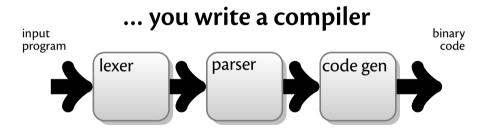
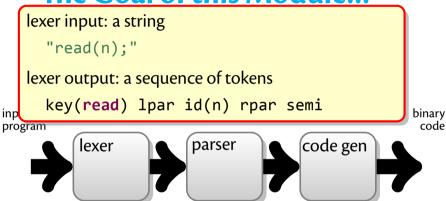
Compilers and Formal Languages

Email: christian.urban at kcl.ac.uk

Slides & Progs: KEATS

1 Introduction, Languages	6 While-Language
2 Regular Expressions, Derivatives	7 Compilation, JVM
3 Automata, Regular Languages	8 Compiling Functional Languages
4 Lexing, Tokenising	9 Optimisations
5 Grammars, Parsing	10 LLVM

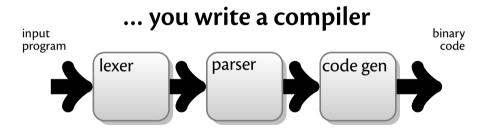


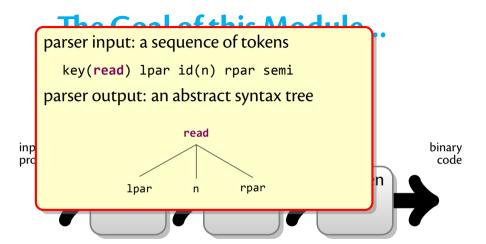


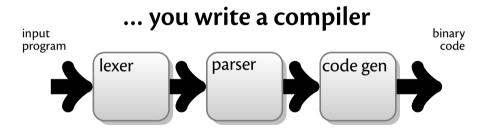
lexer input: a string "read(n);" lexer output: a sequence of tokens key(read) lpar id(n) rpar semi binary program lexer par

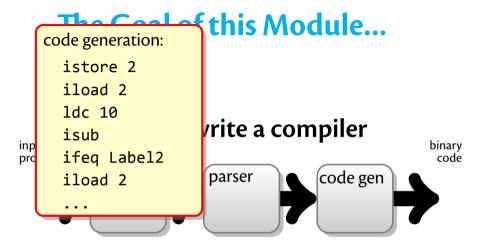
The Goal of this Module... lexer input: a string "read(n);" lexer output: a sequence of tokens key(read) lpar id(n) rpar semi binary program lexer par \Rightarrow keyword $iffoo \Rightarrow identifier$

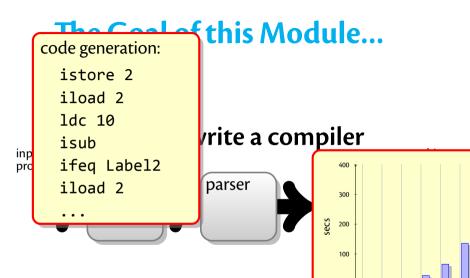
lexing ⇒ recognising words (Stone of Rosetta), King's College London - p. 2/34



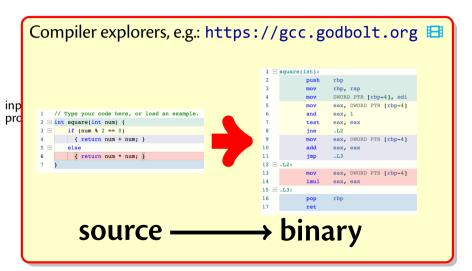




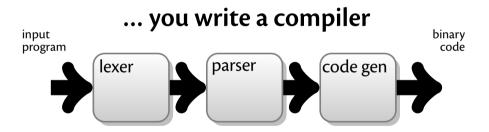




800 1.000 1.200



Compiler explorer for Java: https://javap.yawk.at Code: import java.util.*; stack=1, locals=2, args size=1 import lombok.*: start local 0 // Main this 0: aload 0 1: invokespecial #1 public class Main { 4: iconst 0 public Main() { 5: istore 1 int i = 0: start local 1 // int i i++: 9: return end local 1 // int i end local 0 // Main this byte code source



Why Study Compilers?

John Regehr (Univ. Utah, LLVM compiler hacker) 🖒

"...It's effectively a perpetual employment act for solid compiler hackers."

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 Hardware is getting weirder rather than getting clocked faster.

"Almost all processors are multicores nowadays and it looks like there is increasing asymmetry in resources across cores. Processors come with vector units, crypto accelerators etc. We have DSPs, GPUs, ARM big.little, and Xeon Phi. This is only scratching the surface."

Why Study Compilers?

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"...It's effectively a perpetual employment act for solid compiler hackers."

 We're getting tired of low-level languages and their associated security disasters.

"We want to write new code, to whatever extent possible, in safer, higher-level languages. Compilers are caught right in the middle of these opposing trends: one of their main jobs is to help bridge the large and growing gap between increasingly high-level languages and increasingly wacky platforms."

Why Bother with Compilers?

Boeing 777's: First flight in 1994. They want to achieve triple redundancy for potential hardware

faults. */>

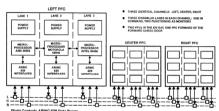
They compile 1 Ada program to

Intel 80486

Motorola 68040 (old Macintosh's)

• AMD 29050 (RISC chips used often in laser printers)

using 3 independent compilers.



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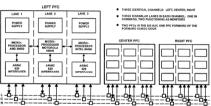
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using 3 independent compilers.

Airbus uses C and static analysers. Recently started using CompCert.



What Do Compilers Do?

Remember BF*** from PEP?

- > ⇒ move one cell right
- \Rightarrow move one cell left
- $+ \Rightarrow$ increase cell by one
- \rightarrow decrease cell by one
- \Rightarrow print current cell
- \Rightarrow input current cell
- $[\Rightarrow loop begin$
- $] \Rightarrow loop end$
 - ⇒ everything else is a comment

A "Compiler" for BF*** to C

```
\Rightarrow ptr++
\prec \Rightarrow ptr--
+ \Rightarrow (*ptr)++
- ⇒ (*ptr)--
\Rightarrow putchar(*ptr)
\Rightarrow *ptr = getchar()
\Rightarrow while(*ptr){
1 \Rightarrow 1
    \Rightarrow ignore everything else
```

```
char field[30000]
char *ptr = &field[15000]
```

Another "Compiler" for BF to C

```
\rightarrow ... \rightarrow ptr += n
\langle ... \langle \Rightarrow ptr -= n \rangle
+...+ \Rightarrow (*ptr) += n
-...- ⇒ (*ptr) -= n
   . ⇒ putchar(*ptr)
   \Rightarrow *ptr = getchar()
   \Rightarrow while(*ptr){
   1 \Rightarrow 1
       \Rightarrow ignore everything else
```

```
char field[30000]
char *ptr = &field[15000]
```

A Brief Compiler History

- Turing Machines, 1936 (a tape as memory)
- Regular Expressions, 1956
- The first compiler for COBOL, 1957 (Grace Hopper)
- But surprisingly research papers are still published nowadays
- "Parsing: The Solved Problem That Isn't"



Grace Hopper

(she made it to David Letterman's Tonight Show 🖒)

Exams will be online:

- final exam in January (30%)
- mid-term shortly after Reading Week (10%)
- weekly engagement (10%)

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Weekly Homework (optional):

- uploaded on KEATS, send answers via email, responded individually
- all questions in the exam and mid-term will be from the HW!!

Coursework (5 accounting for 45%):

- matcher (5%)
- lexer (8%)
- parser / interpreter (10%)
- JVM compiler (10%)
- LLVM compiler (12%)

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Lectures 1 - 5

transforming strings into structured data

Lexing

based on regular expressions

(recognising "words")

Parsing

(recognising "sentences")



Stone of Rosetta

Lectures 1 - 5

transforming strings into structured data

Lexing

based on regular expressions

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Stone of Rosetta

Lectures 5 - 10

code generation for a small imperative and a small functional language

Interpreters

(directly runs a program)

Compilers

(generate JVM code and LLVM-IR code)





Familiar Regular Expresssions

$$[a-z0-9_{.-}]+ @ [a-z0-9_{.-}]+ . [a-z_{.}]{2,6}$$

```
matches 0 or more times
re*
          matches 1 or more times
re+
re?
          matches 0 or 1 times
re{n}
          matches exactly n number of times
          matches at least n and at most m times
re{n,m}
           matches any single character inside the brackets
[\ldots]
          matches any single character not inside the brackets
[^...]
a-z A-Z character ranges
          matches digits; equivalent to [0-9]
\d
           matches every character except newline
          groups regular expressions and remembers the
(re)
           matched text
```

Some "innocent" examples

Let's try two examples

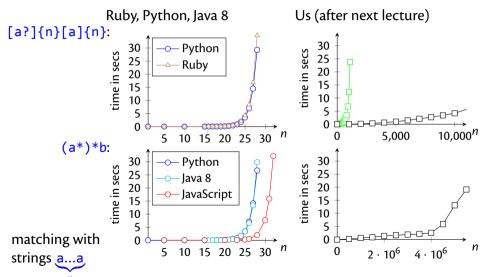
```
(a*)*b [a?]{n}[a]{n}
```

Some "innocent" examples

Let's try two examples

and match them with strings of the form

Why Bother with Regexes?



Incidents

 a global outage on 2 July 2019 at Cloudflare (first one for six years)

```
(?:(?:\"|'|\]|\\|\d|(?:nan|infinity|true|false|
null|undefined|symbol|math)|\`|\-|\+)+[)]*;?((?:\s
|-|~|!|{}|\|\||\+)*.*(?:.*=.*)))
```



It serves more web traffic than Twitter, Amazon, Apple, Instagram, Bing & Wikipedia combined.

 on 20 July 2016 the Stack Exchange webpage went down because of an evil regular expression

Evil Regular Expressions

- Regular expression Denial of Service (ReDoS)
- Some evil regular expressions:

```
[a?]{n} [a]{n}(a*)*b([a-z]+)*(a + aa)*(a + a?)*
```

- sometimes also called catastrophic backtracking
- this is a problem for Network Intrusion Detection systems, Cloudflare, StackExchange, Atom editor
- https://vimeo.com/112065252

(Basic) Regular Expressions

Their inductive definition:

```
nothing
 \begin{vmatrix} 1 \\ c \\ r_1 + r_2 \\ r_1 \cdot r_2 \end{vmatrix}  alternative sequence  \begin{vmatrix} r^* \\ r^* \end{vmatrix}  star (z_F)
                                                    empty string / "" / []
                                                    alternative / choice
                                                    star (zero or more)
```

```
(B
Their
```

```
abstract class Rexp
case object ZERO extends Rexp
case object ONE extends Rexp
case class CHAR(c: Char) extends Rexp
case class ALT(r1: Rexp, r2: Rexp) extends Rexp
case class SEQ(r1: Rexp, r2: Rexp) extends Rexp
case class STAR(r: Rexp) extends Rexp
```

```
r ::= 0nothing1empty string / "" / []ccharacterr_1 + r_2alternative / choicer_1 \cdot r_2sequencer^*star (zero or more)
```

Strings

...are lists of characters. For example "hello"

the empty string: [] or ""

the concatenation of two strings:

$$s_1 @ s_2$$

$$foo @ bar = foobar$$

 $baz @ [] = baz$

Languages, Strings

Strings are lists of characters, for example[], abc (Pattern match: c::s)

• A language is a set of strings, for example

Concatenation of strings and languages

foo @ bar = foobar
$$A @ B \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in A \land s_2 \in B\}$$

```
L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}
L(\mathbf{1}) \stackrel{\text{def}}{=} \{[]\}
L(c) \stackrel{\text{def}}{=} \{[c]\}
L(r_1 + r_2) \stackrel{\text{def}}{=} L(r_1) \cup L(r_2)
L(r_1 \cdot r_2) \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}
L(r^*) \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in L(r_1) \land s_2 \in L(r_2)\}
```

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     L(r)^0 \stackrel{\text{def}}{=} \{[]\}
L(r)^{n+1} \stackrel{\text{def}}{=} L(r) @ L(r)^n (append on sets)
                                                    \{s_1@s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}
```

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           L(r^*) \stackrel{\text{def}}{=} \bigcup_{0 \le n} L(r)^n
     L(r)^0 \stackrel{\text{def}}{=} \{[]\}
L(r)^{n+1} \stackrel{\text{def}}{=} L(r) @ L(r)^n (append on sets)
                                                     \{s_1@s_2 \mid s_1 \in L(r) \land s_2 \in L(r)^n\}
```

The Meaning of Matching

A regular expression *r* matches a string *s* provided

$$s \in L(r)$$

...and the point of the next lecture is to decide this problem as fast as possible (unlike Python, Ruby, Java)

The Power Operation

• The *n*th Power of a language:

$$A^{0} \stackrel{\text{def}}{=} \{[]\}$$

$$A^{n+1} \stackrel{\text{def}}{=} A @ A^{n}$$

For example

$$A^4 = A@A@A@A$$
 (@ {[]})
 $A^1 = A$ (@ {[]})
 $A^0 = \{[]\}$

Questions

• Say $A = \{[a], [b], [c], [d]\}.$

How many strings are in A^4 ?

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• Say $A = \{[a], [b], [c], [d]\}.$

How many strings are in A^4 ?

What if $A = \{[a], [b], [c], []\};$ how many strings are then in A^4 ?

Languages (Sets of Strings)

• A Language is a set of strings, for example

Concatenation for strings and languages

foo @ bar = foobar
$$A @ B \stackrel{\text{def}}{=} \{s_1 @ s_2 \mid s_1 \in A \land s_2 \in B\}$$

For example
$$A = \{foo, bar\}$$
, $B = \{a, b\}$

$$A @ B = \{fooa, foob, bara, barb\}$$

Two Corner Cases

$$A@\{[]\}=?$$

Two Corner Cases

$$A@\{[]\}=?$$

$$A@\{\}=?$$

...all the strings a regular expression can match.

$$L(\mathbf{0}) \stackrel{\text{def}}{=} \{\}$$

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$$L(r_1 + r_2) \stackrel{\text{def}}{=} L(r_1) \cup L(r_2)$$

$$L(r_1 \cdot r_2) \stackrel{\text{def}}{=} L(r_1) @ L(r_2)$$

$$L(r^*) \stackrel{\text{def}}{=}$$

L is a function from regular expressions to sets of strings (languages):

$$L: Rexp \Rightarrow Set[String]$$

The Power Operation

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$$A^4 = A@A@A@A$$
 (@ { [] }]
 $A^1 = A$ (@ { [] }]
 $A^0 = \{ [] \}$

The Star Operation

• The **Kleene Star** of a language:

$$A\star \stackrel{\mathrm{def}}{=} \bigcup_{0\leq n} A^n$$

This expands to

$$A^0 \cup A^1 \cup A^2 \cup A^3 \cup A^4 \cup \dots$$

or

$$\{[]\} \cup A \cup A@A \cup A@A@A \cup A@A@A@A \cup \dots$$

Written Exam

- Accounts for 80%.
- The question "Is this relevant for the exam?" is very demotivating for the lecturer!
- Deal: Whatever is in the homework (and is not marked "optional") is relevant for the exam.
- Each lecture has also a handout. There are also handouts about notation and Scala.

Coursework

Accounts for 20%. Two strands. Choose one!

Strand 1

- 4 programming tasks:
 - matcher (4%, 11.10.)
 - lexer (5%, 04.11.)
 - parser (5%, 22.11.)
 - compiler (6%, 13.12.)
- in any lang. you like, but I want to see the code

Strand 2

- one task: prove the correctness of a regular expression matcher in the <u>Isabelle</u> theorem prover
- 20%, submission on 13.12.
- Solving more than one strand will **not** give you more marks.

Questions?