

# Automata and Formal Languages (4)

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Slides: KEATS (also home work is there)

# Regexps and Automata

Thompson's subset  
construction construction

**Regexps → NFAs → DFAs**

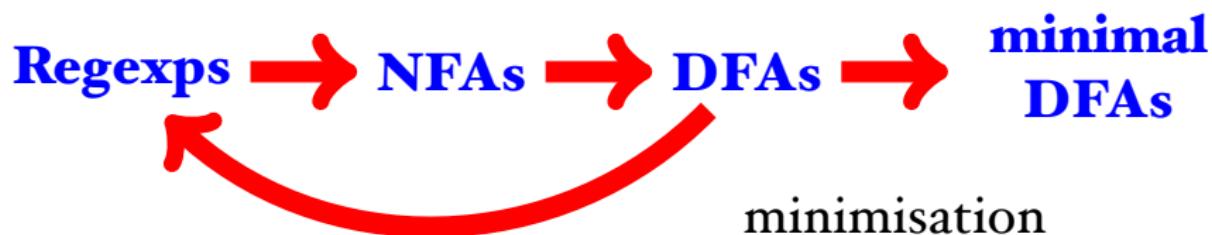
# Regexps and Automata

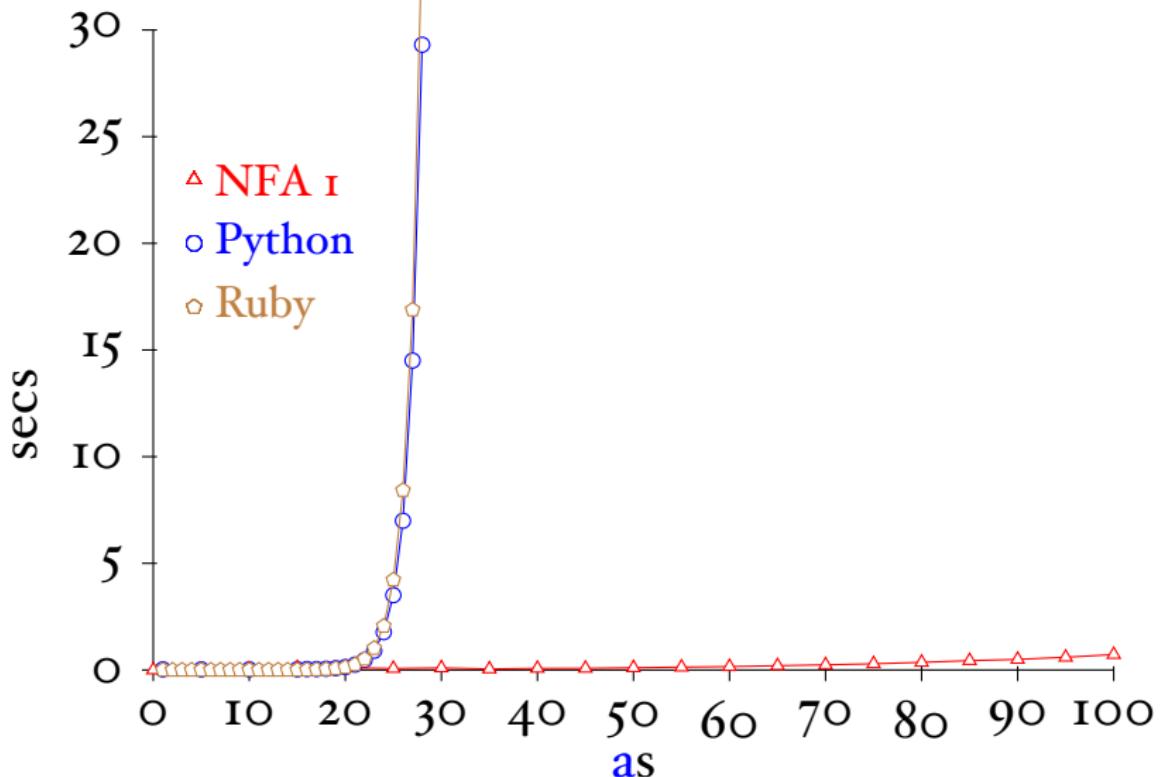
Thompson's      subset  
construction   construction

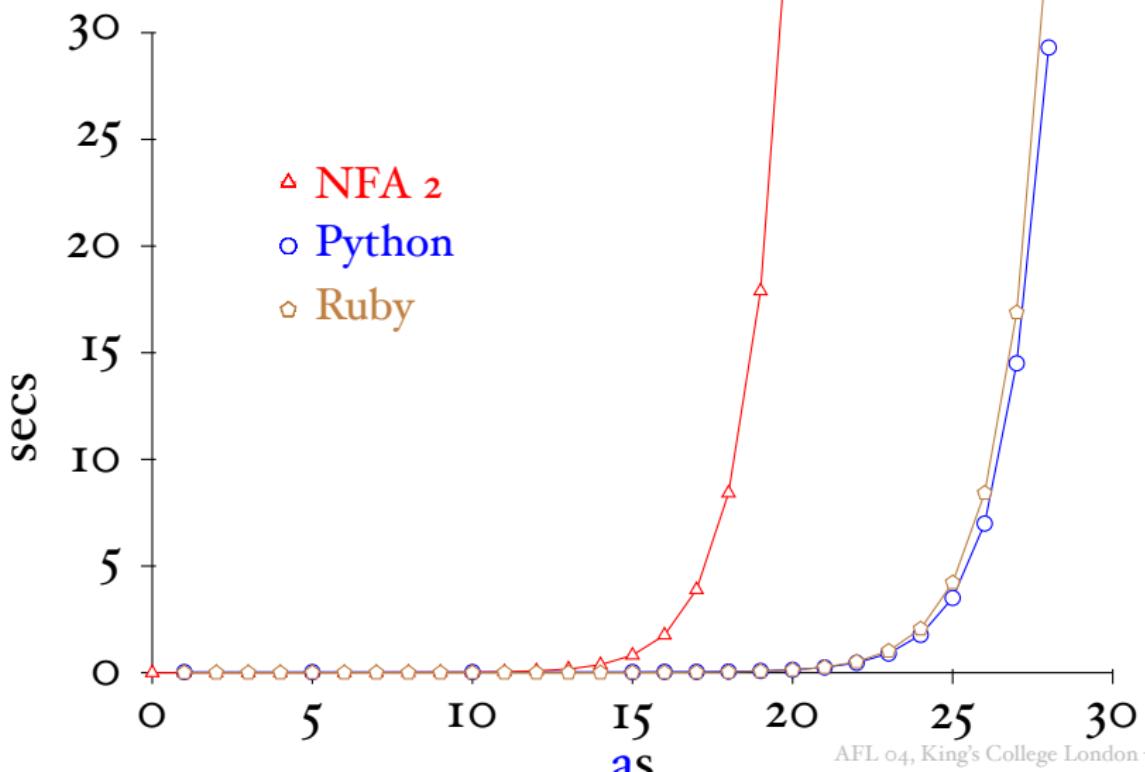


# Regexps and Automata

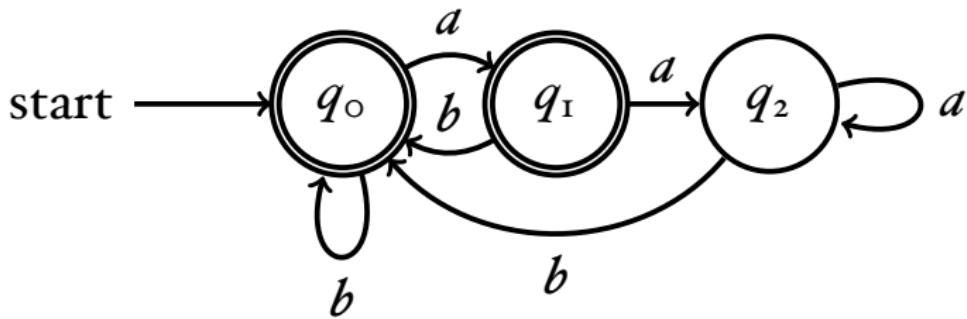
Thompson's construction      subset construction

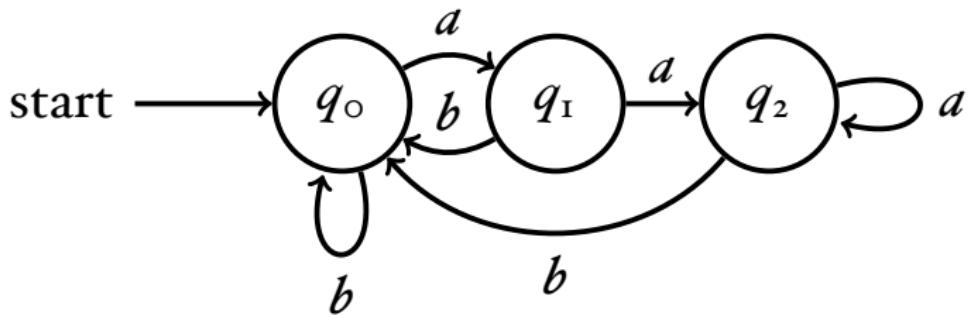


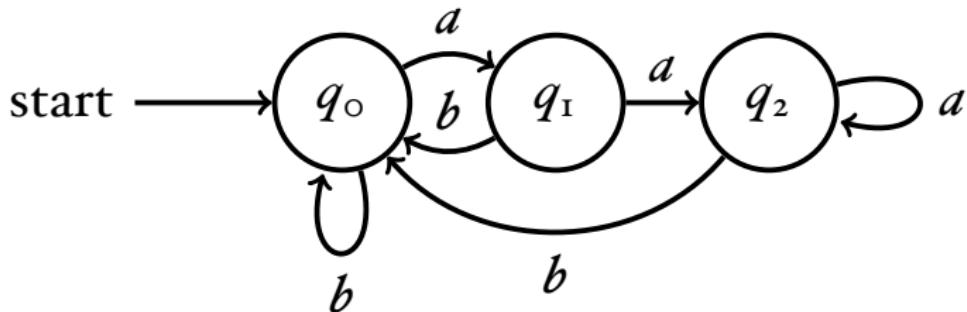
$$(a? \{n\}) \cdot a\{n\}$$


$$(a? \{n\}) \cdot a\{n\}$$


# DFA to Rexp



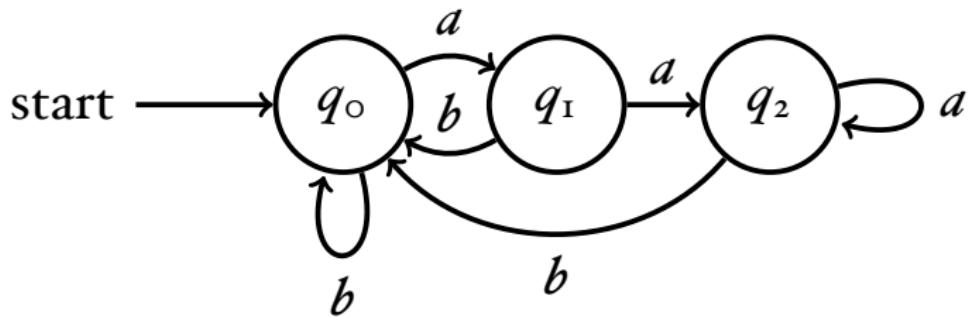


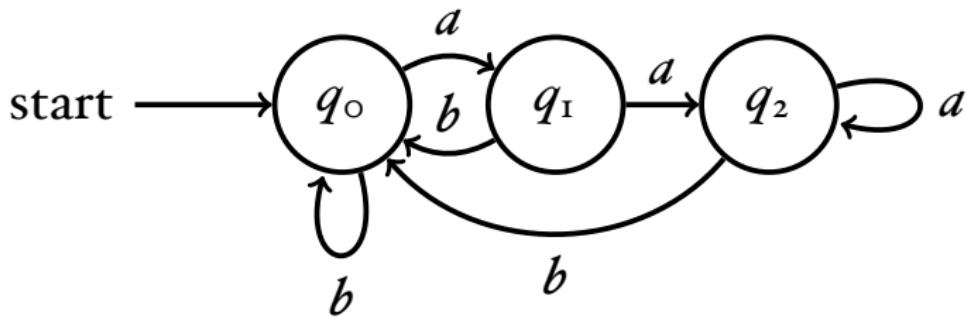


$$q_0 = 2q_0 + 3q_1 + 4q_2$$

$$q_1 = 2q_0 + 3q_1 + 1q_2$$

$$q_2 = 1q_0 + 5q_1 + 2q_2$$

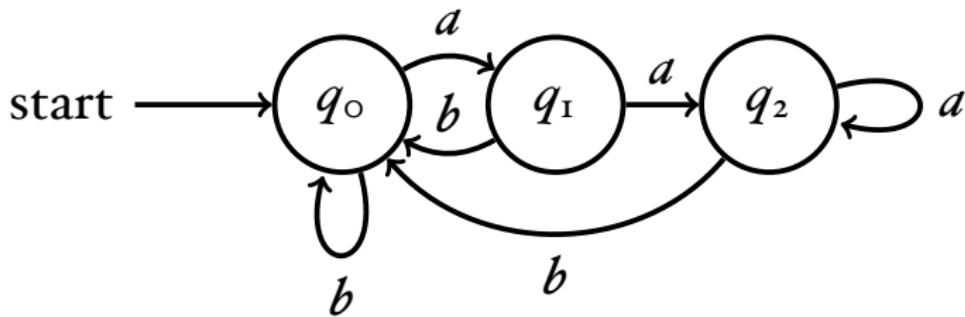




$$q_o = \epsilon + q_o b + q_I b + q_2 b$$

$$q_I = q_o a$$

$$q_2 = q_I a + q_2 a$$



$$q_0 = \epsilon + q_0 b + q_I b + q_2 b$$

$$q_I = q_0 a$$

$$q_2 = q_I a + q_2 a$$

Arden's Lemma:

If  $q = qr + s$  then  $q = sr^*$

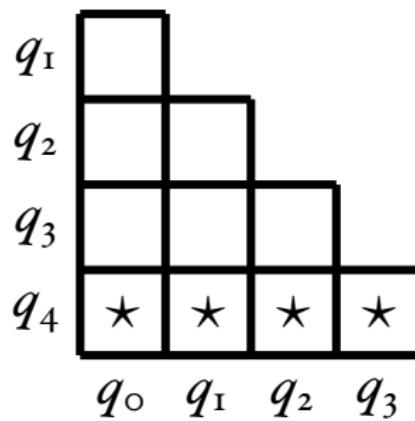
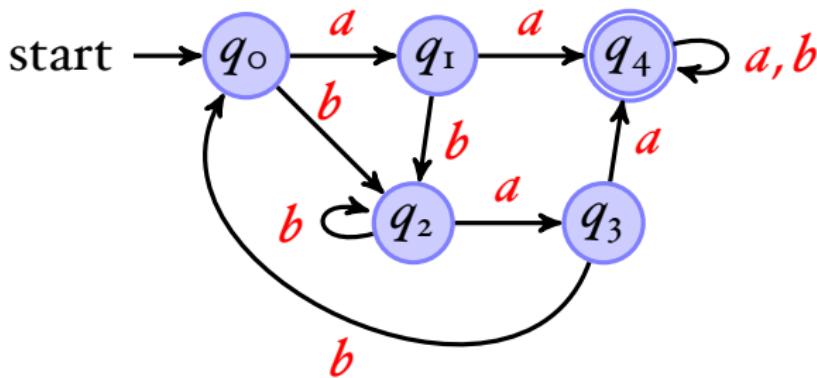
# DFA Minimisation

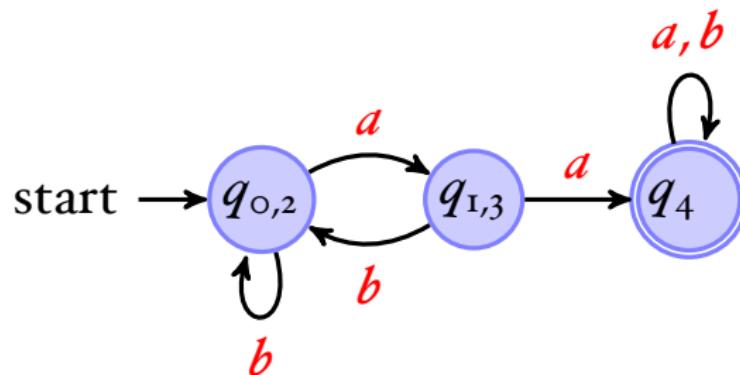
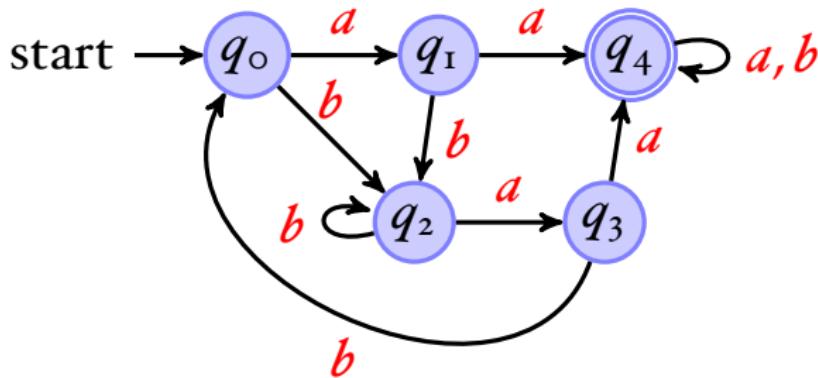
- ➊ Take all pairs  $(q, p)$  with  $q \neq p$
- ➋ Mark all pairs that accepting and non-accepting states
- ➌ For all unmarked pairs  $(q, p)$  and all characters  $c$  test whether

$$(\delta(q, c), \delta(p, c))$$

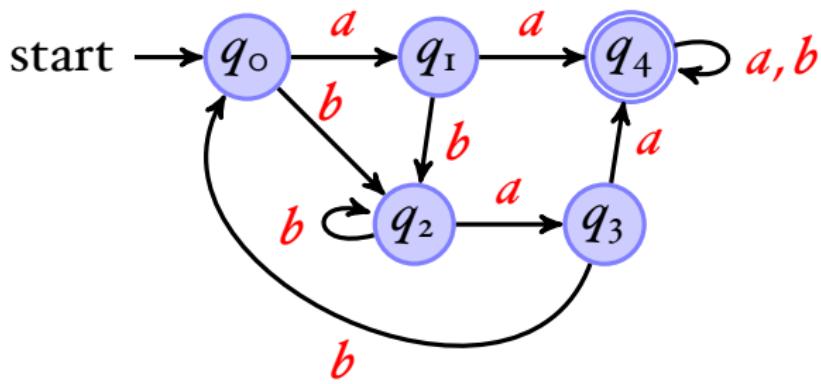
are marked. If yes, then also mark  $(q, p)$ .

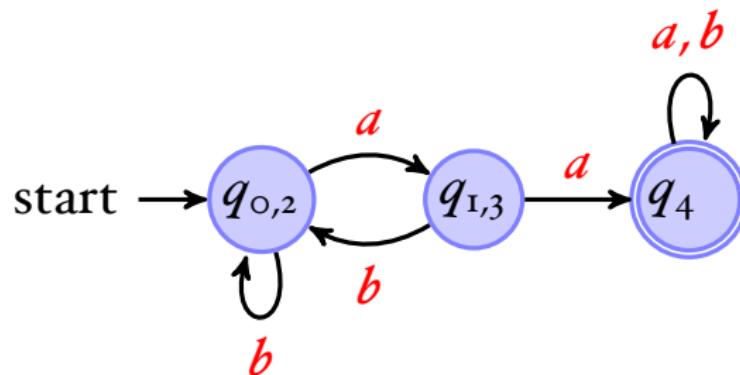
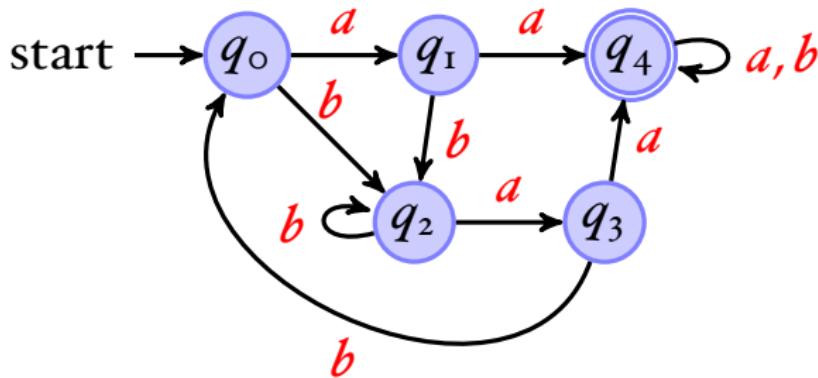
- ➍ Repeat last step until no change.
- ➎ All unmarked pairs can be merged.





minimal automaton





minimal automaton

- Assuming you have the alphabet  $\{a, b, c\}$
- Give a regular expression that can recognise all strings that have at least one  $b$ .