

Compilers and Formal Languages

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Slides: KEATS (also home work is there)

Compilers & Boeings 777

First flight in 1994. They want to achieve triple redundancy in hardware faults.

They compile 1 Ada program to

- Intel 80486
- Motorola 68040 (old Macintosh's)
- AMD 29050 (RISC chips used often in laser printers)

using 3 independent compilers.

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Airbus uses C and static analysers. Recently started using CompCert.

seL4 / Isabelle

- verified a microkernel operating system (≈ 8000 lines of C code)
- US DoD has competitions to hack into drones; they found that the isolation guarantees of seL4 hold up
- CompCert and seL4 sell their code

POSIX Matchers

- Longest match rule (“maximal munch rule”): The longest initial substring matched by any regular expression is taken as the next token.

i f f o o _ b l a

- Rule priority: For a particular longest initial substring, the first regular expression that can match determines the token.

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Kuklewicz: most POSIX matchers are buggy
http://www.haskell.org/haskellwiki/Regex_Posix

$der\ c\ (\mathbf{0})$	$\stackrel{\text{def}}{=} \mathbf{0}$
$der\ c\ (\mathbf{1})$	$\stackrel{\text{def}}{=} \mathbf{0}$
$der\ c\ (d)$	$\stackrel{\text{def}}{=} \text{if } c = d \text{ then } \mathbf{1} \text{ else } \mathbf{0}$
$der\ c\ (r_1 + r_2)$	$\stackrel{\text{def}}{=} (der\ c\ r_1) + (der\ c\ r_2)$
$der\ c\ (r_1 \cdot r_2)$	$\stackrel{\text{def}}{=} \text{if } nullable(r_1) \\ \text{then } ((der\ c\ r_1) \cdot r_2) + (der\ c\ r_2) \\ \text{else } (der\ c\ r_1) \cdot r_2$
$der\ c\ (r^*)$	$\stackrel{\text{def}}{=} (der\ c\ r) \cdot (r^*)$
$der\ c\ (r^{\{n\}})$	$\stackrel{\text{def}}{=} \text{if } n = 0 \text{ then } \mathbf{0} \\ \text{else if } nullable(r) \text{ then } (der\ c\ r) \cdot (r^{\{\uparrow n-1\}}) \\ \text{else } (der\ c\ r) \cdot (r^{\{n-1\}})$
$der\ c\ (r^{\{\uparrow n\}})$	$\stackrel{\text{def}}{=} \text{if } n = 0 \text{ then } \mathbf{0} \\ \text{else } (der\ c\ r) \cdot (r^{\{\uparrow n-1\}})$

Proofs about Rexp

Remember their inductive definition:

$$r ::= \begin{array}{l} \mathbf{0} \\ \mathbf{I} \\ c \\ r_1 \cdot r_2 \\ r_1 + r_2 \\ r^* \\ r\{n\} \\ r\{\uparrow n\} \end{array}$$

If we want to prove something, say a property $P(r)$, for all regular expressions r then ...

Proofs about Rexp (2)

- P holds for $\mathbf{0}$, $\mathbf{1}$ and c
- P holds for $r_1 + r_2$ under the assumption that P already holds for r_1 and r_2 .
- P holds for $r_1 \cdot r_2$ under the assumption that P already holds for r_1 and r_2 .
- P holds for r^* under the assumption that P already holds for r .
- ...

Proofs about Strings

If we want to prove something, say a property $P(s)$, for all strings s then ...

- P holds for the empty string, and
- P holds for the string $c::s$ under the assumption that P already holds for s

Correctness of the Matcher

- We want to prove

matches r s if and only if $s \in L(r)$

where *matches r s* $\stackrel{\text{def}}{=} \text{nullable}(\text{ders } s \text{ } r)$

Correctness of the Matcher

- We want to prove

matches r s if and only if $s \in L(r)$

where *matches r s* $\stackrel{\text{def}}{=} \text{nullable}(\text{ders } s r)$

- We can do this, if we know

$$L(\text{der } c r) = \text{Der } c (L(r))$$

Some Lemmas

- $Der\ c\ (A \cup B) = (Der\ c\ A) \cup (Der\ c\ B)$
- If $[\] \in A$ then
$$Der\ c\ (A @ B) = (Der\ c\ A) @ B \cup (Der\ c\ B)$$
- If $[\] \notin A$ then
$$Der\ c\ (A @ B) = (Der\ c\ A) @ B$$
- $Der\ c\ (A^*) = (Der\ c\ A) @ A^*$

(interesting case)

Why?

Why does $Der\ c\ (A^*) = (Der\ c\ A) @ A^*$ hold?

$$\begin{aligned} Der\ c\ (A^*) &= Der\ c\ (A^* - \{\emptyset\}) \\ &= Der\ c\ ((A - \{\emptyset\}) @ A^*) \\ &= (Der\ c\ (A - \{\emptyset\})) @ A^* \\ &= (Der\ c\ A) @ A^* \end{aligned}$$

using the facts $Der\ c\ A = Der\ c\ (A - \{\emptyset\})$ and
 $(A - \{\emptyset\}) @ A^* = A^* - \{\emptyset\}$

POSIX Spec

$$\overline{\quad} \quad \square \in \mathbf{I} \rightarrow \textit{Empty}$$

$$\overline{\quad} \quad c \in c \rightarrow \textit{Char}(c)$$

$$\frac{s \in r_I \rightarrow v}{s \in r_I + r_2 \rightarrow \textit{Left}(v)}$$

$$\frac{s \in r_2 \rightarrow v \quad s \notin L(r_I)}{s \in r_I + r_2 \rightarrow \textit{Right}(v)}$$

$$s_I \in r_I \rightarrow v_I$$

$$s_2 \in r_2 \rightarrow v_2$$

$$\neg(\exists s_3 s_4. s_3 \neq \square \wedge s_3@s_4 = s_2 \wedge s_I@s_3 \in L(r_I) \wedge s_4 \in L(r_2))$$

$$\frac{}{s_I@s_2 \in r_I \cdot r_2 \rightarrow \textit{Seq}(v_I, v_2)}$$

...

Sulzmann & Lu Paper

- I have no doubt the algorithm is correct — the problem is I do not believe their proof.

“How could I miss this? Well, I was rather careless when stating this Lemma :)

Great example how formal machine checked proofs (and proof assistants) can help to spot flawed reasoning steps.”

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