Handout 6 (Parser Combinators)

In what follows we explain *parser combinators*. Their distinguishing feature is that they are very easy to implement. However, they only work when the grammar to be parsed is *not* left-recursive and they are efficient only when the grammar is unambiguous. It is the responsibility of the grammar designer to ensure these two properties.

Parser combinators can deal with any kind of input as long as this input is a kind of sequence, for example a string or a list of tokens. The general idea behind parser combinators is to transform the input into sets of pairs, like so

$$\underbrace{\text{list of tokens}}_{\text{input}} \Rightarrow \underbrace{\text{set of (parsed input, unparsed input)}}_{\text{output}}$$

In Scala parser combinators are functions of type

$$I \Rightarrow Set[(T, I)]$$

that is they take as input something of type I and return a set of pairs. The first component of these pairs corresponds to what the parser combinator was able to process from the input and the second is the unprocessed part of the input. As we shall see shortly, a parser combinator might return more than one such pair, the idea being that there are potentially several ways how to interpret the input. To simplify matters we will first look at the case where the input to the parser combinators is just strings. As a concrete example, consider the string

We might have a parser combinator which tries to interpret this string as a keyword (if) or as an identifier (iffoo). Then the output will be the set

where the first pair means the parser could recognise if from the input and leaves the rest as 'unprocessed' as the second component of the pair; in the other case it could recognise iffoo and leaves _testbar as unprocessed. If the parser cannot recognise anything from the input, then parser combinators just return the empty set {}. This will indicate something "went wrong"...or more precisely, nothing could be parsed.

The main attraction of parser combinators is that we can easily build parser combinators out of smaller components following very closely the structure of a grammar. In order to implement this in an object-oriented programming language, like Scala, we need to specify an abstract class for parser combinators. This abstract class requires the implementation of the function parse taking an argument of type I and returns a set of type Set[(T, I)].

```
abstract class Parser[I, T] {
   def parse(ts: I): Set[(T, I)]

def parse_all(ts: I): Set[T] =
   for ((head, tail) <- parse(ts); if (tail.isEmpty))
   yield head
}</pre>
```

From the function parse we can then "centrally" derive the function parse_all, which just filters out all pairs whose second component is not empty (that is has still some unprocessed part). The reason is that at the end of the parsing we are only interested in the results where all the input has been consumed and no unprocessed part is left over.

One of the simplest parser combinators recognises just a character, say *c*, from the beginning of strings. Its behaviour can be described as follows:

- if the head of the input string starts with a c, then returns the set $\{(c, tail\ of\ s)\}$, where $tail\ of\ s$ is the unprocessed part of the input string
- otherwise return the empty set {}

The input type of this simple parser combinator for characters is String and the output type Set[(Char, String)]. The code in Scala is as follows:

```
case class CharParser(c: Char) extends Parser[String, Char] {
  def parse(sb: String) =
    if (sb.head == c) Set((c, sb.tail)) else Set()
}
```

The parse function tests whether the first character of the input string sb is equal to c. If yes, then it splits the string into the recognised part c and the unprocessed part sb.tail. In case sb does not start with c then the parser returns the empty set (in Scala Set()).

More interesting are the parser combinators that build larger parsers out of smaller component parsers. For example the alternative parser combinator is as follows: given two parsers, say, p and q, then we apply both parsers to the input (remember parsers are functions) and combine the output (remember they are sets)

```
p(\text{input}) \cup q(\text{input})
```

In Scala we would implement alternative parser combinator as follows

The types of this parser combinator are polymorphic (we just have I for the input type, and T for the output type). The alternative parser builds a new parser out of two existing parsers p and q. Both need to be able to process input of type I and return the same output type Set[(T, I)]. The alternative parser should run the input with the first parser p (producing a set of outputs) and then run the same input with q. The result should be then just the union of both sets, which is the operation ++ in Scala.

The alternative parser combinator already allows us to construct a parser that parses either a character **a** or **b**, as

```
new AltParser(CharParser('a'), CharParser('b'))
```

Scala allows us to introduce some more readable shorthand notation for this, like 'a' || 'b'. We can call this parser combinator with the strings

```
\begin{array}{ccc} \text{input strings} & \text{output} \\ & \textbf{a} & \textbf{c} & \rightarrow & \left\{ (\textbf{a}, \textbf{c}) \right\} \\ & \textbf{b} & \textbf{c} & \rightarrow & \left\{ (\textbf{b}, \textbf{c}) \right\} \\ & \textbf{c} & \textbf{c} & \rightarrow & \left\{ \right\} \end{array}
```

We receive in the first two cases a successful output (that is a non-empty set). In each case, either a or b are in the processed parts, and c in the unprocessed part. Clearly this parser cannot parse anything in the string cc, therefore the empty set.

A bit more interesting is the *sequence parser combinator*. Given two parsers, say, p and q, apply first the input to p producing a set of pairs; then apply q to all the unparsed parts; then combine the results like

```
\{((output_1, output_2), u_2) \mid (output_1, u_1) \in p(input) \land (output_2, u_2) \in q(u_1)\}
```

This can be implemented in Scala as follows:

```
class SeqParser[I, T, S]
          (p: => Parser[I, T],
                q: => Parser[I, S]) extends Parser[I, (T, S)] {
    def parse(sb: I) =
        for ((output1, u1) <- p.parse(sb);
                (output2, u2) <- q.parse(u1))
                yield ((output1, output2), u2)
}</pre>
```

¹There is an interesting detail of Scala, namely the => in front of the types of p and q. They will prevent the evaluation of the arguments before they are used. This is often called *lazy evaluation* of the arguments. We will explain this later.

This parser takes as input two parsers, p and q. It implements parse as follows: let first run the parser p on the input producing a set of pairs (output1, u1). The u1 stands for the unprocessed parts left over by p. Let q run on these unprocessed parts producing again a set of pairs. The output of the sequence parser combinator is then a set containing pairs where the first components are again pairs, namely what the first parser could parse together with what the second parser could parse; the second component is the unprocessed part left over after running the second parser q. Therefore the input type of the sequence parser combinator is as usual I, but the output type is

Scala allows us to provide some shorthand notation for the sequence parser combinator. We can write for example 'a' ~ 'b', which is the parser combinator that first consumes the character a from a string and then b. Three examples of this parser combinator are as follows:

A slightly more complicated parser is ('a' || 'b') ~ 'b' which parses as first character either an a or b followed by a b. This parser produces the following outputs.

input strings output
$$\begin{array}{cccc} \textbf{a} & \textbf{b} & \textbf{c} & \rightarrow & \{((\textbf{a}, \textbf{b}), \textbf{c})\} \\ \textbf{b} & \textbf{b} & \textbf{c} & \rightarrow & \{((\textbf{b}, \textbf{b}), \textbf{c})\} \\ \textbf{a} & \textbf{a} & \textbf{c} & \rightarrow & \{\} \end{array}$$

Two more examples: first consider the parser ('a' \sim 'a') \sim 'a' and the input aaaa:

Notice how the results nest deeper and deeper as pairs (the last a is in the unprocessed part). To consume everything of this string we can use the parser (('a' ~'a') ~ 'a') ~ 'a'. Then the output is as follows:

This is an instance where the parser consumed completely the input, meaning the unprocessed part is just the empty string.

Note carefully that constructing a parser such 'a' || ('a' ~ 'b') will result in a typing error. The first parser has as output type a single character (recall the type of CharParser), but the second parser produces a pair of characters as output. The alternative parser is however required to have both component parsers to have the same type. We will see later how we can build this parser without the typing error.

The next parser combinator does not actually combine smaller parsers, but applies a function to the result of a parser. It is implemented in Scala as follows

This parser combinator takes a parser p with output type T as one argument as well as a function f with type T => S. The parser p produces sets of type (T, I). The FunParser combinator then applies the function f to all the parser outputs. Since this function is of type T => S, we obtain a parser with output type S. Again Scala lets us introduce some shorthand notation for this parser combinator. Therefore we will write p ==> f for it.

How to build parsers using parser combinators?

Implementing an Interpreter