# **Automata and Formal Languages (1)**





Antikythera automaton, 100 BC (Archimedes?)

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#### Write A Compiler



```
lexer input: a string
    "read(n);"
lexer output: a sequence of tokens
    key(read); lpar; id(n); rpar; semi
```



```
lexer input: a string
    "read(n);"
lexer output: a sequence of tokens
    key(read); lpar; id(n); rpar; semi
```



parser input: a sequence of token parser output: an abstract syntax tree read 1par rpar code gen lexer

#### code generator:

istore 2
iload 2
ldc 10
isub
ifeq Label2
iload 2

#### A Compiler



code generator:

istore 2 iload 2

ldc 10

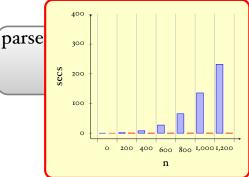
isub

ifeq Label2

iload 2

. . .

A Compiler



## The subject is quite old

- Turing Machines, 1936
- Regular Expressions, 1956
- The first compiler for COBOL, 1957 (Grace Hopper)
- But surprisingly research papers are still published nowadays



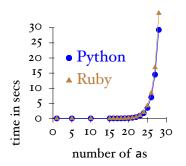
Grace Hopper

(she made it to David Letterman's Tonight Show,

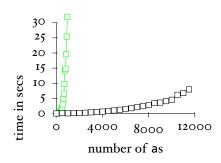
http://www.youtube.com/watch?v=aZOxtURhfEU)

## Why Bother?

# Ruby, Python and Others



#### Us (after next lecture)



### Lectures 1 - 5

transforming strings into structured data

# Lexing

(recognising "words")

## **Parsing**

(recognising "sentences")

Stone of Rosetta

### Lectures 1 - 5

transforming strings into structured data

# Lexing

based on regular expressions

(recognising "words")

## **Parsing**

Stone of Rosetta

(recognising "sentences")

# Familiar Regular Expr.

$$[a-z0-9..]+ @ [a-z0-9..]+ . [a-z.]{2,6}$$

re*	matches o or more times
re+	matches I or more times
re?	matches o or 1 times
re{n}	matches exactly n number of times
re{n,m}	matches at least n and at most m times
[]	matches any single character inside the brackets
[^]	matches any single character not inside the
	brackets
a-zA-Z	character ranges
\d	matches digits; equivalent to [0-9]
•	matches every character except newline
(re)	groups regular expressions and remembers the
	matched text

# **Today**

• While the ultimate goal is to implement a small compiler (a really small one for the JVM)...

#### Let's start with:

- a web-crawler
- an email harvester
- (a web-scraper)

#### A Web-Crawler

- ogiven an URL, read the corresponding webpage
- extract all links from it
- o call the web-crawler again for all these links

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(we need a bound for the number of recursive calls) (the purpose is to check all links on my own webpage)





#### Scala

A simple Scala function for reading webpages:

```
import io.Source

def get_page(url: String) : String = {
   Source.fromURL(url).take(10000).mkString
}
```

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get_page("""http://www.inf.kcl.ac.uk/staff/urbanc/""")
```

### Scala

A simple Scala function for reading webpages:

def get page(url: String) : String = {

import io.Source

```
Source.fromURL(url).take(10000).mkString
get page("""http://www.inf.kcl.ac.uk/staff/urbanc/""")
A slightly more complicated version for handling errors
properly:
def get page(url: String) : String = {
  Try(Source.fromURL(url).take(10000).mkString) getOrElse
    { println(s" Problem with: $url"); ""}
```

• • •

• • •

5 yrs 2013: 1% 2014: 3% 2015: 9% 2016: 27% 2017: 81% 2018: 243%

**in London today:** I Scala job for every 30 Java jobs; Scala programmers seem to get up to 20% better salary

Scala is a functional and object-oriented programming language; compiles to the JVM; does not need null-pointer exceptions; a course on Coursera <a href="http://www.scala-lang.org">http://www.scala-lang.org</a>

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# **A Regular Expression**

... is a pattern or template for specifying strings

```
"https?://[^"]*"
```

#### matches for example

```
"http://www.foobar.com"
"https://www.tls.org"
```

# **A Regular Expression**

... is a pattern or template for specifying strings

```
""""https?://[^"]*""".r
```

#### matches for example

```
"http://www.foobar.com"
"https://www.tls.org"
```

# **Finding Operations**

#### rexp.findAllIn(string)

returns a list of all (sub)strings that match the regular expression

#### rexp.findFirstIn(string)

returns either

- None if no (sub)string matches or
- Some(s) with the first (sub)string

```
val http pattern = """"https?://[^"]*""".r
def unquote(s: String) = s.drop(1).dropRight(1)
def get all URLs(page: String) : Set[String] =
  http pattern.findAllIn(page).map(unquote).toSet
def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else {
    println(s"Visiting: $n $url")
    for (u <- get_all_URLs(get_page(url))) crawl(u, n - 1)</pre>
crawl(some start URL, 2)
```

#### A version that only crawls links in "my" domain:

```
val my urls = """urbanc"".r
def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else if (my urls.findFirstIn(url) == None) {
    println(s"Visiting: $n $url")
    get page(url); ()
  else {
    println(s"Visiting: $n $url")
    for (u <- get_all_URLs(get_page(url))) crawl(u, n - 1)</pre>
```

#### A little email harvester:

```
val http pattern = """"https?://[^"]*""".r
val email pattern =
  """([a-z0-9 \ -]+)@([\da-z \ -]+) \ ([a-z \ ]{2,6})"".r
def print str(s: String) =
  if (s == "") () else println(s)
def crawl(url: String, n: Int) : Unit = {
  if (n == 0) ()
  else {
    println(s"Visiting: $n $url")
    val page = get page(url)
    print str(email pattern.findAllIn(page).mkString("\n"))
    for (u <- get all URLs(page).par) crawl(u, n - 1)</pre>
```

http://net.tutsplus.com/tutorials/other/8-regular-expressions-you-should-know/

# **Regular Expressions**

Their inductive definition:

$$r ::= \emptyset$$
 null
$$\begin{array}{ccc} & & & \text{null} \\ & & & \text{empty string } / \text{"" } / [] \\ & & c & & \text{character} \\ & & r_1 + r_2 & & \text{alternative } / \text{ choice} \\ & & r_1 \cdot r_2 & & \text{sequence} \\ & & r^* & & \text{star (zero or more)} \end{array}$$

```
abstract class Rexp
case object ZERO extends Rexp
case object ONE extends Rexp
case class CHAR(c: Char) extends Rexp
case class ALT(r1: Rexp, r2: Rexp) extends Rexp
case class SEQ(r1: Rexp, r2: Rexp) extends Rexp
case class STAR(r: Rexp) extends Rexp
```

```
r ::= \emptyset null
\epsilon empty string / "" / []
c character
r_1 + r_2 alternative / choice
r_1 \cdot r_2 sequence
r^* star (zero or more)
```

# **Regular Expressions**

In Scala:

```
def OPT(r: Rexp) = ALT(r, ONE)

def NTIMES(r: Rexp, n: Int) : Rexp = n match {
  case 0 => ONE
  case 1 => r
  case n => SEQ(r, NTIMES(r, n - 1))
}
```

# **Strings**

...are lists of characters. For example "hello"

$$[h, e, l, l, o]$$
 or just *hello*

the empty string: [] or ""

the concatenation of two strings:

$$s_1 @ s_2$$

# Languages, Strings

- **Strings** are lists of characters, for example [], *abc* (Pattern match: *c*::*s*)
- A language is a set of strings, for example

• Concatenation of strings and languages

$$foo @ bar = foobar$$

$$A @ B \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in A \land s_2 \in B\}$$

$$egin{array}{lll} L(arnothing) & \stackrel{ ext{def}}{=} & arnothing \ L(\epsilon) & \stackrel{ ext{def}}{=} & \{[]\} \ L(oldsymbol{r}_1 + oldsymbol{r}_2) & \stackrel{ ext{def}}{=} & L(oldsymbol{r}_1) \cup L(oldsymbol{r}_2) \ L(oldsymbol{r}_1 \cdot oldsymbol{r}_2) & \stackrel{ ext{def}}{=} & \{s_1 @ s_2 \mid s_1 \in L(oldsymbol{r}_1) \wedge s_2 \in L(oldsymbol{r}_2)\} \ L(oldsymbol{r}^*) & \stackrel{ ext{def}}{=} & \{s_1 @ s_2 \mid s_1 \in L(oldsymbol{r}_1) \wedge s_2 \in L(oldsymbol{r}_2)\} \ \end{array}$$

$$egin{aligned} L(arnothing)&\stackrel{ ext{def}}{=}&arnothing\ L(c)&\stackrel{ ext{def}}{=}&\{[]\}\ L(r_{ ext{i}}+r_{2})&\stackrel{ ext{def}}{=}&L(r_{ ext{i}})\cup L(r_{2})\ L(r_{ ext{i}}\cdot r_{2})&\stackrel{ ext{def}}{=}&\{s_{ ext{i}}@s_{2}\mid s_{ ext{i}}\in L(r_{ ext{i}})\wedge s_{2}\in L(r_{2})\}\ L(r^{*})&\stackrel{ ext{def}}{=}&\{[]\}\ L(r)^{n+ ext{i}}&\stackrel{ ext{def}}{=}&L(r)\,@L(r)^{n} \end{aligned}$$

$$L(\varnothing) \stackrel{\mathrm{def}}{=} \varnothing$$
 $L(\varepsilon) \stackrel{\mathrm{def}}{=} \{[]\}$ 
 $L(c) \stackrel{\mathrm{def}}{=} \{[c]\}$ 
 $L(r_1 + r_2) \stackrel{\mathrm{def}}{=} L(r_1) \cup L(r_2)$ 
 $L(r_1 \cdot r_2) \stackrel{\mathrm{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}$ 
 $L(r^*) \stackrel{\mathrm{def}}{=} \{[]\}$ 
 $L(r)^{n+1} \stackrel{\mathrm{def}}{=} L(r) @ L(r)^n \quad \text{(append on sets)}$ 
 $\{s_1 @ s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}$ 

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 $L(r_1 \cdot r_2) \stackrel{\mathrm{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}$ 
 $L(r^*) \stackrel{\mathrm{def}}{=} \bigcup_{n \geq 0} L(r)^n$ 
 $L(r)^{\circ} \stackrel{\mathrm{def}}{=} \{[]\}$ 
 $L(r)^{n+1} \stackrel{\mathrm{def}}{=} L(r) @ L(r)^n \text{ (append on sets)}$ 
 $\{s_1 @ s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}$ 

## The Meaning of Matching

A regular expression *r* matches a string *s* provided

$$s \in L(r)$$

...and the point of the next lecture is to decide this problem as fast as possible (unlike Python, Ruby)

#### **Written Exam**

- Accounts for 75%.
- You will understand the question "Is this relevant for the exam?" is very demotivating for the lecturer!
- Deal: Whatever is in the homework (and is not marked "optional") is relevant for the exam.
- Each lecture has also a handout. There are also handouts about notation and Scala.

#### Coursework

• Accounts for 25%. Two strands. Choose one!

#### Strand 1

- four programming subtasks:
  - matcher (5%, 16.10.)
  - lexer (5%, 06.11.)
  - parser (5%, 27.11.)
  - compiler (10%, 11.12.)

#### Strand 2

- one task: prove the correctness of a regular expression matcher in the Isabelle theorem prover
- 25%, submission 11.12.
- Solving more than one strand will **not** give you more marks.
- The exam will contain in much, much smaller form elements from both (but will also be in lectures and HW).

## **Questions?**