobs is to help bridge the large and growing gap between increasingly high-level languages and increasingly wacky platforms."

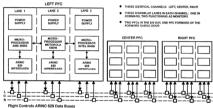
Why Bother with Compilers?

Boeing 777's: First flight in 1994. They want to achieve triple redundancy for potential hardware faults.

They compile 1 Ada program to

- Intel 80486
- Motorola 68040 (old Macintosh's)
- AMD 29050 (RISC chips used often in laser printers)

using 3 independent compilers.



Why Bother with Compilers?

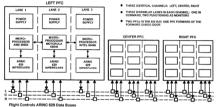
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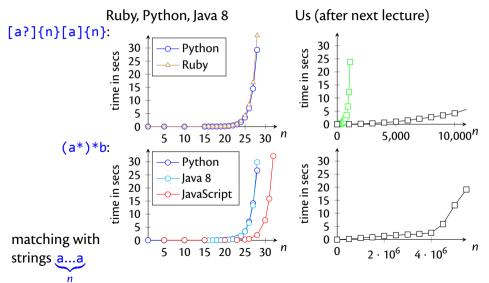
- Intel 80486
- Motorola 68040 (old Macintosh's)
- AMD 29050 (RISC chips used often in laser printers)

using 3 independent compilers.

Airbus uses C and static analysers. Recently started using CompCert.



Why Bother with Regexes?



Incidents

• a global outage on 2 July 2019 at **Cloudflare** (first one for six years)

(?:(?:\"|'|\]|\}|\\|\d|(?:nan|infinity|true|false|
null|undefined|symbol|math)|\`|\-|\+)+[)]*;?((?:\s
|-|~|!|{}|\|\||+)*.*(?:.*=.*)))



It serves more web traffic than Twitter, Amazon, Apple, Instagram, Bing & Wikipedia combined.

 on 20 July 2016 the Stack Exchange webpage went down because of an evil regular expression C

Evil Regular Expressions

- Regular expression Denial of Service (ReDoS)
- Some evil regular expressions:
 - [a?]{n} [a]{n}
 - (a*)* b
 - ([a-z]+)*
 - (a + aa)*
 - (a + a?)*
- sometimes also called catastrophic backtracking
- this is a problem for Network Intrusion Detection systems, Cloudflare, StackExchange, Atom editor
- https://vimeo.com/112065252

The Acad. Subject is Mature

- Turing Machines, 1936 (a tape as memory)
- Regular Expressions, 1956
- The first compiler for COBOL, 1957 (Grace Hopper)
- But surprisingly research papers are still published nowadays
- "Parsing: The Solved Problem That Isn't" 🖒



Grace Hopper (she made it to David Letterman's Tonight Show 🖒

What Do Compilers Do?

Remember BF*** from PEP?

- \rightarrow move one cell right
- + \Rightarrow increase cell by one
- \Rightarrow decrease cell by one
- . \Rightarrow print current cell
- , \Rightarrow input current cell
- $[\Rightarrow loop begin$
-] \Rightarrow loop end
 - \Rightarrow everything else is a comment

char field[30000] char *ptr = &field[15000]

- \Rightarrow ignore everything else
- $1 \Rightarrow \}$
- $\Rightarrow while(*ptr)$

$$\Rightarrow$$
 *ptr = getchar()

$$\rightarrow \Rightarrow (*ptr) - -$$

+
$$\Rightarrow$$
 (*ptr)++

 \rightarrow ptr++

<

$$\Rightarrow$$
 ptr--
 \Rightarrow (*ntr)++

$$\Rightarrow$$
 ptr--

A "Compiler" for BF*** to C

$$\Rightarrow$$
 (*ptr)++

$$\Rightarrow$$
 (*ptr)++

$$\rightarrow$$
 (*ptr)++

$$\Rightarrow$$
 (*ptr)++

$$\rightarrow$$
 (*ptr)++

Lectures 1 - 5

transforming strings into structured data

Lexing based on regular expressions (recognising "words")

Parsing

(recognising "sentences")



Stone of Rosetta

Lectures 5 - 10

code generation for a small imperative and a small functional language

Interpreters

(directly runs a program)

Compilers

(generate JVM code and LLVM-IR code)



Familiar Regular Expr.

[a-z0-9].-]+ @ [a-z0-9].-]+ . [a-z]{2,6}

- re* matches 0 or more times
- re+ matches 1 or more times
- re? matches 0 or 1 times
- re{n} matches exactly n number of times
- re{n,m} matches at least n and at most m times
- [...] matches any single character inside the brackets
- [^...] matches any single character not inside the brackets
- a-z A-Z character ranges
- \d matches digits; equivalent to [0-9]
 - matches every character except newline
- (re) groups regular expressions and remembers the matched text

A Regular Expression

• ... is a pattern or template for specifying strings

"https?://[^"]*"

matches for example

```
"http://www.foobar.com"
"https://www.tls.org"
```

but not

```
"http://www."foo"bar.com"
```

A Regular Expression

• ... is a pattern or template for specifying strings

""""https?://[^"]*""".r

matches for example

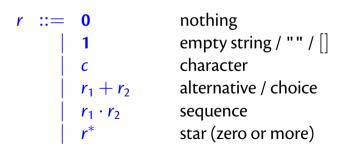
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```

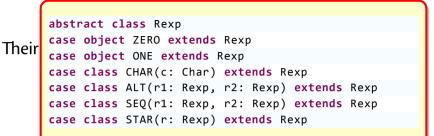
but not

```
"http://www."foo"bar.com"
```

Regular Expressions

Their inductive definition:





r ::= 0nothing1empty string / "" / []ccharacter $r_1 + r_2$ alternative / choice $r_1 \cdot r_2$ sequence r^* star (zero or more)



... are lists of characters. For example "hello"

[*h*, *e*, *l*, *l*, *o*] or just *hello*

the empty string: [] or ""

the concatenation of two strings:

s₁@s₂

foo @ bar = foobar baz @ [] = baz

Languages, Strings

- Strings are lists of characters, for example
 [], *abc* (Pattern match: *c*::s)
- A language is a set of strings, for example

 $\{[], hello, foobar, a, abc\}$

Concatenation of strings and languages
 foo @ bar = foobar
 A @ B ^{def} = {s₁ @ s₂ | s₁ ∈ A ∧ s₂ ∈ B}

$$L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}$$

$$L(\mathbf{1}) \stackrel{\text{def}}{=} \{[]\}$$

$$L(c) \stackrel{\text{def}}{=} \{[c]\}$$

$$L(r_1 + r_2) \stackrel{\text{def}}{=} L(r_1) \cup L(r_2)$$

$$L(r_1 \cdot r_2) \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}$$

$$L(r^*) \stackrel{\text{def}}{=}$$

$$L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}$$

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$$L(r^*) \stackrel{\text{def}}{=}$$

$$L(r)^0 \stackrel{\text{def}}{=} \{[]\}$$

$$L(r)^{n+1} \stackrel{\text{def}}{=} L(r) \circledast L(r)^n$$

$$\begin{array}{cccc} L(\mathbf{0}) & \stackrel{\text{def}}{=} & \{\} \\ L(\mathbf{1}) & \stackrel{\text{def}}{=} & \{[]\} \\ L(c) & \stackrel{\text{def}}{=} & \{[c]\} \\ L(r_1 + r_2) & \stackrel{\text{def}}{=} & L(r_1) \cup L(r_2) \\ L(r_1 \cdot r_2) & \stackrel{\text{def}}{=} & \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\} \\ L(r^*) & \stackrel{\text{def}}{=} \\ \end{array}$$

$$\begin{array}{c} L(r)^0 & \stackrel{\text{def}}{=} & \{[]\} \\ L(r)^{n+1} & \stackrel{\text{def}}{=} & L(r) @ L(r)^n & (\text{append on sets}) \\ & \{s_1 @ s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\} \end{array}$$

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$$L(0) \stackrel{\text{def}}{=} \{\}$$

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$$L(r_1 + r_2) \stackrel{\text{def}}{=} L(r_1) \cup L(r_2)$$

$$L(r_1 \cdot r_2) \stackrel{\text{def}}{=} \{s_1 \otimes s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}$$

$$L(r^*) \stackrel{\text{def}}{=} \bigcup_{0 \le n} L(r)^n$$

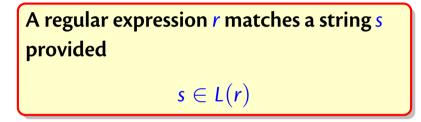
$$L(r)^0 \stackrel{\text{def}}{=} \{[]\}$$

$$L(r)^{n+1} \stackrel{\text{def}}{=} L(r) \otimes L(r)^n \quad \text{(append on sets)}$$

$$\{s_1 \otimes s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}$$

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The Meaning of Matching



...and the point of the next lecture is to decide this problem as fast as possible (unlike Python, Ruby, Java)

The Power Operation

• The *n*th Power of a language:

$$\begin{array}{rcl} A^0 & \stackrel{\text{def}}{=} & \{[]\} \\ A^{n+1} & \stackrel{\text{def}}{=} & A @ A^n \end{array}$$

For example

$$A^{4} = A @ A @ A @ A @ A A^{1} = A A^{0} = \{[]\}$$

$$(@ \{[]\}) (@ \{[]\})$$

$$(@ {[]})$$

 $(@ {[]})$



• Say $A = \{[a], [b], [c], [d]\}.$

How many strings are in A^4 ?



• Say $A = \{[a], [b], [c], [d]\}.$

How many strings are in A^4 ?

What if $A = \{[a], [b], [c], []\};$ how many strings are then in A^4 ?

Languages (Sets of Strings)

• A Language is a set of strings, for example

 $\{[], hello, foobar, a, abc\}$

• Concatenation for strings and languages

foo @ bar = foobar A @ B $\stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in A \land s_2 \in B\}$

For example $A = \{foo, bar\}, B = \{a, b\}$

 $A @ B = \{fooa, foob, bara, barb\}$

Two Corner Cases

$A @ \{[]\} = ?$

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Two Corner Cases

$A @ \{[]\} = ?$

 $A @ \{\} = ?$

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The Meaning of a Regex

...all the strings a regular expression can match.

$$L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}$$

$$L(\mathbf{1}) \stackrel{\text{def}}{=} \{[]\}$$

$$L(c) \stackrel{\text{def}}{=} \{[c]\}$$

$$L(r_1 + r_2) \stackrel{\text{def}}{=} L(r_1) \cup L(r_2)$$

$$L(r_1 \cdot r_2) \stackrel{\text{def}}{=} L(r_1) @ L(r_2)$$

$$L(r^*) \stackrel{\text{def}}{=}$$

L is a function from regular expressions to sets of strings (languages): $L : \text{Rexp} \Rightarrow \text{Set}[\text{String}]$

The Power Operation

• The *n*th Power of a language:

$$\begin{array}{rcl} A^0 & \stackrel{\text{def}}{=} & \{[]\} \\ A^{n+1} & \stackrel{\text{def}}{=} & A @ A^n \end{array}$$

For example

$$A^{4} = A @ A @ A @ A @ A A^{1} = A A^{0} = \{[]\}$$

$$(@ \{[]\})$$

The Star Operation

• The Kleene Star of a language:

$$\mathsf{A}\star\stackrel{\mathrm{\tiny def}}{=}\bigcup_{0\leq n}\mathsf{A}^n$$

This expands to

 $A^0 \cup A^1 \cup A^2 \cup A^3 \cup A^4 \cup \dots$

or

$\{[]\} \cup A \cup A@A \cup A@A@A \cup A@A@A@A \cup \dots$

Written Exam

- Accounts for 80%.
- The question "Is this relevant for the exam?" is very demotivating for the lecturer!
- Deal: Whatever is in the homework (and is not marked *"optional"*) is relevant for the exam.
- Each lecture has also a handout. There are also handouts about notation and Scala.

Coursework

• Accounts for 20%. Two strands. Choose one!

Strand 1

- 4 programming tasks:
 - matcher (4%, 11.10.)
 - lexer (5%, 04.11.)
 - parser (5%, 22.11.)
 - compiler (6%, 13.12.)
- in any lang. you like, but I want to see the code

Strand 2

• one task: prove the correctness of a regular expression matcher in the <u>Isabelle</u> theorem

prover

- 20%, submission on 13.12.
- Solving more than one strand will **not** give you more marks.

